

# IGCSE Edexcel Syllabus

## Worksheets

Questions

### Grades 1 to 5

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

#### *Instructions for use*

Clicking on something like this **Grade 4** will take you to the Grade 4 clip numbers and titles.



Clicking on something like this **Compound Units. . . . . 142** will take you to Worksheet 142.



Clicking on something like this 

©MathsWatch	Clip 142
Grade 4 questions	

 will take you back to the contents page.





Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 1 Foundation and Higher

Place Value . . . . .	1
Ordering Integers . . . . .	2
Ordering Decimals . . . . .	3
Reading Scales . . . . .	4
Simple Mathematical Notation . . . . .	5
Interpreting Real-Life Tables . . . . .	6
Introduction to Algebraic Conventions . . . . .	7
Coordinates . . . . .	8
Simple Geometric Definitions. . . . .	9
Polygons . . . . .	10
Symmetries . . . . .	11
Congruent Shapes. . . . .	12
Names of Angles . . . . .	13
The Probability Scale . . . . .	14
Tally Charts and Bar Charts . . . . .	15
Pictograms . . . . .	16

Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 2 Foundation and Higher

Adding Integers and Decimals . . . . .	17
Subtracting Integers and Decimals . . . . .	18
Multiplying Integers . . . . .	19
Dividing Integers . . . . .	20
Inverse Operations. . . . .	21
Negatives in Real Life . . . . .	22
Introduction to Fractions. . . . .	23 A/B
Equivalent Fractions. . . . .	24
Simplifying Fractions . . . . .	25
Half-Way Values. . . . .	26
Factors, Multiples and Primes . . . . .	27
Introduction to Powers/Indices . . . . .	28
Multiply and Divide by Powers of 10 . . . . .	29
Rounding to the Nearest 10, 100 etc . . . . .	30
Rounding to Decimal Places . . . . .	31
Ratio - Introduction . . . . .	32
Percentages - Introduction . . . . .	33
Direct Proportion - Introduction . . . . .	34
Value for Money. . . . .	35
Algebraic Simplification. . . . .	36 A/B/C/D
Function Machines . . . . .	37
Generating a Sequence - Term to Term . . . . .	38



Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 2 Foundation and Higher

Properties of Solids . . . . .	.39
Angles on a Line and at a Point . . . . .	.40
Measuring and Drawing Angles . . . . .	.41
Drawing a Triangle Using a Protractor . . . . .	.42
Reflections . . . . .	.43
Rotations . . . . .	.44
Translations . . . . .	.45
Perimeters . . . . .	.46
Area of a Rectangle . . . . .	.47
Area of a Triangle. . . . .	.48
Area of a Parallelogram . . . . .	.49
Area of a Trapezium. . . . .	.50
Listing Outcomes . . . . .	.51
Calculating Probabilities. . . . .	.52
Mutually Exclusive Events . . . . .	.53
Data - Discrete and Continuous . . . . .	.54
Frequency Tables and Diagrams . . . . .	.55 A/B/C

Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 3 Foundation and Higher

Multiplying Decimals . . . . .	56
Dividing Decimals. . . . .	57
Four Rules of Negatives. . . . .	58
Comparing Fractions . . . . .	59
Adding and Subtracting Fractions . . . . .	60
Finding a Fraction of an Amount . . . . .	61
Multiplying Fractions . . . . .	62
Dividing Fractions. . . . .	63
BODMAS/BIDMAS. . . . .	64
Reciprocals . . . . .	65
Calculator Questions . . . . .	66
Product of Primes. . . . .	67
Squares, Cubes and Roots . . . . .	68
Working with Indices . . . . .	69
Decimals and Fractions . . . . .	70
Fractions, Percentages, Decimals . . . . .	71
Reciprocals. . . . .	72
Percentage of an Amount . . . . .	73 A/B
Change to a Percentage . . . . .	74 A/B/C
Rounding to Significant Figures . . . . .	75
Estimating Answers . . . . .	76
Exchanging Money . . . . .	77



Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 3 Foundation and Higher

Expanding Brackets . . . . .	78
Simple Factorisation . . . . .	79
Substitution . . . . .	80
Straight Line Graphs . . . . .	81 A/B/C
The Gradient of a Line . . . . .	82
Sketching Functions . . . . .	83
Solving Equations . . . . .	84 A/B
Subject of a Formula . . . . .	85 A/B
Generate a Sequence from the <i>n</i> th Term . . . . .	86
Metric Conversions . . . . .	87
Problems on Coordinate Axes . . . . .	88
Surface Area of a Prism . . . . .	89 A/B
Volume of a Cuboid . . . . .	90
Circle Definitions . . . . .	91
Angles in a Triangle . . . . .	92
Properties of Special Triangles . . . . .	93
Angles and Parallel Lines . . . . .	94 A/B/C
Angle Sum of Polygons . . . . .	95 A/B
Two-Way Tables . . . . .	96
Averages and the Range . . . . .	97
Experimental Probabilities . . . . .	98
Possibility Spaces . . . . .	99

Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 4 Foundation and Higher

Index Notation . . . . .	100	A/B
Standard Form . . . . .	101	
Highest Common Factor (HCF) . . . . .	102	
Lowest Common Multiple (LCM) . . . . .	103	A/B
Introduction to Bounds. . . . .	104	
Sharing Using Ratio . . . . .	105	
Ratios, Fractions and Graphs . . . . .	106	
Increase/Decrease by a Percentage. . . . .	107	
Simple Interest. . . . .	108	
Midpoint of a Line on a Graph . . . . .	109	
Expanding and Simplifying Brackets . . . . .	110	A/B
Solving Equations . . . . .	111	
Rearranging Simple Formulae . . . . .	112	
Forming Formulae and Equations . . . . .	113	A/B/C
Inequalities on a Number Line . . . . .	114	
Drawing Quadratic Graphs. . . . .	115	A/B/C/D
Distance-Time Graphs . . . . .	116	
Finding the $n$ th Term. . . . .	117	A/B/C
Drawing a Triangle Using Compasses . . . . .	118	
Bisecting a Line or an Angle . . . . .	119	A/B
Enlargements . . . . .	120	
Area of a Circle. . . . .	121	
Circumference of a Circle . . . . .	122	A/B/C
Volume of a Prism. . . . .	123	A/B



Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 4 Foundation and Higher

Tangents, Arcs, Sectors and Segments . . . . .	124
Compound Units - Speed . . . . .	125
Pythagoras' Theorem . . . . .	126 A/B/C
Bearings . . . . .	127 A/B
Venn Diagrams - Introduction. . . . .	128
Pie Charts . . . . .	129
Averages from a Table. . . . .	130



Take me to . . .

Grade 1

Grade 2

Grade 3

Grade 4

Grade 5

## Grade 5 Foundation and Higher

Negative Indices. . . . .	131
Percentage Change . . . . .	132
Reverse Percentage Problems. . . . .	133
Compound Interest and Depreciation. . . . .	134
Ratio Questions . . . . .	135
Mathematical Reasoning . . . . .	136
Factorising and Solving Quadratics . . . . .	137
The Difference of Two Squares . . . . .	138
Equation of a Straight Line - $y = mx + c$ . . . . .	139
Roots and Turning Points of Quadratics . . . . .	140
Simultaneous Equations Algebraically . . . . .	141
Simultaneous Equations Graphically . . . . .	142
Solving Linear Inequalities . . . . .	143 A/B
Inequalities on a Graph . . . . .	144
Compound Units - Density. . . . .	145
Compound Units - Pressure . . . . .	146
Similar Shapes . . . . .	147 A/B/C
Trigonometry . . . . .	148 A/B/C/D/E
Circle Theorems - Introduction. . . . .	149
Venn Diagrams - Notation. . . . .	150
Estimate for the Mean. . . . .	151

- 1)
  - a) Write the number forty five thousand, two hundred and seventy three in figures.
  - b) Write the number five thousand, one hundred and three in figures.
  - c) Write the number three hundred thousand, seven hundred and ninety one in figures.
  - d) Write the number two and a half million in figures.
  - e) Write the number one and three quarter million in figures.
  
- 2) Write the following numbers in words
  - a) 1 250
  - b) 3 502
  - c) 72 067
  - d) 192 040
  - e) 30 000 000
  
- 3)
  - a) Write down the value of the 7 in the number 3 752.
  - b) Write down the value of the 6 in the number 56 025.
  - c) Write down the value of the 2 in the number 99 723.
  - d) Write down the value of the 5 in the number 258 610.
  - e) Write down the value of the 2 in the number 1 253 549.
  
- 4) What is the value of the digit 7 in 38.1472?  
 Choose, and circle, the correct answer from the following:

$$\frac{7}{10}$$

$$\frac{7}{100}$$

$$\frac{7}{1000}$$

$$\frac{7}{10000}$$

Put these numbers in order, starting with the smallest:

1) 74, 57, 38, 8, 61

2) 39, 84, 11, 128, 24

3) 76, 102, 12, 140, 73

4) 3, -2, -7, 10, -1

5) -3, -11, 1, -5, 7

6) -4, 6, 0, -6, -1

7) 205, 2005, 105, 55, 5005

8) 83, -61, -42, 65, -14

1) Put these amounts of money in order, starting with the smallest:

a) £4.50, £3.82, £4.05, £3.99, £3.54

b) £1.25, £2.41, £1.24, £2.04, £1.99

c) £15.83, £24.18, £13.99, £46.01, £46.10

2) Circle the smallest number: 0.1, 0.09, 0.99, 0.15, 0.11

3) Put these numbers in order, starting with the smallest:

2.01, 2.45, 2.14, 2.006, 2.405

4) Put these numbers in order, starting with the smallest:

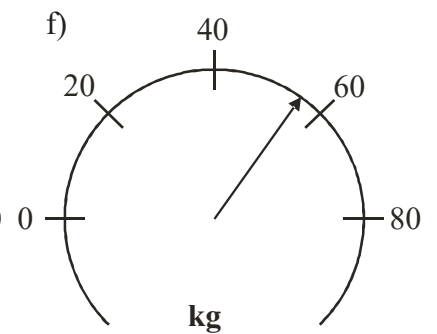
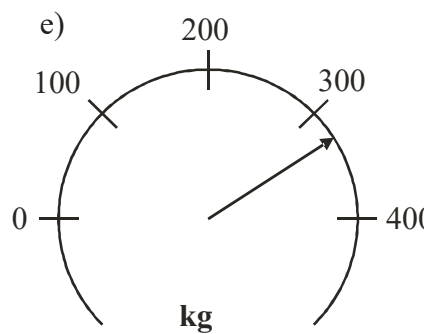
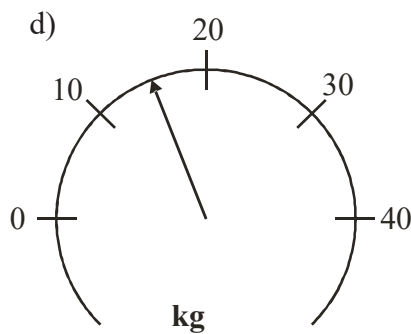
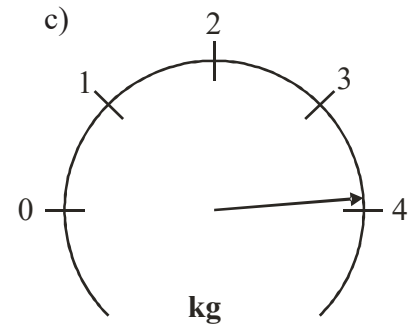
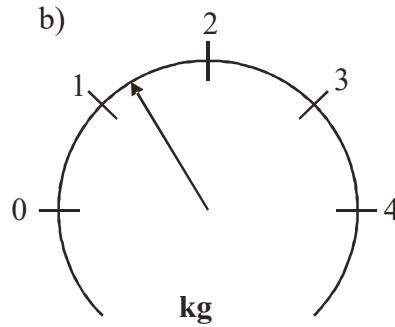
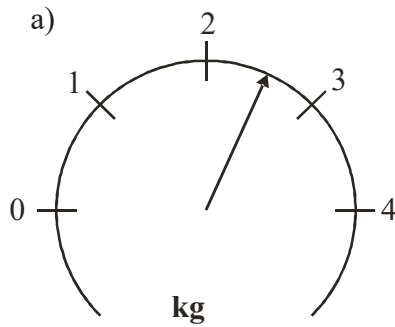
0.76, 0.668, 0.608, 0.099, 0.909

5) Put these numbers in order, starting with the smallest:

5.004, 4.889, 4.099, 5.002, 4.095

## Reading Scales

1) Estimate the reading on each of these scales:



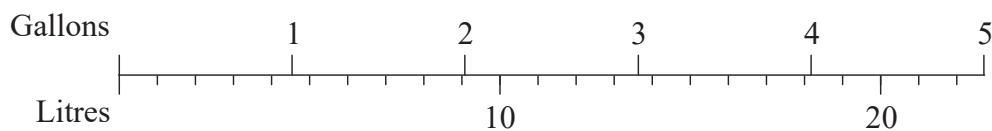
2) This scale shows degrees Centigrade.



a) What temperature is the arrow pointing to?

b) Draw an arrow which points to  $-17^{\circ}\text{C}$ .

3) This is a diagram for converting between gallons and litres.



Use the diagram to convert

a) 3 gallons to litres.

b) 4.5 gallons to litres.

c) 6 litres to gallons.

- 1) For each mathematical sign, below, write a brief description of the sign.  
The first one has already been done.

a)  $<$  less than

b)  $\geq$  \_\_\_\_\_

c)  $>$  \_\_\_\_\_

d)  $\leq$  \_\_\_\_\_

e)  $\neq$  \_\_\_\_\_

- 2) Insert one of the two symbols  $<$  or  $>$  to make the following statements true:

a)  $8 \dots 5$

b)  $-4 \dots -6$

c)  $2.08 \dots 2.8$

d)  $8 + 3 \dots 2 + 7$

e)  $2 \times 7 \dots 5 \times 8$

- 3) You must be at least 1.6 m tall to ride on a rollercoaster at Romy Park.  
Circle the correct description of this out of the following:

Height  $< 1.6$  m

Height  $\leq 1.6$  m

Height  $= 1.6$  m

Height  $\geq 1.6$  m

Height  $> 1.6$  m

- 1) Calculate the difference in hours and minutes between 9.30 am and 2.45 pm.
- 2) Calculate the difference in hours and minutes between 11 35 and 13 25.
- 3) The table shows the distances in kilometres between some cities in the USA.

San Francisco			
4827	New York		
4990	2132	Miami	
668	4541	4375	Los Angeles
3493	1352	2183	3366 Chicago

- a) Write down the distance between San Francisco and Miami.
- One of the cities in the table is 4541 km from Los Angeles.
- b) Write down the name of this city.
  - c) Write down the name of the city which is furthest from Chicago.
- 4) Here is part of a train timetable

Manchester	05 15	06 06	06 45	07 05	07 15	07 46
Stockport	05 26	06 16	06 55	07 15	07 25	07 55
Macclesfield	05 39	06 29	07 08		07 38	08 08
Stoke	05 54	06 45	07 24		07 54	08 24
Stafford	06 12		07 41		08 11	
Euston	08 09	08 26	09 06	09 11	09 50	10 08

- a) Tim catches the 06 06 train from Manchester.
- At what time should he expect to arrive at Euston?
- b) Jenny arrives at the Stockport train station at 07 00
- (i) How long should she expect to wait for a train to Stoke?
  - (ii) How long should her train journey take?
- c) Sarah needs to travel to Euston from Macclesfield.

She has to arrive at Euston before 09 30.

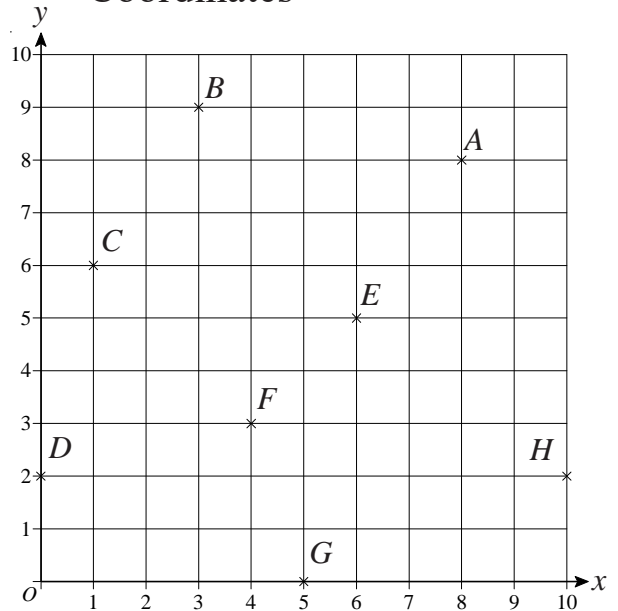
What is the departure time of the latest train she can catch to get there on time?

- 1) Write the following in their simplest forms using algebraic notation:
  - a)  $r \times 5$
  - b)  $c \div 4$
  - c)  $x + x + x + x$
  - d)  $e \times 1$
  
- 2) Write the following using algebraic notation:
  - a) I think of a number and multiply it by 4.
  - b) I think of a number, multiply it by 6 and then add 5.
  - c) I think of a number, triple it and then subtract 7.
  
- 3) Write the following using algebraic notation:
  - a) I think of a number, add 2 and then multiply the result by 3.
  - b) I think of a number, subtract 6 and then divide the result by 2.
  
- 4) Write the following using algebraic notation:
  - a) I think of a number, add 9, multiply the result by 4 and then divide everything by 2.
  - b) I think of a number, take away 5, divide the result by 3 and then multiply the result by 2.

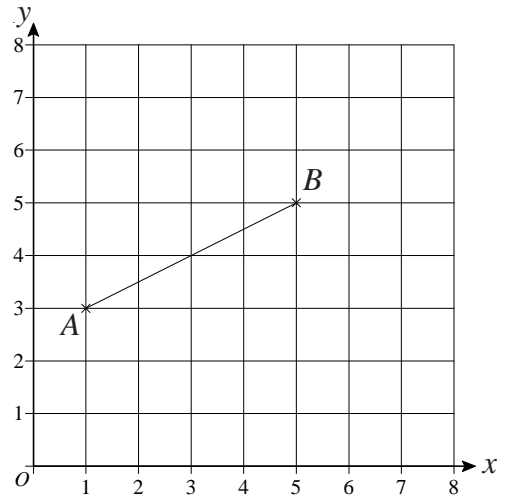


## Coordinates

- 1) Write down the coordinates of the points  $A$  to  $H$ .



- 2) a) Write down the coordinates of: (i)  $A$  (ii)  $B$   
 b) Write down the coordinates of the midpoint of the line  $AB$ .



- 3) Using the pair of axes,  
 a) Plot the points  $A(2, 0)$ ,  $B(4, 0)$ ,  $C(5, 2)$  and  $D(3, 2)$ .

- b) Join the points in order, to form a shape and name the shape.

$M$  is the midpoint of the line segment  $AC$ .

- c) Find the coordinates of  $M$ .

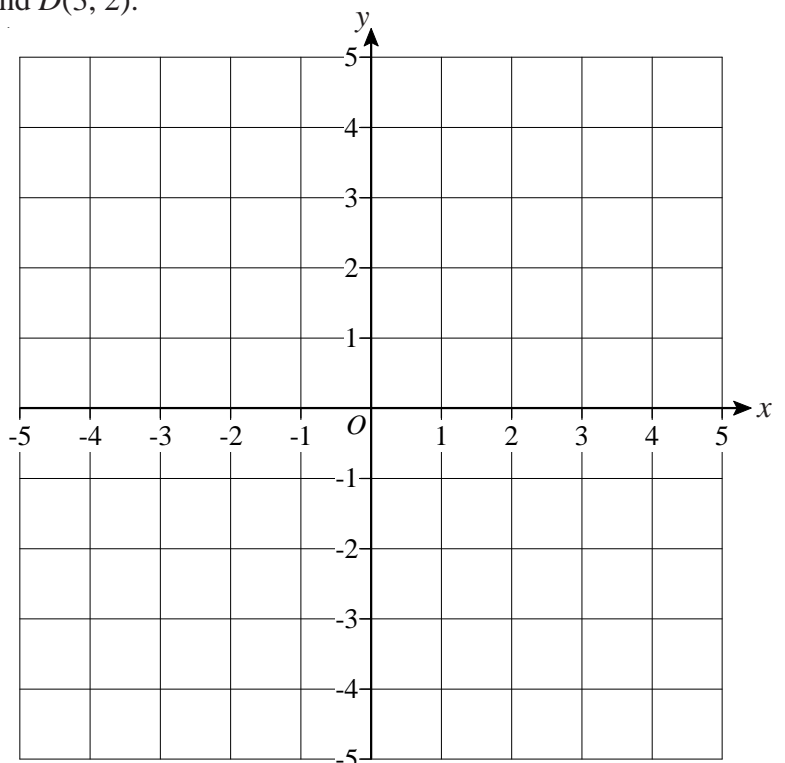
- 4) Using the same pair of axes,

- a) Plot the points  $R(-1, -2)$ ,  $S(1, 1)$  and  $T(-1, 2)$ .

- b) Join  $R$  to  $S$  and  $S$  to  $T$ .

$RSTU$  is a kite.

- c) Write the coordinates of point  $U$ .



- 1) Write one or two short sentences which say what the special features are of the triangles listed, below.  
The first one has been done for you.

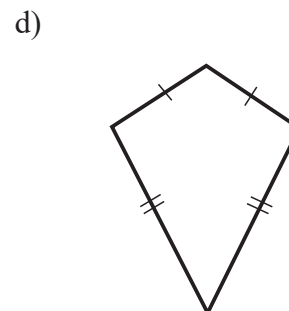
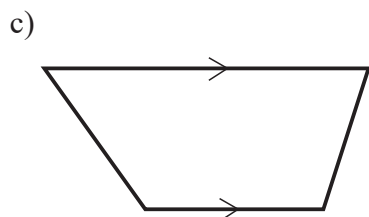
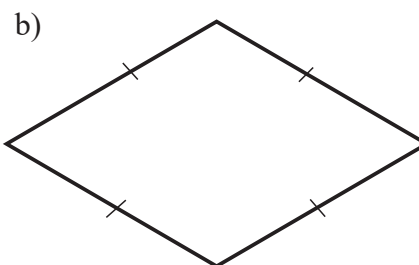
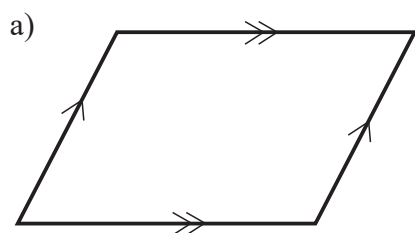
a) An equilateral triangle *All the sides are the same length.  
All three angles are  $60^\circ$*

b) A right-angled triangle

c) A scalene triangle

d) An isosceles triangle

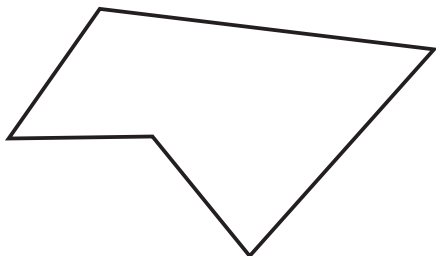
- 2) Next to each of the quadrilaterals, write down its special name.



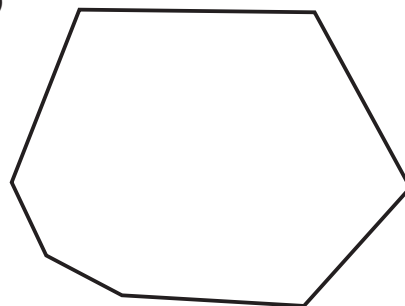
## Polygons

- 1) Next to each of the shapes, write down its name.

a)



b)



- 2) a) What is the name given to a 10-sided shape?

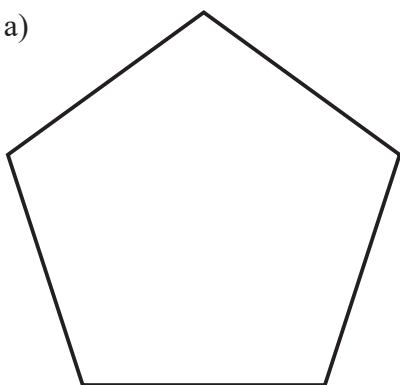
- b) What is the name given to an 8-sided shape?

- 3) To be a regular polygon the shape must have equal \_\_\_\_\_ and equal \_\_\_\_\_.

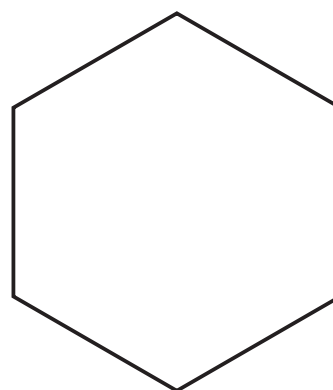
Fill in the blanks.

- 4) What are the names of these regular polygons?

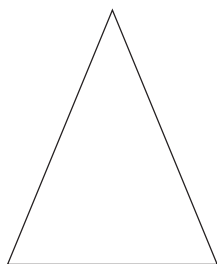
a)



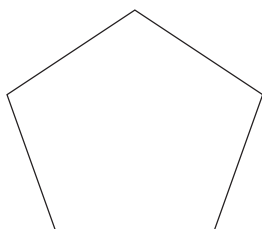
b)



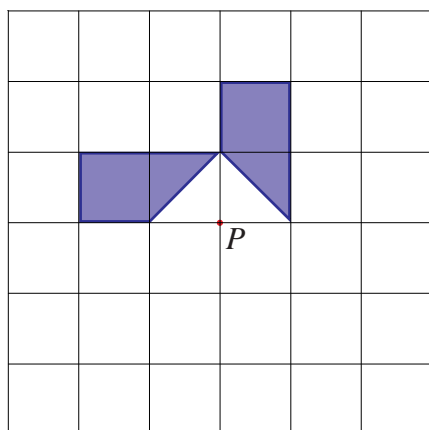
- 1) Draw all the lines of symmetry on the triangle and the rectangle.



- 2) What is the order of rotational symmetry of the two shapes below?



- 3) The diagram below, shows part of a shape.



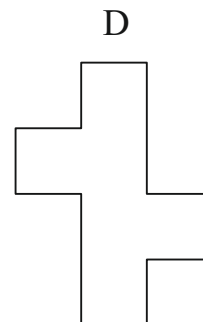
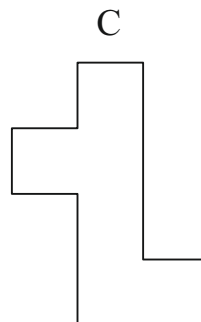
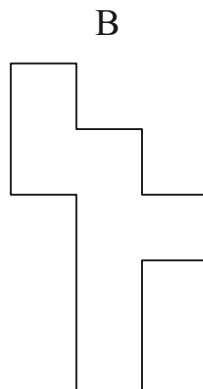
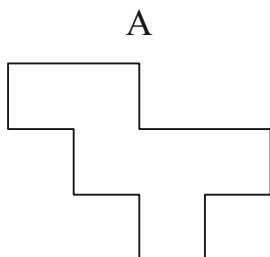
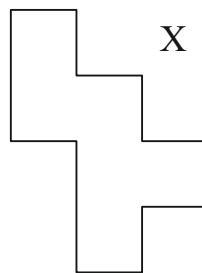
The shape has rotational symmetry of order 4 about point  $P$ .

Complete the shape.

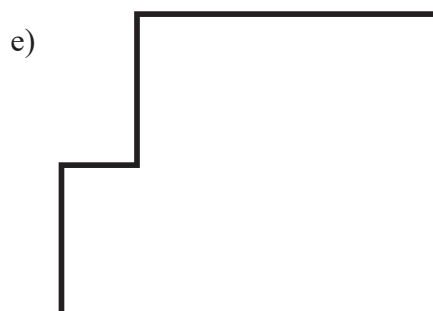
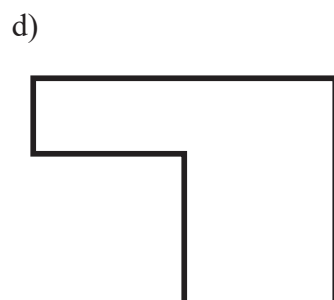
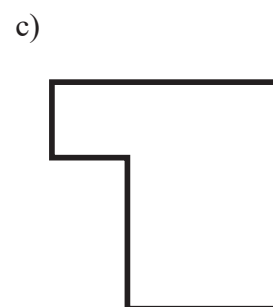
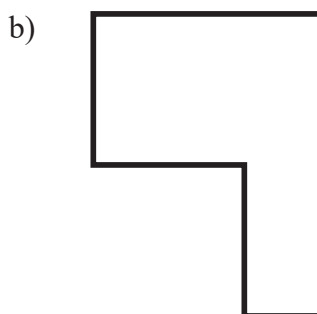
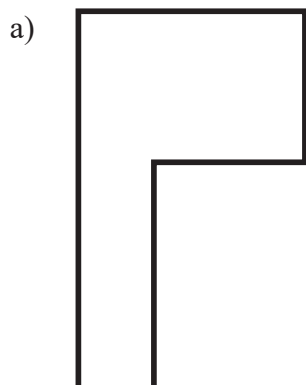
## Congruent Shapes

- 1) Which shape is congruent to shape X?

Circle your answer.

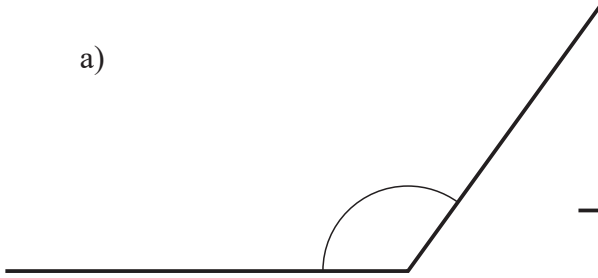


- 2) Two of these shapes are congruent.  
Which are they?

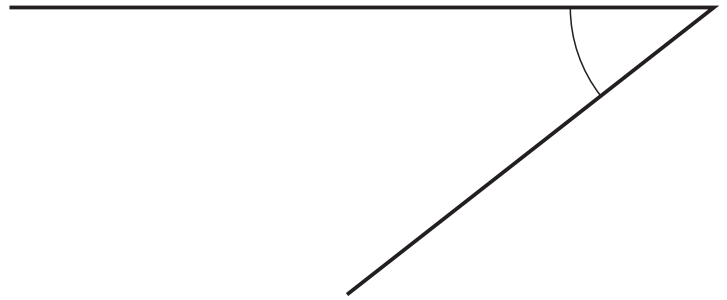


1) Write the name of each angle, below.

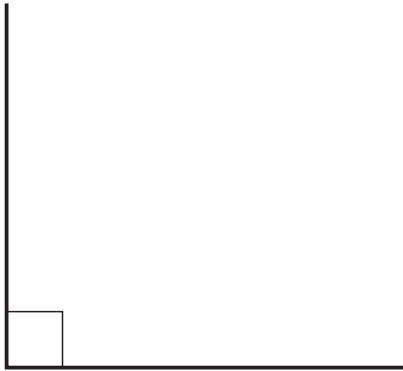
a)



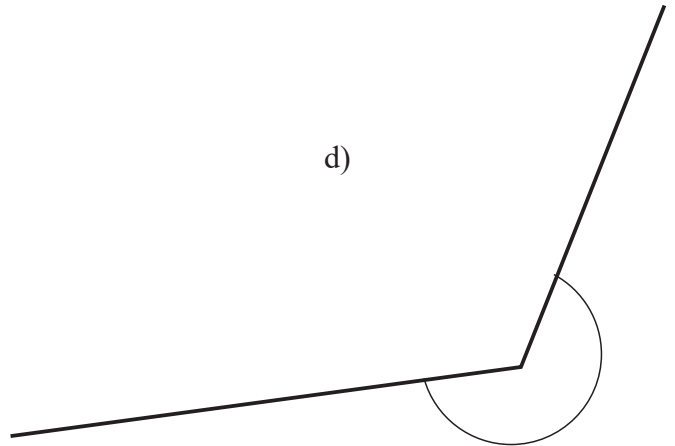
b)



c)



d)

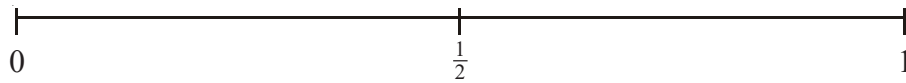


2) Draw a triangle which contains:

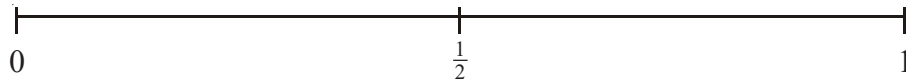
- Three acute angles.
- One obtuse angle and two acute angles.
- A right angle.

## The Probability Scale

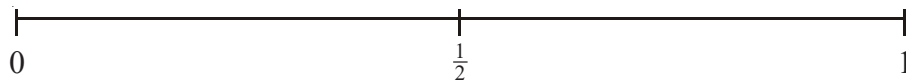
- 1) a) On the probability scale below, mark with a cross (×) the probability that it will snow in Birmingham in July.



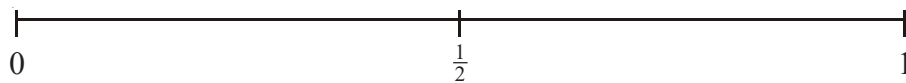
- b) On the probability scale below, mark with a cross (×) the probability that it will rain in Wales next year.



- c) On the probability scale below, mark with a cross (×) the probability that you will get a tail when you flip a fair coin.



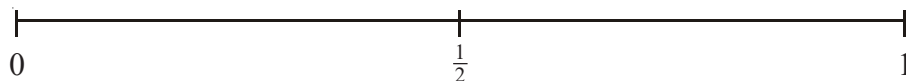
- d) On the probability scale below, mark with a cross (×) the probability that you will get a number bigger than 4 when you roll an ordinary dice.



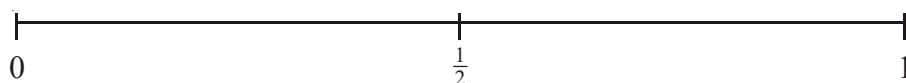
- 2) 4 jelly babies are in a bag.  
2 are red, 1 is green and 1 is black.

Without looking in the bag, a jelly baby is taken out.

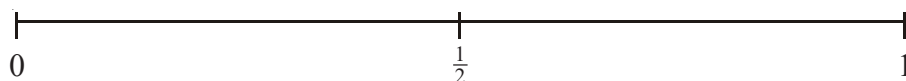
- a) On the probability scale below, mark with a cross (×) the probability that the jelly baby taken from the bag is green.



- b) On the probability scale below, mark with a cross (×) the probability that the jelly baby taken from the bag is green or black.



- c) On the probability scale below, mark with a cross (×) the probability that the jelly baby taken from the bag is red or black.



## Tally Charts and Bar Charts

- 1) Here is a list of coins in Yvonne's purse.

5p   £1   20p   1p   50p

10p   £1   5p   50p   2p

5p   5p   £1   1p   5p

£1   2p   5p   5p   2p

Coin	Tally	Frequency

Complete the table for this information.

- 2) Tim made a note of how many minutes he spent on the internet over the period of a week. His results are as follows:

Monday   20 mins

Tuesday   30 mins

Wednesday 60 mins

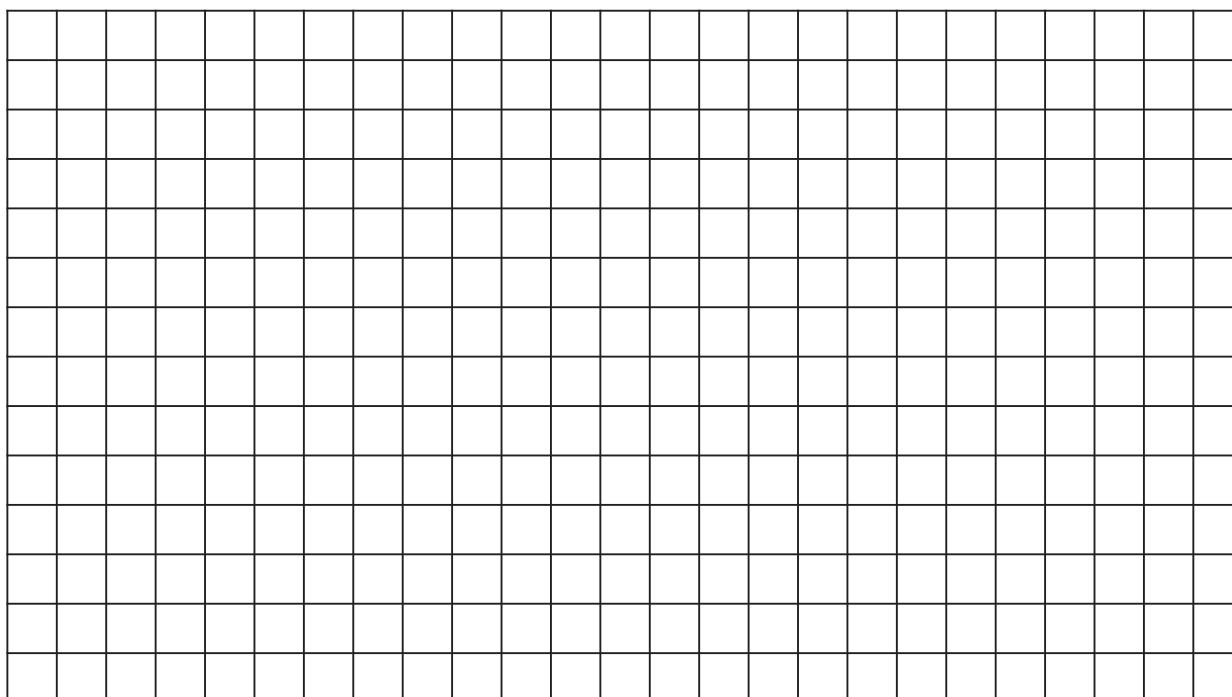
Thursday   40 mins

Friday   20 mins

Saturday   50 mins

Sunday   40 mins









Draw a bar chart to show this information.





## Pictograms

- 1) The pictogram shows the number of watches sold by a shop in January, February and March.

January	   
February	 
March	 
April	
May	








Key  represents 4 watches.

- a) How many watches were sold in January?  
b) How many **more** watches were sold in March than in February?

19 watches were sold in April.  
14 watches were sold in May.

- c) Use this information to complete the pictogram.

- 2) The pictogram shows the number of DVDs borrowed from a shop on Monday and Tuesday.

Monday	   
Tuesday	  
Wednesday	
Thursday	

Key  represents 10 DVDs.

- a) How many DVDs were borrowed on  
(i) Monday?  
(ii) Tuesday?

On Wednesday, 50 DVDs were borrowed.  
On Thursday, 15 DVDs were borrowed.

- b) Show this information in the pictogram.

1) a) 
$$\begin{array}{r} 42 \\ + 26 \\ \hline \end{array}$$
 b) 
$$\begin{array}{r} 57 \\ + 38 \\ \hline \end{array}$$
 c) 
$$\begin{array}{r} 96 \\ + 75 \\ \hline \end{array}$$

2) a) 
$$\begin{array}{r} 637 \\ + 961 \\ \hline \end{array}$$
 b) 
$$\begin{array}{r} 983 \\ + 442 \\ \hline \end{array}$$
 c) 
$$\begin{array}{r} 969 \\ + 758 \\ \hline \end{array}$$

3) a)  $452 + 38$  b)  $147 + 763$  c)  $813 + 431 + 38$

- 4) There were two exhibitions at the NEC one Sunday.  
3816 people went to one of the exhibitions and 13427 people went to the other exhibition.  
How many people went to the NEC, in total, on the Sunday?

5) a)  $2.6 + 1.2$  b)  $2.74 + 6.81$  c)  $45.36 + 6.81$

6) a)  $23 + 1.5$  b)  $13.6 + 38$  c)  $13.2 + 17.82$

1) a) 
$$\begin{array}{r} 78 \\ -42 \\ \hline \end{array}$$

b) 
$$\begin{array}{r} 74 \\ -26 \\ \hline \end{array}$$

c) 
$$\begin{array}{r} 62 \\ -39 \\ \hline \end{array}$$

2) a) 
$$\begin{array}{r} 485 \\ -291 \\ \hline \end{array}$$

b) 
$$\begin{array}{r} 773 \\ -486 \\ \hline \end{array}$$

c) 
$$\begin{array}{r} 100 \\ -34 \\ \hline \end{array}$$

3) a)  $653 - 48$       b)  $362 - 183$       c)  $2000 - 461$

- 4) There were two films showing at a cinema one Saturday.  
One of the films was shown in a large room and the other was in a smaller room.  
The film in the larger room was watched by a total of 3562 people.  
The film in the smaller room was watched by 1671 people.  
How many more people saw the film in the larger room?

5) a)  $782 + 426 - 278$       b)  $8162 + 1149 - 799$

1) Work out

a)  $13 \times 18$

b)  $135 \times 27$

c)  $116 \times 41$

d)  $264 \times 43$

e)  $326 \times 24$

f)  $281 \times 59$

g)  $286 \times 48$

h)  $428 \times 34$

i)  $461 \times 45$

2) “MathsWatch Travel” has 36 coaches.

Each of these coaches can carry 53 passengers.

How many passengers in total can all the coaches carry?

3) “MathsWatch Tours” has a plane that will carry 47 passengers.

To fly from Manchester to Lyon, each passenger pays £65

Work out the total amount that the passengers pay.

4) A Science textbook costs £13.

Mr Jones buys a class set of 34 books.

How much do they cost him?

5) A graphical calculator costs £18.

How much would 43 calculators cost?

## Dividing Integers

- 1) Work out
  - a)  $325 \div 5$
  - b)  $448 \div 8$
  - c)  $221 \div 13$
  - d)  $377 \div 29$
  - e)  $27 \div 6$
  - f)  $123 \div 15$
  - g)  $75 \div 4$
  - h)  $135 \div 20$
  - i)  $381 \div 12$

- 2) A box can hold 19 books.  
Work out how many boxes will be needed to hold 646 books.

- 3) The distance from Glasgow to Paris is 1290 km.  
A flight from Glasgow to Paris lasts 3 hours.

Given that

$$\text{Average speed} = \frac{\text{Distance}}{\text{Time}}$$

Work out the average speed of the aeroplane in km/h.

- 4) Pencils cost 25p each.  
Mr Smith spends £15 on pencils.  
Work out the number of pencils he gets.
- 5) Yesterday, Gino was paid £19.61 for delivering pizzas.  
He is paid 53p for each pizza he delivers.  
Work out how many pizzas Gino delivered yesterday.
- 6) Emma sold 38 teddy bears for a total of £513  
She sold each teddy bear for the same price.  
Work out the price at which Emma sold each teddy bear.

- 7)
 

Canal boat for hire  
£1855.00  
for 14 days

Work out the cost per day of hiring the canal boat.

- 8) A teacher has £539 to spend on books.  
Each book costs £26  
How many books can the teacher buy?
- 9) John delivers large wooden crates with his van.  
The weight of each crate is 68 kg.  
The greatest weight the van can hold is 980 kg.  
Work out the greatest number of crates that the van can hold.

- 1) a) Which operation is the inverse of 'add'?
- b) Which operation is the inverse of 'divide'?

- 2) Use inverse operations to complete the second equation each time.

a)  $12 + 6 = 18 \longrightarrow \square ? \square = 12$

b)  $28 ? 13 = 15 \longrightarrow \square + \square = 28$

- 3) Use inverse operations to complete the second equation each time.

a)  $14 \times 2 = 28 \longrightarrow \square \div \square = 14$

b)  $60 \div 12 = 5 \longrightarrow \square \times \square = 60$

- 4) Use inverse operations to complete the second equation each time.

a)  $19 + 13 = 32 \longrightarrow \square \square = 19$

b)  $46 ? 13 = 33 \longrightarrow \square \square = 46$

- 5) Use inverse operations to complete the second equation each time.

a)  $28 \div 7 = 4 \longrightarrow \square \square = 28$

b)  $16 \times 3 = 48 \longrightarrow \square \square = 3$

## Negatives in Real Life

- 1) At midnight, the temperature was  $-7^{\circ}\text{C}$ .

By 7am the next morning, the temperature had increased by  $6^{\circ}\text{C}$ .

- a) Work out the temperature at 7am the next morning.

At midday, the temperature was  $3^{\circ}\text{C}$ .

- b) Work out the difference between the temperature at midday and the temperature at midnight.

- c) Work out the temperature which is halfway between  $-7^{\circ}\text{C}$  and  $3^{\circ}\text{C}$ .

- 2) The table below gives the temperature recorded on 25th December in 7 cities across the world.

City	Edinburgh	London	New York	Moscow	Paris	Rome	Cairo
Temperature	$-6^{\circ}\text{C}$	$0^{\circ}\text{C}$	$-15^{\circ}\text{C}$	$-23^{\circ}\text{C}$	$3^{\circ}\text{C}$	$5^{\circ}\text{C}$	$18^{\circ}\text{C}$

- a) Which city recorded the lowest temperature?

- b) What is the difference in temperature between New York and Paris?

- c) What is the difference in temperature between Cairo and Edinburgh?

- d) The temperature in Madrid was  $9^{\circ}\text{C}$  lower than in Rome.

What was the temperature in Madrid?

- e) The temperature in Mexico City was  $6^{\circ}\text{C}$  higher than in New York.

What was the temperature in Mexico City?

- 3) The table shows the temperature on the surface of each of five planets.

Planet	Temperature
Venus	$210^{\circ}\text{C}$
Jupiter	$-150^{\circ}\text{C}$
Saturn	$-180^{\circ}\text{C}$
Neptune	$-210^{\circ}\text{C}$
Pluto	$-230^{\circ}\text{C}$

- a) Work out the difference in temperature between Jupiter and Pluto.

- b) Work out the difference in temperature between Venus and Saturn.

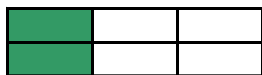
- c) Which planet has a temperature  $30^{\circ}\text{C}$  lower than Saturn?

The temperature on Mars is  $90^{\circ}\text{C}$  higher than the temperature on Jupiter.

- d) Work out the temperature on Mars.

1) What fraction of each of the following shapes is shaded?

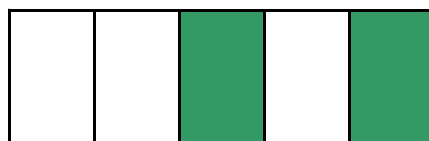
a)



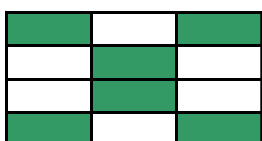
b)



c)



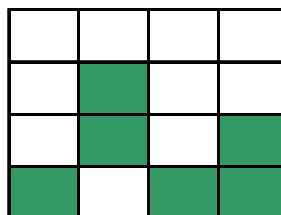
d)



e)

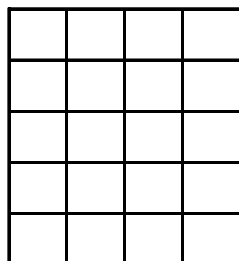


f)

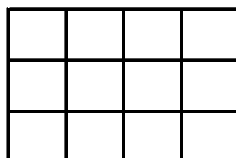


2) Shade the given fraction in the following grids.

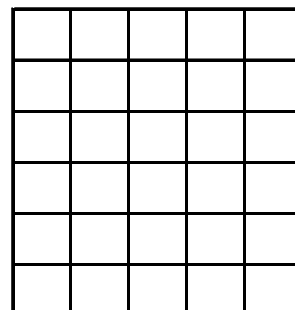
$$\frac{3}{5}$$



$$\frac{1}{4}$$



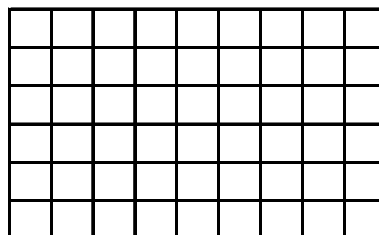
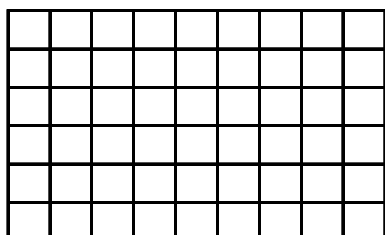
$$\frac{4}{6}$$



3) Which of these fractions is the smallest?

$$\frac{5}{6} \text{ or } \frac{7}{9}$$

(use the grids to help)





## Introduction to Fractions

### Mixed Numbers

1) Write the following as improper fractions in their simplest form.

a)  $3\frac{1}{4}$

b)  $1\frac{2}{5}$

c)  $5\frac{2}{3}$

d)  $4\frac{5}{8}$

2) Write the following as mixed numbers in their simplest form.

a)  $\frac{8}{5}$

b)  $\frac{11}{4}$

c)  $\frac{16}{5}$

d)  $\frac{73}{10}$

3) Write the following as improper fractions in their simplest form.

a)  $7\frac{1}{13}$

b)  $15\frac{2}{5}$

c)  $23\frac{3}{4}$

d)  $9\frac{5}{12}$

4) Write the following as mixed numbers in their simplest form.

a)  $\frac{66}{5}$

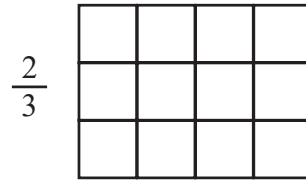
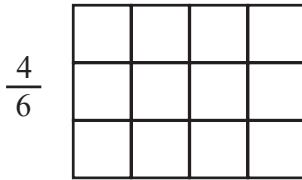
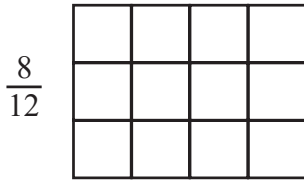
b)  $\frac{87}{4}$

c)  $\frac{54}{11}$

d)  $\frac{98}{13}$

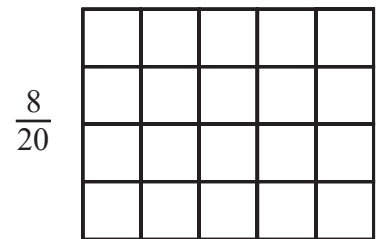
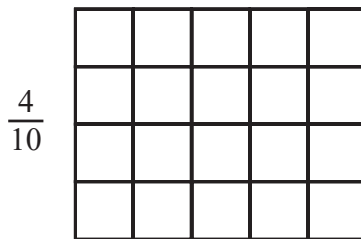
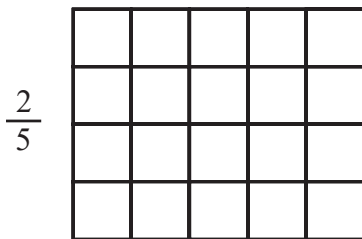
## Equivalent Fractions

- 1) Each of the grids below has a fraction written at the side of it.  
a) Shade the grids to show these fractions.



- b) What do you notice about how many little squares are shaded in each grid?

- 2) Each of the grids below has a fraction written at the side of it.  
a) Shade the grids to show these fractions.



- b) What do you notice about how many little squares are shaded in each grid?

- 3) Find the missing values in these equivalent fractions.

$$\frac{1}{2} = \frac{2}{\square} = \frac{3}{\square} = \frac{4}{\square}$$

- 4) Find the missing values in these equivalent fractions.

$$\frac{2}{5} = \frac{6}{\square} = \frac{\square}{30} = \frac{14}{\square}$$

- 5) How do you know that  $\frac{3}{7}$  is not equivalent to  $\frac{25}{56}$ ?

1) Write the following fractions in their simplest forms

a)  $\frac{2}{4}$

b)  $\frac{5}{10}$

c)  $\frac{4}{6}$

d)  $\frac{6}{9}$

e)  $\frac{12}{15}$

f)  $\frac{8}{12}$

g)  $\frac{15}{20}$

2) Write the following fractions in their simplest forms

a)  $\frac{9}{30}$

b)  $\frac{14}{18}$

c)  $\frac{7}{49}$

d)  $\frac{48}{72}$

e)  $\frac{60}{75}$

f)  $\frac{15}{27}$

g)  $\frac{72}{96}$

1) Write down the number which is in the middle of:

- a) 3 and 9
- b) 12 and 28
- c) 11 and 22
- d) 17 and 32
- e) 72 and 108
- f) 1 and 100
- g)  $-6$  and 2



2) Write down the number which is in the middle of:

- a) 2.4 and 6.8
- b) 5.9 and 12.5
- c)  $-5$  and 7.8



3) a) 7 is in the middle of 3 and which other number?

b) 16 is in the middle of 9 and which other number?

c) 2.4 is in the middle of 1.1 and which other number?

1) Write the factors of

- a) 6                      b) 16                      c) 18                      d) 30

2) In a pupil's book the factors of 12 are listed as

1   2   3   4   5   12

The above list contains a mistake.

Cross it out from the list and replace it with the correct number.

3) The factors of 30 and 40 are listed

**30:** 1, 2, 3, 5, 6, 10, 15, 30

**40:** 1, 2, 4, 5, 8, 10, 20, 40

Write the common factors of 30 and 40 (the numbers that are factors of 30 and 40).

4) Write the first four multiples of

- a) 3                      b) 5                      c) 10                      d) 15

5) In a pupil's book the first 7 multiples of 8 are listed as

8   16   22   32   40   48   54

The above list contains 2 mistakes.

Cross them out and replace them with the correct numbers.

6) The first five multiples of 4 and 10 are listed

**4:** 4, 8, 12, 16, 20

**10:** 10, 20, 30, 40, 50

From the two lists above, write the common multiple of 4 and 10.

7) List the first five prime numbers

8) Using just this list of numbers:

11   18   1   4   21   24   9   3   12   2   19

find the following:

- a) The prime numbers  
b) The factors of 18  
c) The multiples of 3

- 1) Write the following using indices:

eg.  $3 \times 3 \times 3 \times 3 = 3^4$

a)  $2 \times 2 \times 2 \times 2$

d)  $12 \times 12 \times 12 \times 12 \times 12$

b)  $4 \times 4 \times 4$

e)  $3.6 \times 3.6$

c)  $5 \times 5 \times 5 \times 5 \times 5 \times 5$

f)  $5.2 \times 5.2 \times 5.2$

- 2) Write each of the following as a single power:

eg.  $5^2 \times 5^4 = 5^6$

a)  $6^2 \times 6^3$

d)  $5^3 \times 5$

b)  $7^4 \times 7^2$

e)  $2^9 \times 2^3$

c)  $9^3 \times 9^6$

f)  $7.2^3 \times 7.2^2$

- 3) Write each of the following as a single power:

eg.  $7^5 \div 7^2 = 7^3$

a)  $9^5 \div 9^3$

d)  $\frac{7^8}{7^3}$

b)  $6^9 \div 6^5$

e)  $\frac{3^6}{3}$

c)  $11^7 \div 11^2$

f)  $\frac{8^{15}}{8^4}$

- 4) Write each of the following as a single power:

eg.  $\frac{7^3 \times 7^8}{7^6} = \frac{7^{11}}{7^6} = 7^5$

a)  $\frac{4^7 \times 4^3}{4^6}$

b)  $\frac{9^2 \times 9^6}{9^4}$

- 5) Match together cards with the same answer

$5^7$	$5^{10} \div 5^6$	$5^6 \times 5^2$	$5^3$	$5^2$
$5^8$	$5 \times 5$	$\frac{5^2 \times 5^4}{5^3}$	$5^2 \times 5^5$	$5^4$

## Multiply and Divide by Powers of 10

- 1) Multiply the following numbers by 10, 100 and 1000:

		$\times 10$	$\times 100$	$\times 1000$
<i>e.g.</i>	21	210	2100	21000
	9			
	63			
	845			
	3.65			
	0.4			
	1.324			

---

- 2) Divide the following numbers by 10, 100 and 1000:

		$\div 10$	$\div 100$	$\div 1000$
<i>e.g.</i>	21	2.1	0.21	0.021
	9			
	63			
	845			
	3.65			
	0.4			
	1.324			

---

- 3) Work out the following:

$$3 \times 100 =$$

$$65 \times 10 =$$

$$17 \div 10 =$$

$$359 \times 10 =$$

$$0.5 \div 100 =$$

$$2.3 \times 1000 =$$

$$42 \div 100 =$$

$$3582 \div 100 =$$

$$0.9 \times 10 =$$

$$3.645 \times 100 =$$

$$88 \div 1000 =$$

$$39.62 \times 1000 =$$

- 1) Round these numbers to the nearest 10:
  - a) 26
  - b) 62
  - c) 75
  - d) 231
  - e) 797
  - f) 5 842
  - g) 9 875
  - h) 13 758
  
- 2) Round these numbers to the nearest 100:
  - a) 78
  - b) 223
  - c) 549
  - d) 1 450
  - e) 1 382
  - f) 4 537
  - g) 9 193
  - h) 17 625
  
- 3) Round these numbers to the nearest 1000:
  - a) 850
  - b) 1 455
  - c) 3 230
  - d) 7 500
  - e) 8 455
  - f) 9 690
  - g) 12 390
  - h) 28 910



- 1) Round the following numbers to 1 decimal place
  - a) 13.681
  - b) 344.7234
  - c) 0.76133
  
- 2) Round the following numbers to 2 decimal places
  - a) 58.8136
  - b) 14.22731
  - c) 203.86884
  
- 3) Round the following numbers to 1 decimal place
  - a) 48.9732
  - b) 163.9299
  - c) 19.952
  
- 4) Round the following numbers to 2 decimal places
  - a) 10.697
  - b) 8.993
  - c) 14.9964
  
- 5) Work out the answer to  $2.6882 \times 14.71728$  and give your answer correct to 2 decimal places.
  
- 6) Work out the answer to  $64.2 \div 5.7$  and give your answer correct to 1 decimal place.
  
- 7) Work out the answer to  $4.74^2$  giving your answer correct to 2 decimal places.
  
- 8) Find the answer to  $\sqrt{17.3}$  giving your answer correct to 1 decimal place.

1) Write the following ratios in their simplest form:

- a)  $6 : 9$
- b)  $10 : 5$
- c)  $7 : 21$
- d)  $4 : 24$
- e)  $12 : 40$
- f)  $4 : 2 : 8$
- g)  $18 : 63 : 9$

2) Write the missing value in these equivalent ratios:

- a)  $3 : 5 = 12 : \square$
- b)  $4 : 9 = \square : 27$
- c)  $\square : 7 = 16 : 14$

3) The ratio of girls to boys in a class is  $4 : 5$ .

What fraction of the class are girls?

4) A model of a plane is made using a scale of  $1 : 5$ .

- a) If the real length of the plane is 20 m, what is the length of the model?
- b) If the wings of the model are 1.2 m long, what is the actual length of the wings on the plane?

- 1) Here are the ingredients needed to make 8 pancakes.  
James makes 24 pancakes.

<b>Pancakes</b>
Ingredients to make <b>8</b> pancakes
250 ml milk
1 egg
140 g flour
5 g butter

- a) Work out how much milk he needs.

Kate makes 12 pancakes.

- b) Work out how much flour she needs.



- 2) Here are the ingredients for making fish pie for 6 people.

<b>Fish pie for 6 people</b>
180 g flour
240 g fish
80 g butter
4 eggs
180 ml milk

Jill makes a fish pie for 3 people.

- a) Work out how much flour she needs.

Tim makes a fish pie for 15 people.

- b) Work out how much milk he needs.



- 3) Here are the ingredients for making pineapple sorbet for 6 people.

<b>Pineapple sorbet for 6 people</b>
800 g of pineapple
4 egg whites
$\frac{1}{2}$ lemon
100 g caster sugar

Trevor makes pineapple sorbet for 18 people.

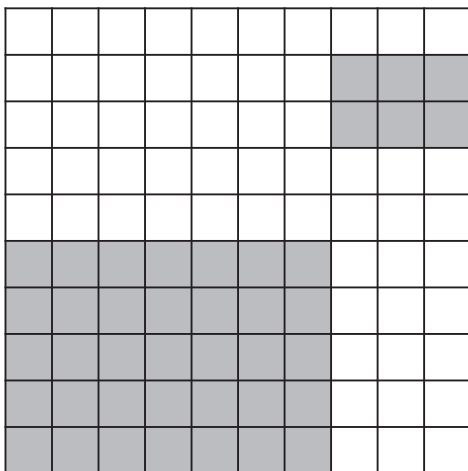
- a) Work out how much caster sugar he uses.

Sid makes a pineapple sorbet.

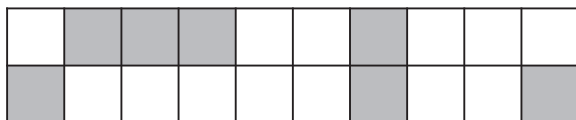
He uses 2 lemons.

- b) Work out how many people he makes pineapple sorbet for.

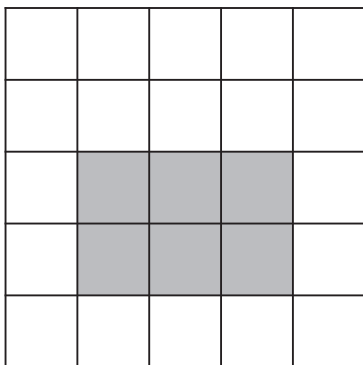
- 1) What percentage of this grid is shaded?



- 2) What percentage of this grid is shaded?

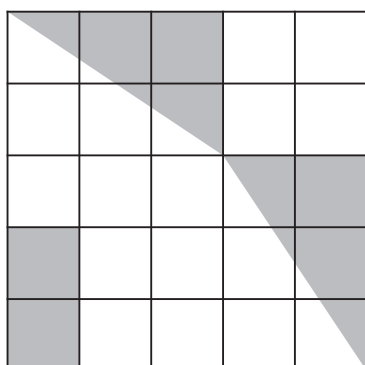




- 3) a) What percentage of this grid is shaded?



- b) How many more squares should be shaded to make 80% of the grid shaded?

- 4) What percentage of this grid is shaded?



- 1) 8 bananas cost £4  
Work out the cost of 5 bananas.
  
- 2) Emily bought 4 identical pairs of socks for £3.60  
Work out the cost of 9 pairs of these socks.
  
- 3) The price of 36 chocolates is £7.20  
Work out the cost of 8 chocolates.
  
- 4) Theresa bought 5 theatre tickets for £60  
Work out the cost of 9 theatre tickets.
  
- 5) Jenny buys 4 folders.  
The total cost of these 4 folders is £6.40  
Work out the total cost of 7 of these folders.
  
-  6) The cost of 15 litres of petrol is £12  
Work out the cost of 20 litres of petrol.
  
-  7) 3 maths books cost £7.47  
Work out the cost of 5 of these.

- 1) Which of the following offer better value for money?

*Working must be shown*

a) 200ml of toothpaste for 50p or 400ml of toothpaste for 90p

b) 600g of bananas for 70p or 200g of bananas for 22p

c) 2 litres of paint for £1.60 or 5 litres of paint for £3.50

d) 60 teabags for £1.62 or 40 teabags for £0.96



- 2) Which of these is the best buy?

20 exercise books  
for £4.00

35 exercise books  
for £7.80

- 3) Hamza needs to buy 2 litres of paint.

At the shop he gets two choices:

500ml for £2.55 or 1 litre for £4.79.

a) Work out which of these would be the best buy for Hamza.

b) How much does he save if he buys the 'best buy' rather than the 'worst buy'?

You must show all your working.



- 4) Honey pots are sold in two sizes.

A small pot costs 45p and weighs 450g.

A large pot costs 80p and weighs 850g.

Which pot of honey is better value for money?

You must show all your working.

1) Simplify the following

a)  $x + x$

b)  $2x + 3x$

c)  $5t - 3t$

d)  $7y - 6y$

e)  $x + 2x + 3x$

f)  $3g - g + 6g$

g)  $2x - 7x + 8x$

h)  $y - 2y - 3y + 6y$

2) Simplify the following

a)  $xy + 3xy$

b)  $5xy - 2xy$

c)  $4x^2y + x^2y$

d)  $3xy^2 - 2xy^2$

e)  $2x^2y^3 + 4x^2y^3 - 3x^2y^3$

f)  $6a^2bc^4 + 5a^2bc^4 - 2a^2bc^4$

3) Simplify the following

a)  $x + y + x + y$

b)  $2x + 3y + x + 4y$

c)  $2a + 4b - a + 2b$

d)  $3x + 4y - x - 2y$

e)  $6x - 2y + 2x + 5y$

f)  $4x - 3y - 2x - 5y$

g)  $3t + 4u + 2t - 7u$

h)  $2xy + 3t - xy - 4t$

1) Simplify the following

a)  $x \times x$

b)  $x \times x \times x \times x \times x$

c)  $y \times y \times y$

2) Simplify the following

a)  $x^2 \times x^4$

b)  $x^3 \times x^5$

c)  $y \times y^3$

d)  $x^2 \times x \times x^4$

e)  $y^2 \times y^3 \times y^4$

3) Simplify the following

a)  $2x \times x$

b)  $4x \times 3x$

c)  $3t^2 \times 2t$

d)  $4y^2 \times 3y^3$

e)  $x \times 2x^2 \times 3x^3$

4) Simplify the following

a)  $x \times y$

b)  $2x \times 3y$

c)  $5r \times 2s \times 3t$

d)  $6x \times 2y \times z$

5) Simplify the following

a)  $3x \times y$

b)  $4x^2y \times 2x$

c)  $3xy^2 \times 2xy^3$

d)  $6xy \times x^2y^3 \times 2y$

e)  $2x^2y^3 \times 5x^4y^2$

f)  $tu^2 \times t^2u \times 4tu$



1) Simplify the following

a)  $x^5 \div x$

b)  $y^4 \div y^3$

c)  $g^8 \div g^5$

d)  $y^4 \div y^2$

e)  $x^3 \div x^3$

2) Simplify the following

a)  $6x^4 \div x$

b)  $12y^5 \div 3y^2$

c)  $10g^7 \div 2g^5$

3) Simplify the following

a)  $\frac{x^6}{x^2}$

b)  $\frac{x^9}{x^4}$

c)  $\frac{6x^8}{2x^6}$

4) Simplify the following

a)  $\frac{x^6 \times x^3}{x^4}$

b)  $\frac{x^3 \times x^4}{x^2 \times x}$

c)  $\frac{(x+5)^5}{(x+5)^2}$

5) Simplify the following

a)  $20x^6 \div 5x^2$

b)  $\frac{14x^7}{2x^2}$

c)  $\frac{8x \times 2x^3}{4x^2}$

## Simplifying

1) a) Simplify  $4p \times 6q$

b) Simplify  $d \times d \times d \times d$

c) Simplify  $t^9 \div t^4$

2) a) Simplify  $4a + 3c - 2a + c$

b) Simplify  $2x - 6c - x + 2c$

3) a) Simplify  $5xt + 2xt - 4xt$

b) Simplify  $4x + 3y - 2x + 4y$

c) Simplify  $m \times m \times m$

d) Simplify  $3n \times 2t$

4) Simplify  $3x^2 \times 4x^5y^4$

5) Simplify  $4x + 3y - 2x + 6y$

6) a) Simplify  $t^4 \times t^5$

b) Simplify  $a \times a \times a$

7) a) Simplify  $x^6 \times x^2$

b) Simplify  $10x^2y^4 \div 2xy^2$

8) a) Simplify  $3a + 5c - a + 3c$

b) Simplify  $x^3 \times x^4$

c) Simplify  $4x^2y^4 \times 5xy^2$

9) Simplify  $6x + 8y + 2x - 10y$

10) a) Simplify  $x \times x \times x \times x$

b) Simplify  $2x \times 3y$

11) a) Simplify  $pq + 2pq$

b) Simplify  $5x + 3y - x - 4y$

12) a) Simplify  $6a + 5b - 3b + a$

b) Simplify  $x^4 + x^4$

13) a) Simplify  $x + y + x + y + x$

b) Simplify  $t^2 + t^2 + t^2$

14) a) Simplify  $a^3 \times a^3$

b) Simplify  $\frac{3x^2y \times 4xy^3}{2xy^2}$

15) a) Simplify  $3d + e - d + 4e$

b) Simplify  $3x^2 - x^2$

c) Simplify  $5t + 8d - 2t - 3d$

d) Simplify  $\frac{(3x + 1)^3}{(3x + 1)}$

- 1) Complete the table for the function machine.



In	Out
4	
7	
	48
	73

- 2) Complete the table for the function machine.



In	Out
-2	
1	
	17
$x$	

- 3) Complete the table for the function machine.



In	Out
-3	
0	
	66
$x$	

1) Write the first 5 terms of each of these sequences.

- a) Start at 2 and add 6.
- b) Start at 14 and subtract 3.
- c) Start at 4 and subtract 7.
- d) Start at 2 and multiply by 3.
- e) Start at 64 and divide by 2.
- f) Start at 600 and divide by 10.

2) Find the term to term rule for each of these sequences.

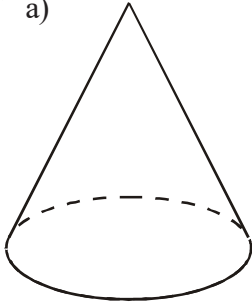
- a) 4, 7, 10, 13, 16
- b) 15, 13, 11, 9, 7
- c) 2, -3, -8, -13, -18
- d) 7, 14, 28, 56, 112
- e) 100, 10, 1, 0.1, 0.01

1) Draw a sketch of each of the following solids:

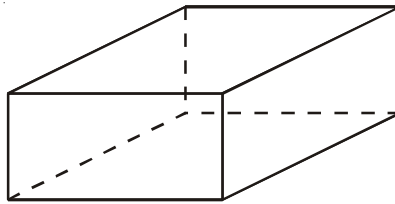
- a) A cube.
- b) A cylinder.

2) Write down the mathematical name of each of these 3-D shapes.

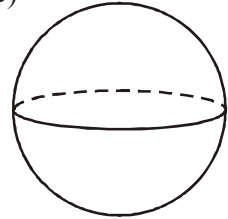
a)



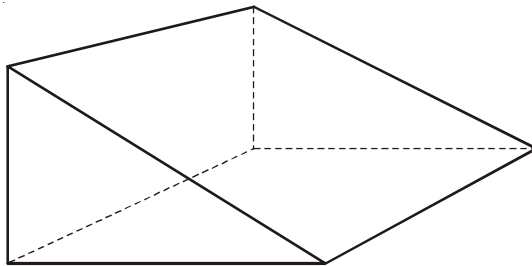
b)



c)



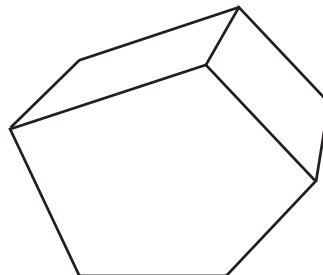
3) Look at this solid.



- a) What is its name?
- b) How many vertices does it have?
- c) How many edges are there?
- d) How many faces does it have?

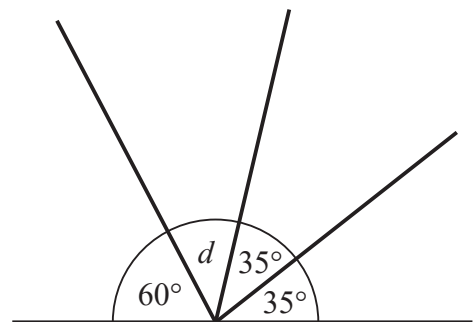
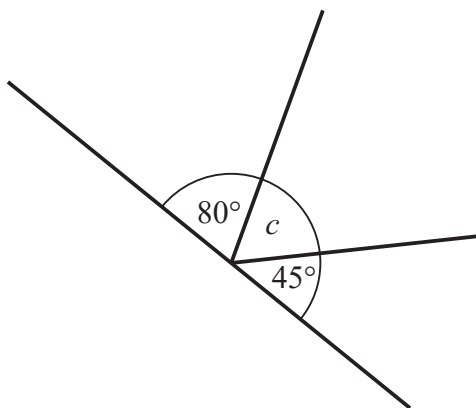
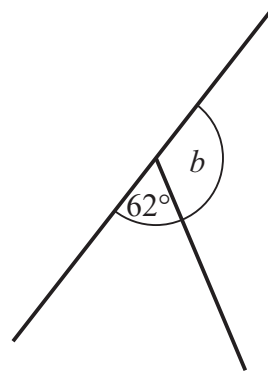
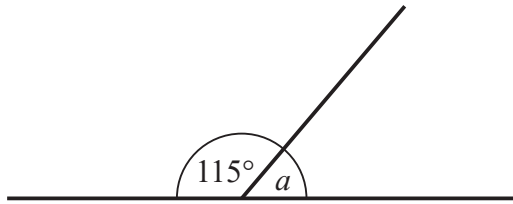
4) This is a picture of a pentagonal prism.

- a) How many faces does it have?
- b) How many edges does it have?
- c) How many vertices does it have?

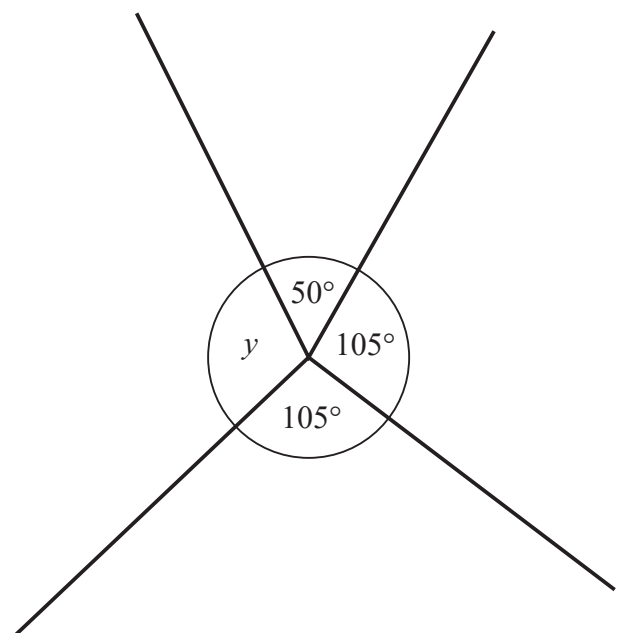
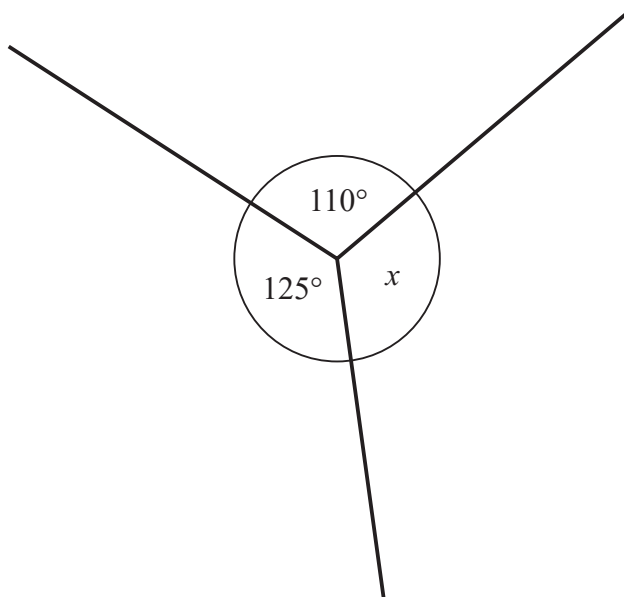


## Angles on a Line and at a Point

- 1) Work out the values of the unknown angles.

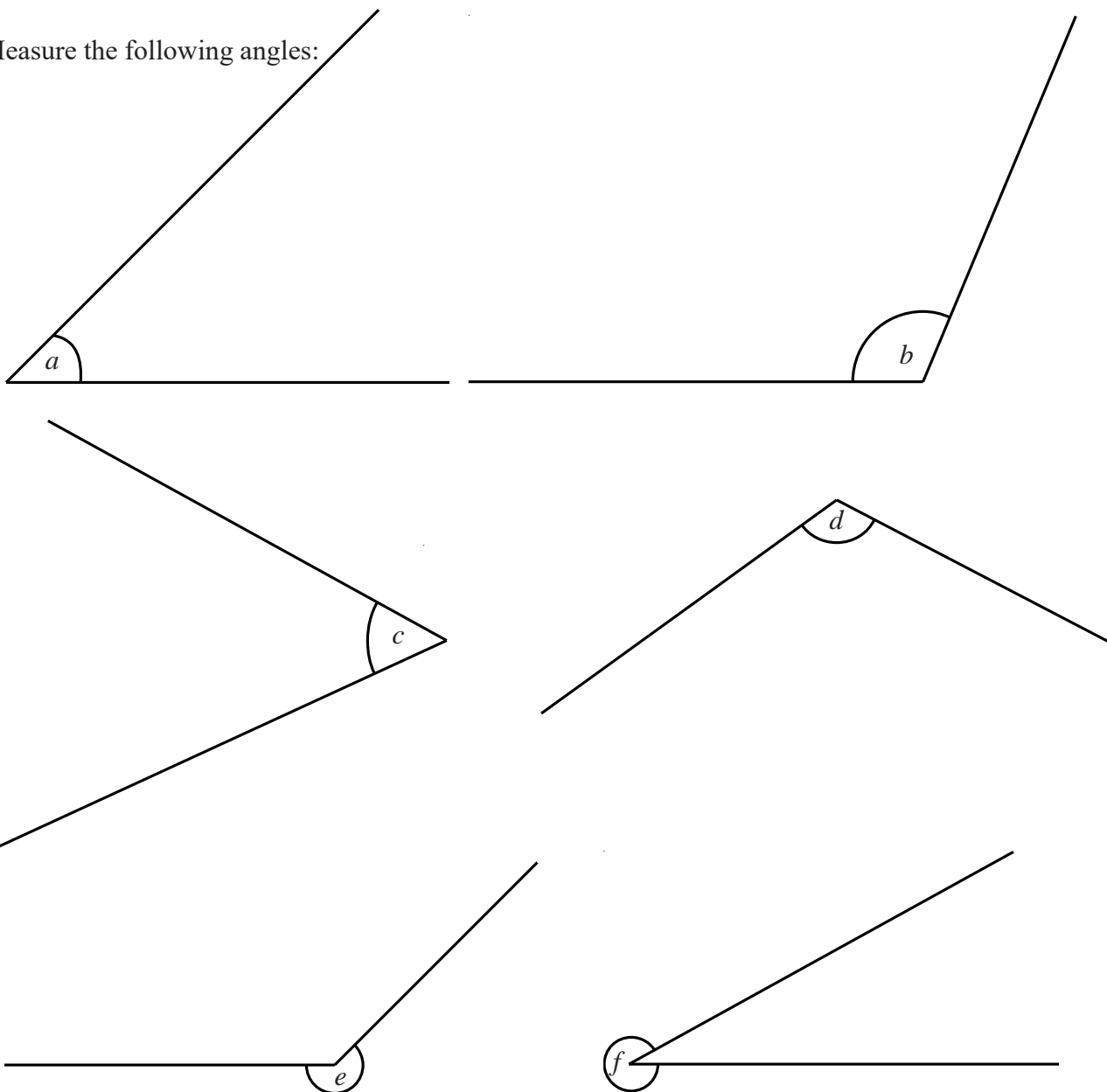


- 2) Work out the values of the unknown angles.



# Measuring and Drawing Angles

1) Measure the following angles:



2) Draw the following angles:

a) Angle  $ABC = 60^\circ$

b) Angle  $PQR = 127^\circ$

c) Angle  $XYZ = 275^\circ$

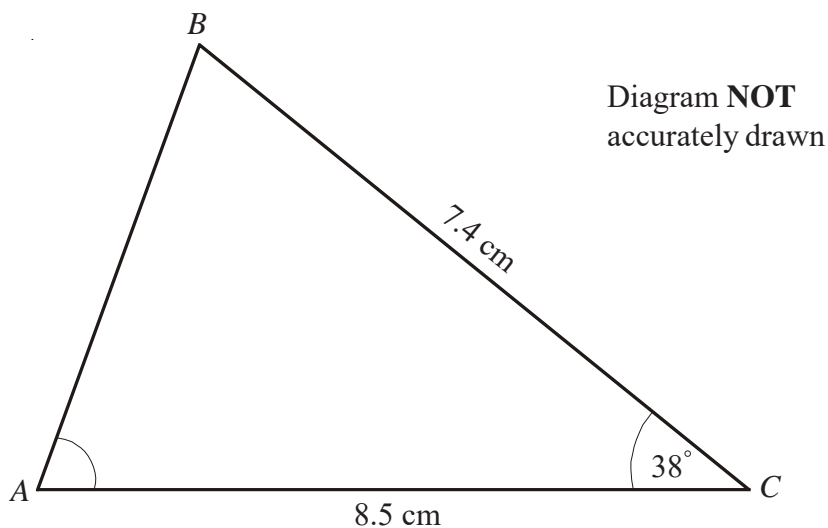
$B$  —————  $A$

$P$  —————  $Q$

$X$   
|  
 $Y$

## Drawing a Triangle Using a Protractor

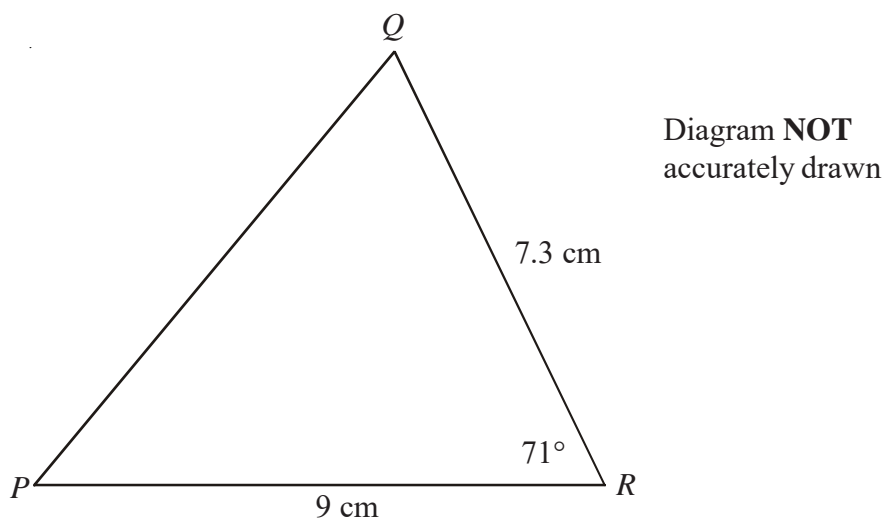
- 1) The diagram shows a sketch of triangle  $ABC$ .



$BC = 7.4 \text{ cm}$   
 $AC = 8.5 \text{ cm}$   
 $\text{Angle } C = 38^\circ$

- Make an accurate drawing of triangle  $ABC$ .
- Measure the size of angle  $A$  on your diagram.

- 2) The diagram shows a sketch of triangle  $PQR$ .



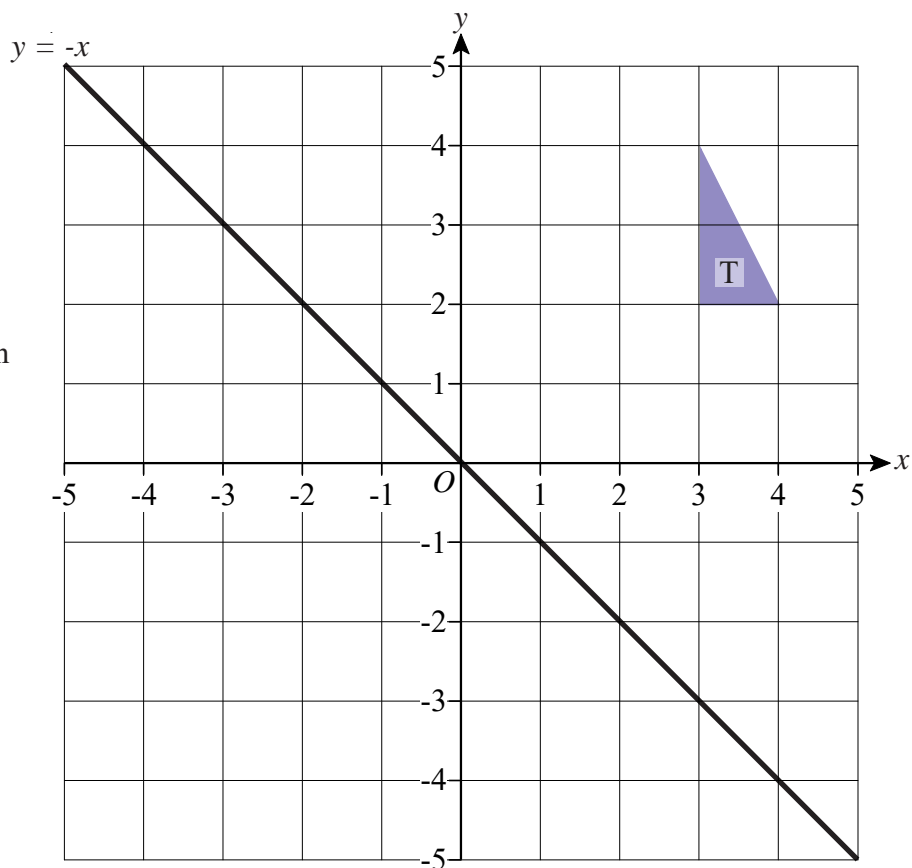
Make an accurate drawing of triangle  $PQR$ .



## Reflections

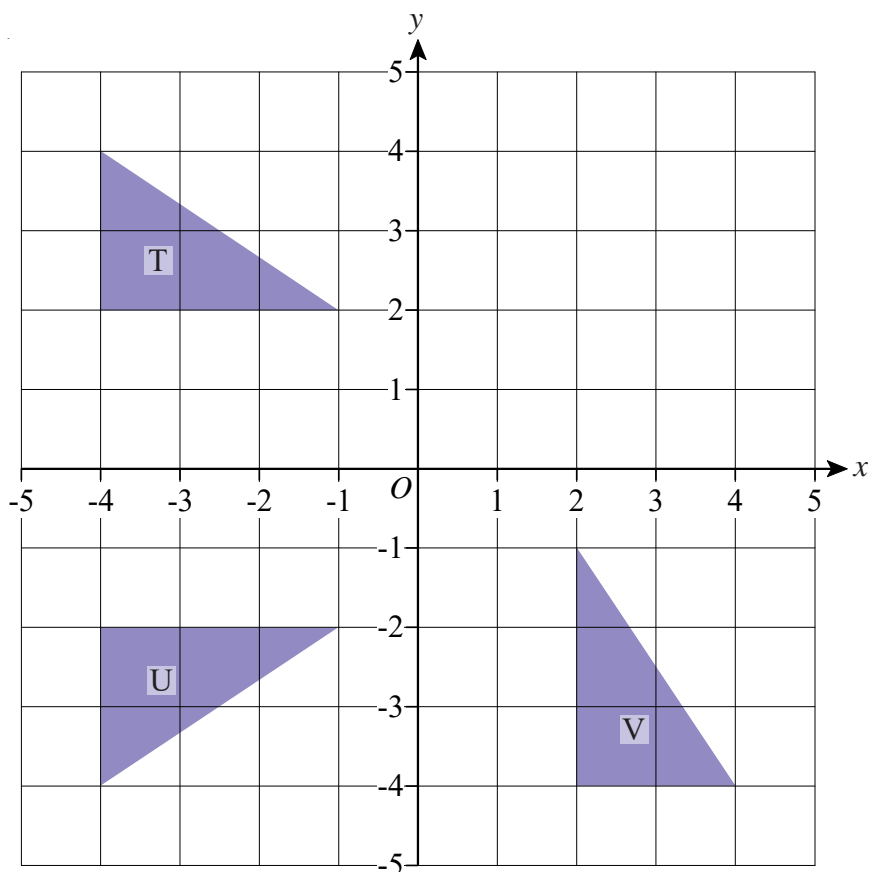
- 1) a) Reflect triangle T in the  $x$  axis.  
Label your new triangle U.

- b) Reflect triangle T in the line with  
equation  $y = -x$ .  
Label your new triangle V.



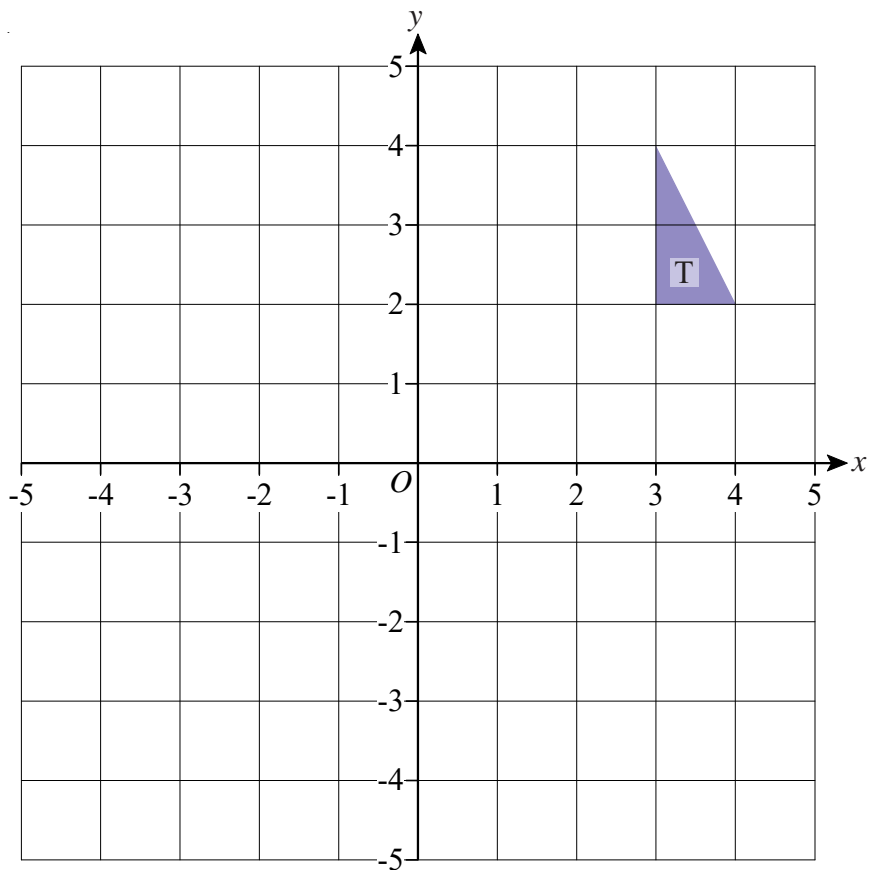
- 2) a) Describe fully the single  
transformation which maps  
triangle T to triangle U.

- b) Describe fully the single  
transformation which maps  
triangle T to triangle V.

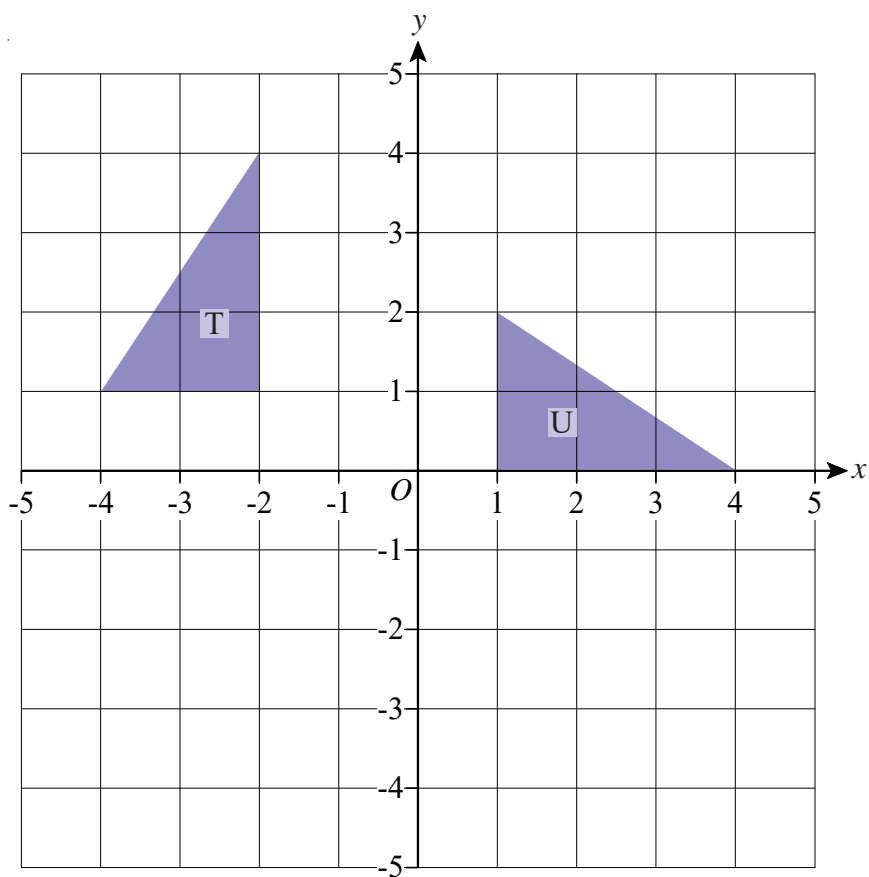


## Rotations

- 1) a) Rotate triangle T  $90^\circ$  anti-clockwise about the point  $(0, 0)$ .  
Label your new triangle U.
- b) Rotate triangle T  $180^\circ$  about the point  $(2, 0)$ .  
Label your new triangle V.

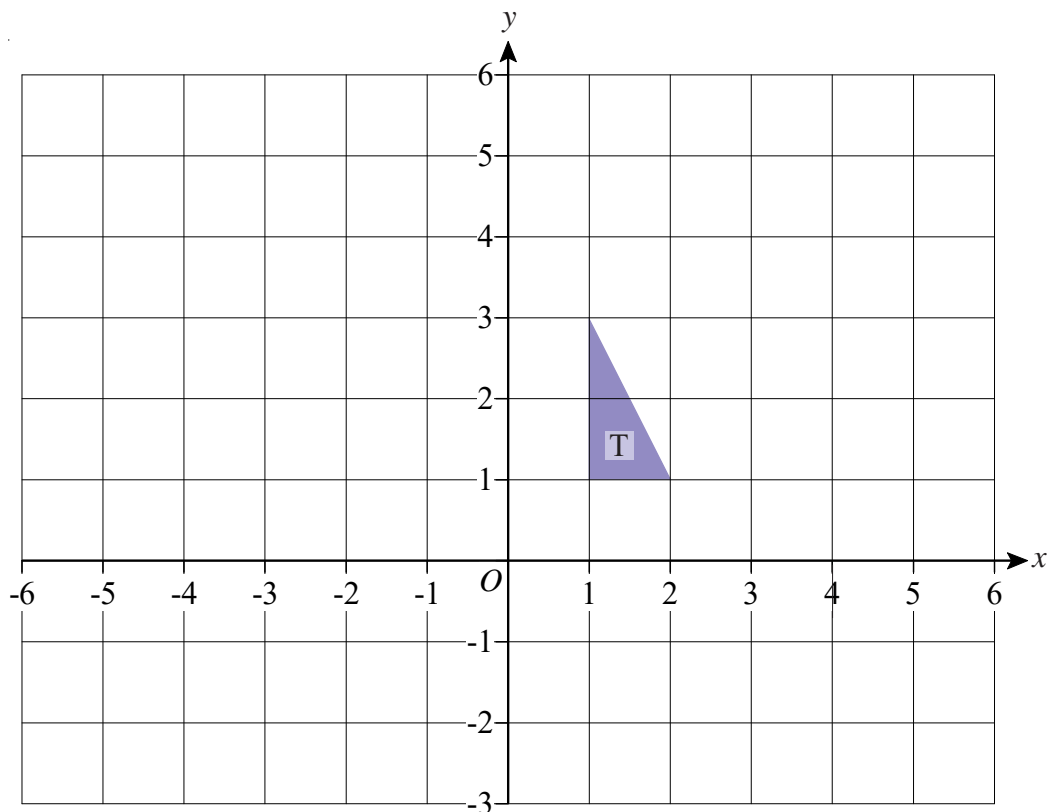


- 2) Describe fully the single transformation which maps triangle T to triangle U.

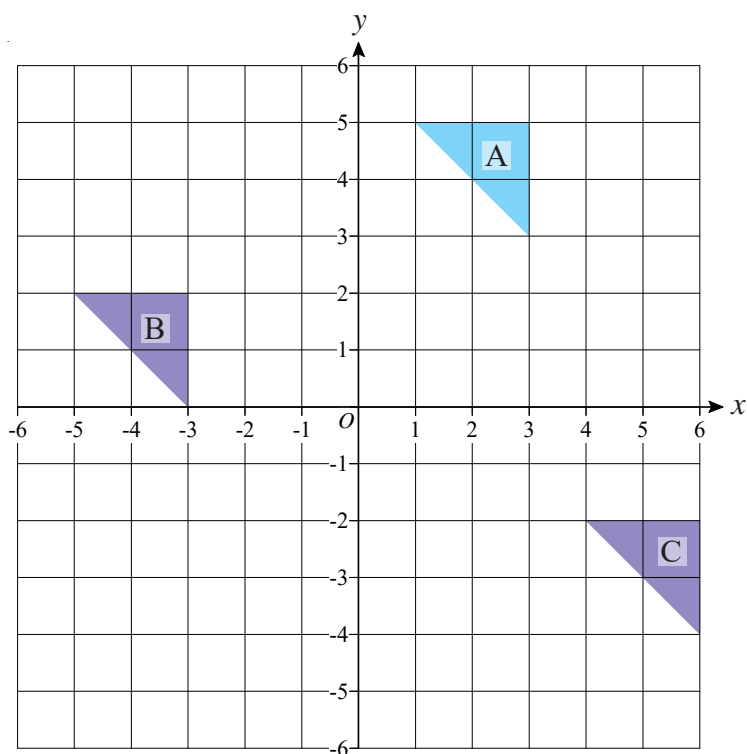


# Translations

- 1) a) Translate triangle T by vector  $\begin{bmatrix} -4 \\ 2 \end{bmatrix}$  and label it U.
- b) Translate triangle T by vector  $\begin{bmatrix} 3 \\ -2 \end{bmatrix}$  and label it V.

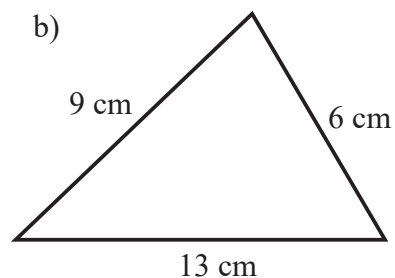
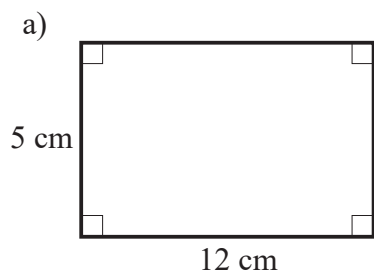


- 2) a) Describe fully the single transformation which maps triangle A to triangle B.
- b) Describe fully the single transformation which maps triangle A to triangle C.



## Perimeters

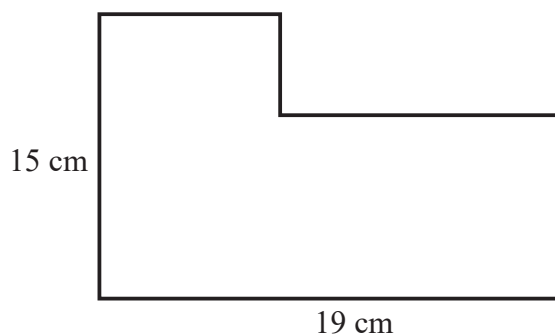
- 1) Find the perimeters of the following two shapes.



- 2) The length of a rectangle is 9 cm.  
The total perimeter is 30 cm.

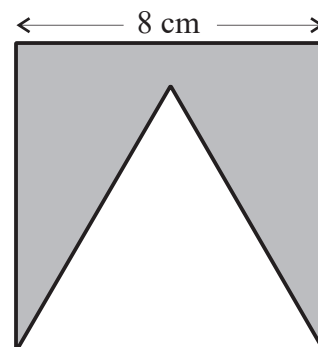
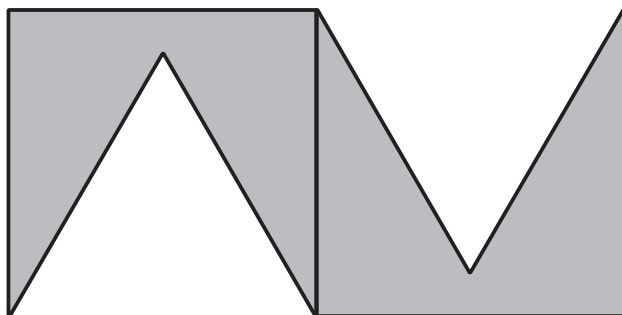
Calculate the length of the width of the rectangle.

- 3) Work out the perimeter of this L shape.



- 4) This shape is made by cutting out an equilateral triangle from a square.

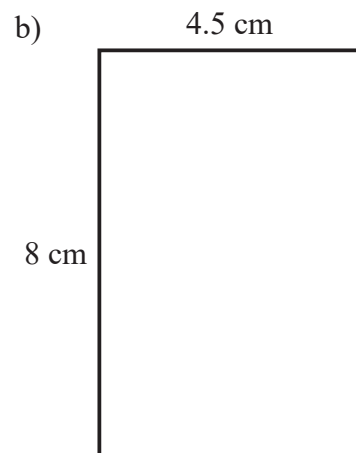
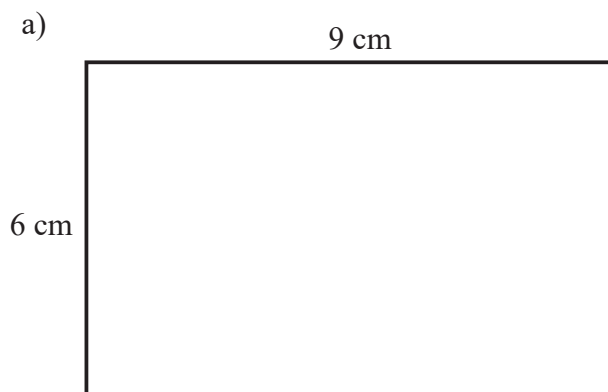
Two of these shapes are then put together to make this shape.



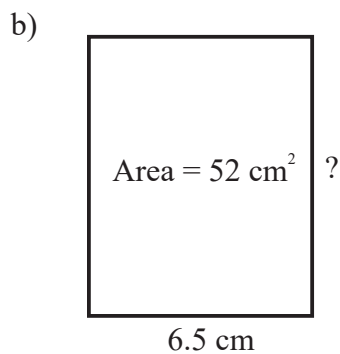
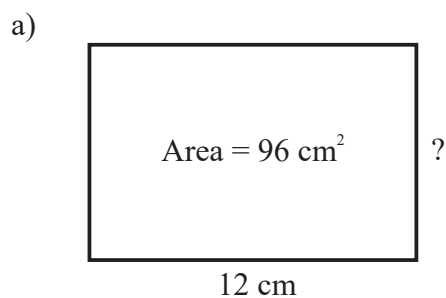
Work out the perimeter of this new shape.

## Area of a Rectangle

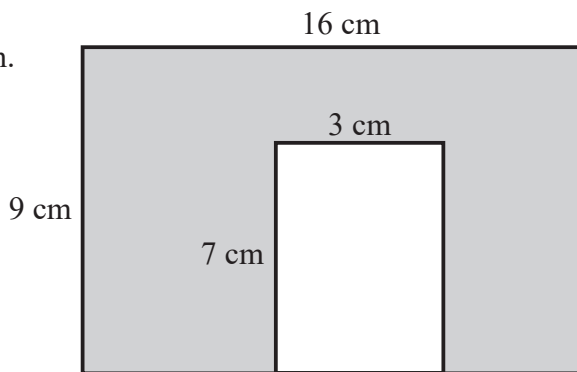
- 1) Find the areas of these two rectangles.



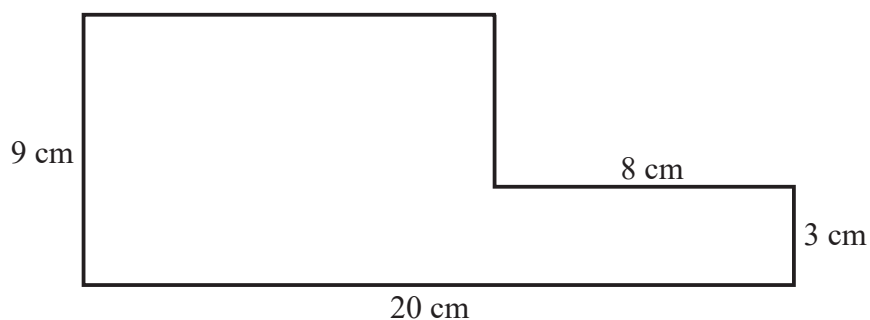
- 2) Find the size of the missing sides in these two rectangles.



- 3) Find the area of the shaded section.

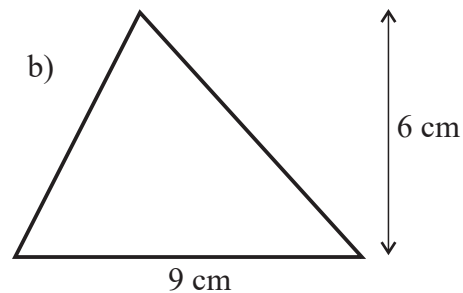
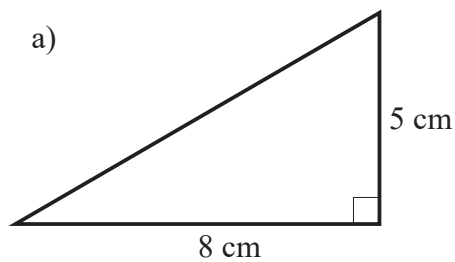


- 4) Find the area of the L shape.

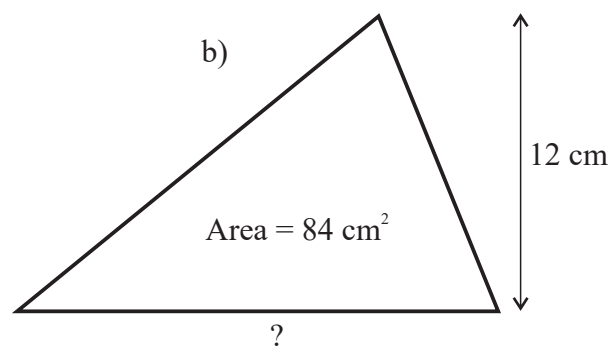
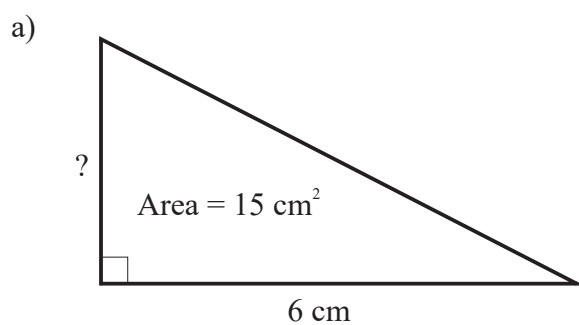


## Area of a Triangle

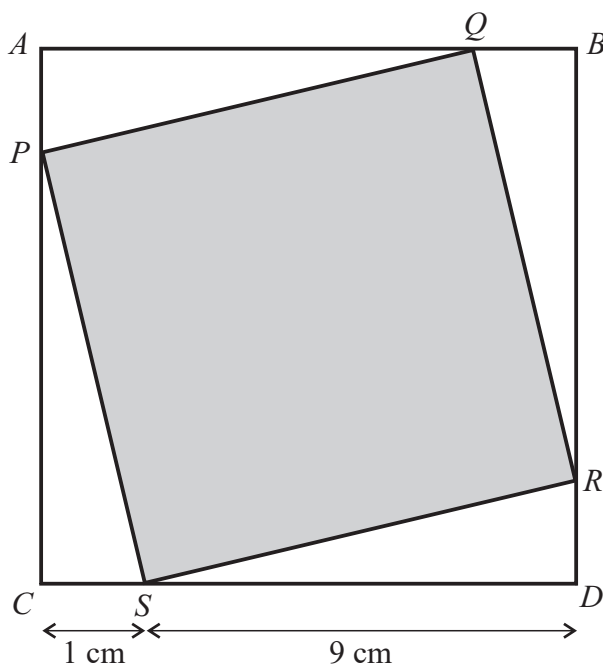
- 1) Find the areas of the following two triangles.



- 2) Find the missing lengths.



- 3)  $ABCD$  is a square.  
 $PQRS$  is a square.

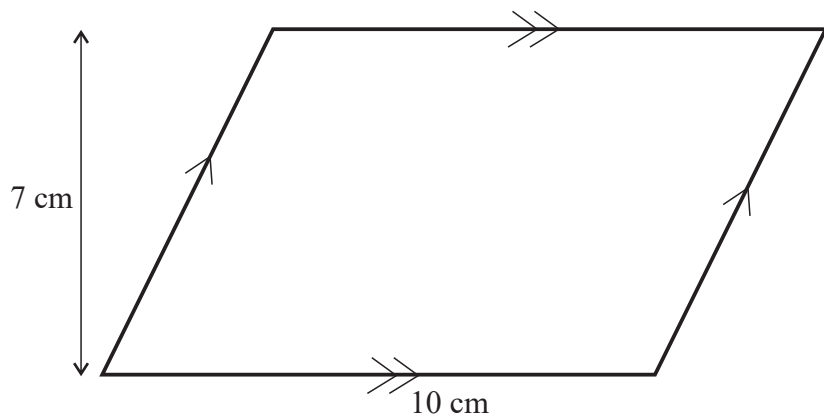


Find the area of the shaded square,  $PQRS$ .

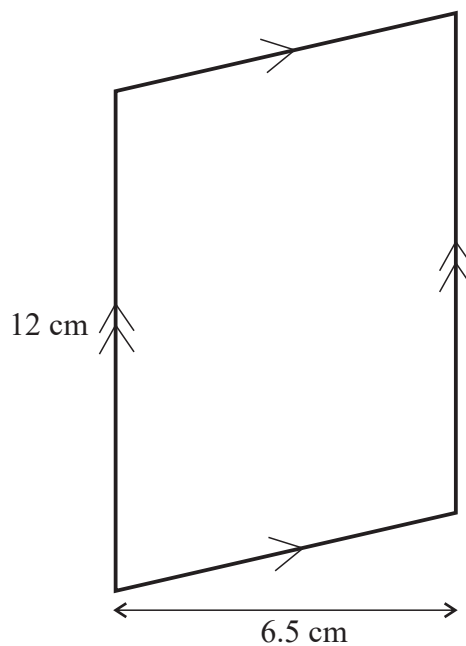
## Area of a Parallelogram

1) Find the area of each of these parallelograms.

a)

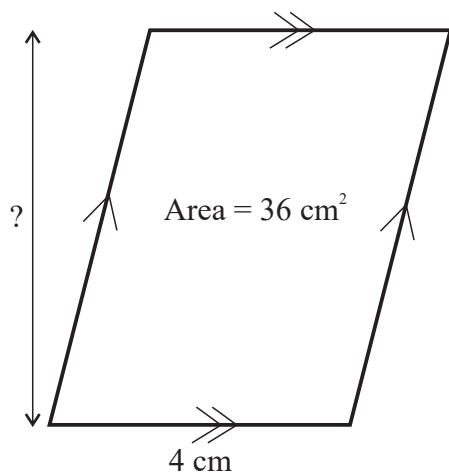


b)

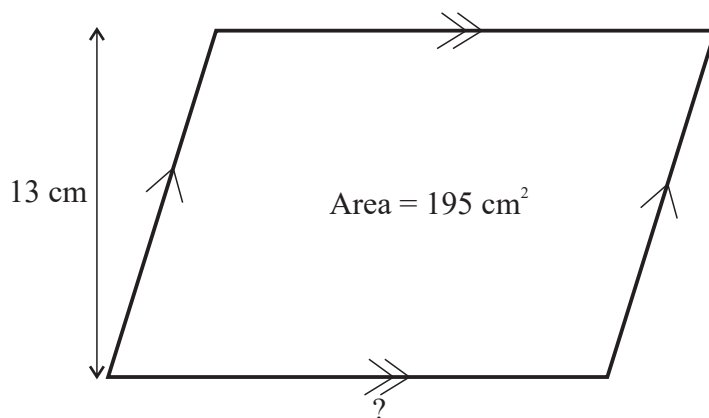


2) Find the missing lengths in these two parallelograms.

a)

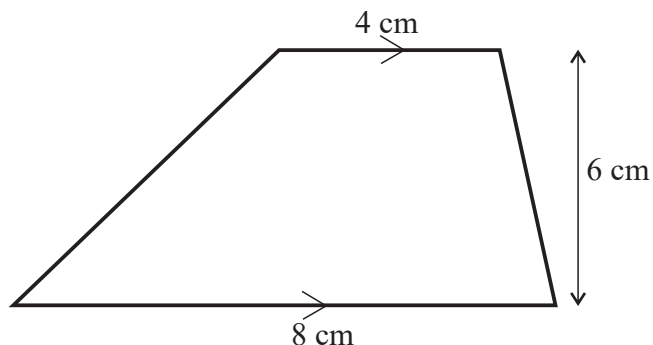


b)

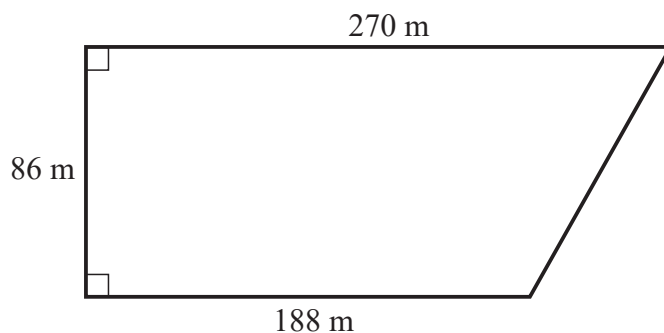


## Area of a Trapezium

- 1) Find the area of this trapezium.



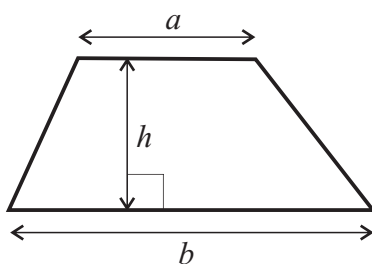
- 2) The diagram shows a field.



Work out the area of the field.



- 3) In the trapezium,  $a = 6.6$  cm,  $b = 8.4$  cm and  $h = 3.6$  cm.

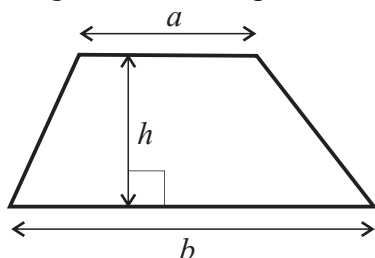


Work out the area of the trapezium.



- 4) In the trapezium below, the area is  $45 \text{ cm}^2$ .  
 $a = 5$  cm and  $b = 10$  cm.

Calculate the height,  $h$ , of the trapezium.



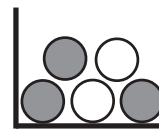


- 1) List all the outcomes if two coins are flipped.
  
- 2)
  - a) How many possible outcomes are there if three coins are flipped?
  - b) List them all - the first one has been done for you: H H H
  
- 3)
  - a) How many possible outcomes are there if two six-sided dice are rolled?
  - b) List them all.
  
- 4)
  - a) How many possible outcomes are there if a coin is flipped and a dice is rolled?
  - b) List them all.
  
- 5)
  - a) How many possible outcomes are there if two coins are flipped and a dice is rolled?
  - b) List them all.
  
- 6) How many possible outcomes are there if 6 coins are flipped?



- 7) If Carly has each fingernail painted at a salon and can choose between red, blue and green for each nail, how many different combinations are there for her to choose from?

- 1) A box contains 3 grey counters and 2 white counters.  
A counter is taken from the box at random.  
What is the probability of choosing a white counter?



- 2) There are 3 blue counters, 5 red counters and 7 green counters in a bag.  
A counter is taken from the bag at random.
- What is the probability that a green counter will be chosen?
  - What is the probability that a blue or red counter will be chosen?
- 3) In a class there are 10 boys and 15 girls.  
A teacher chooses a student at random from the class.  
Eric says that the probability a boy will be chosen is 0.5 because a student can be either a boy or a girl.  
Jenny says that Eric is wrong.  
Decide who is correct - Eric or Jenny - giving reasons for your answer.
- 4) Spinner A has numbers 1 to 4 on it.  
Spinner B has numbers 1 to 3 on it.  
Both spinners are spun and the numbers on each are added together to give a score.  
What is the probability that the score will be
- 7?
  - 3 or 4?

## Mutually Exclusive Events

- 1) If the probability of passing a driving test is 0.54,  
what is the probability of failing it?
  
- 2) The probability that a football team will win their next game is  $\frac{2}{11}$ .  
The probability they will lose is  $\frac{3}{11}$ .  
What is the probability the game will be a draw?



- 3) On the school dinner menu there is only ever one of four options.  
Some of the options are more likely to be on the menu than others.  
The table shows the options available on any day, together with three of the probabilities.

Food	Curry	Sausages	Fish	Casserole
Probability	0.36	0.41		0.09

- a) Work out the probability of the dinner option being Fish.
- b) Which option is most likely?
- c) Work out the probability that it is a Curry or Sausages on any particular day.
- d) Work out the probability that it is **not** Casserole.



- 4) Julie buys a book every week.  
Her favourite types are Novel, Drama, Biography and Romance.  
The table shows the probability that Julie chooses a particular type of book.

Type of book	Novel	Drama	Biography	Romance
Probability	0.24	0.16	$x$	$x$

- a) Work out the probability that she will choose a Novel or a Drama.
- b) Work out the probability that she will choose a Biography or a Romance.

The probability that she will choose a Biography is the same as the probability she will choose a Romance.

- c) Work out the probability that she will choose a Biography.

- 1) Out of the following types of data, decide which is continuous and which is discrete:

The lengths of some roads.

The number of 'cats eyes' on a one mile stretch of road.

The time it takes twenty students to complete an English essay.

The number of pages in twenty students English essays.

The weights of sacks of potatoes.

The number of potatoes in some sacks of potatoes.

The depth of water as the tide comes in and goes out.

The number of crackers in some packets of biscuits.

The weight of the crackers in some packs of biscuits.

- 2) Write a short statement which explains what continuous data is.

- 3) Write a short statement which explains what discrete data is.

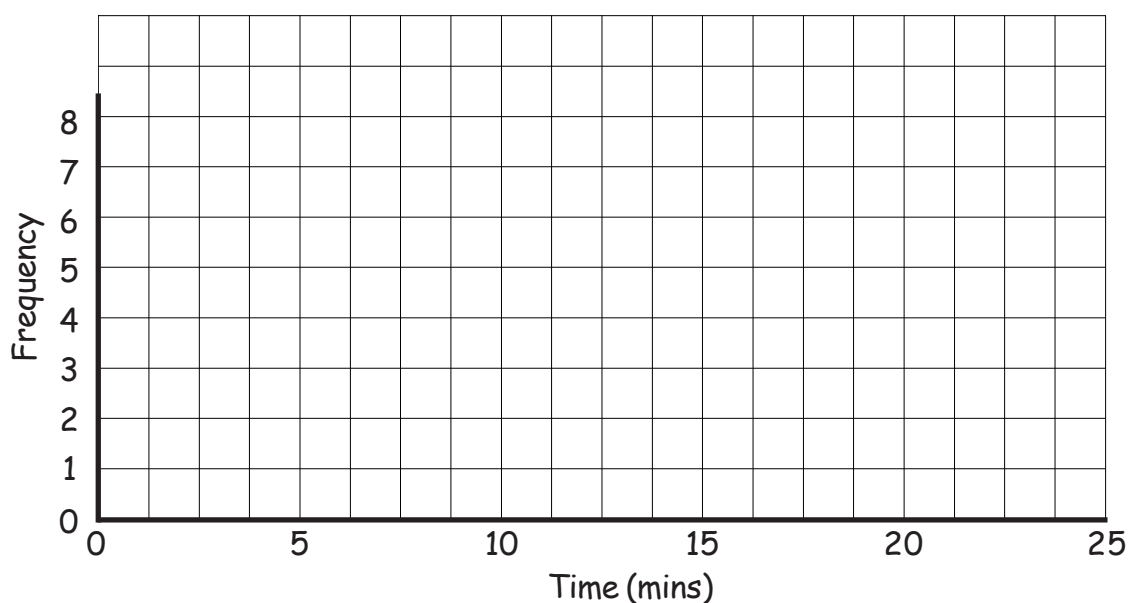
## Frequency Tables and Diagrams

A class of pupils is asked to solve a puzzle.

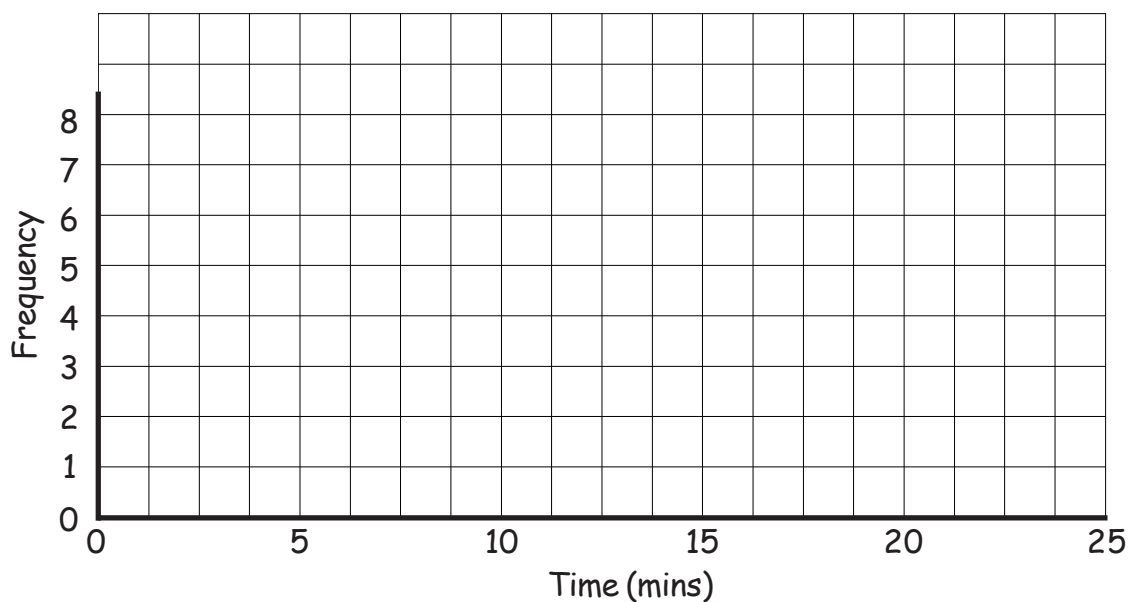
The frequency table below shows the times taken by the pupils to solve the puzzle.

Time ( $t$ ) in min	Frequency
$0 < t \leq 5$	3
$5 < t \leq 10$	4
$10 < t \leq 15$	5
$15 < t \leq 20$	7
$20 < t \leq 25$	5

a) Draw a frequency diagram to show this information.



b) Draw a frequency polygon to show this information.



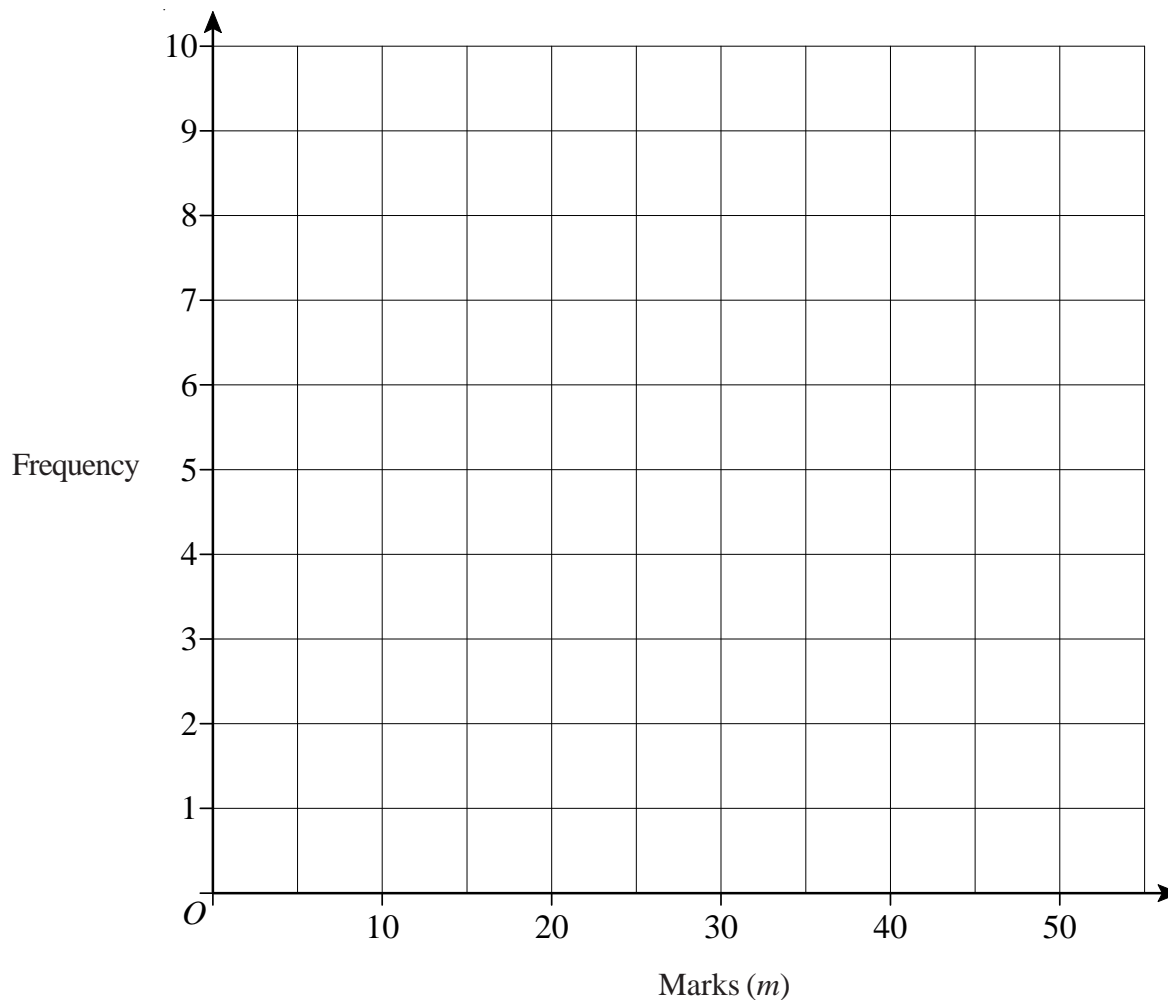
## Frequency Tables and Diagrams

30 students took a test.

The table shows information about how many marks they gained in the test.

Marks ( $m$ )	Frequency
$0 < m < 10$	4
$10 < m < 20$	8
$20 < m < 30$	9
$30 < m < 40$	6
$40 < m < 50$	3

On the grid, draw a frequency polygon for this information.



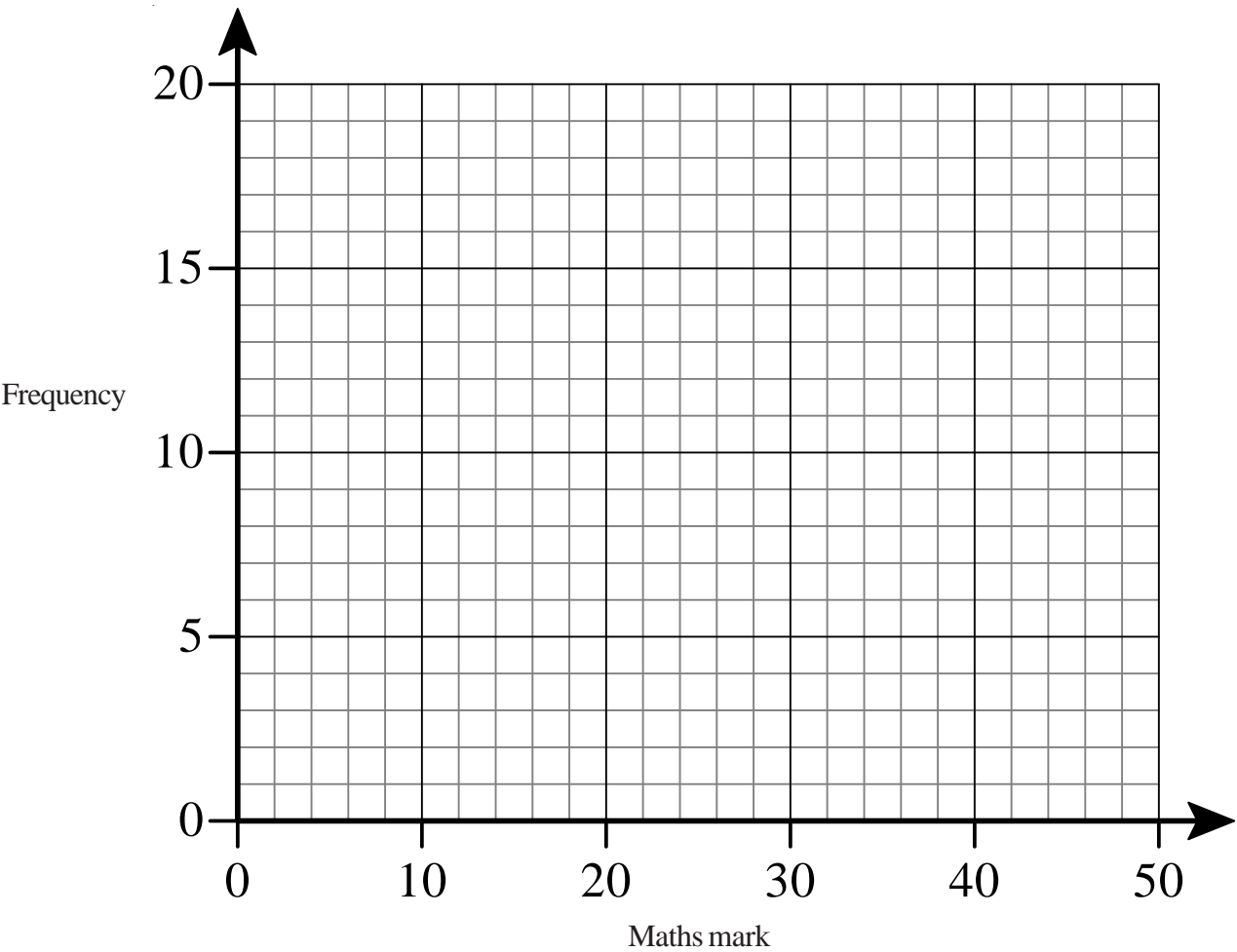
Frequency Tables and Diagrams

60 students take a Maths test.  
The test is marked out of 50.

This table shows information about students' marks.

Maths mark	0 - 10	11 - 20	21 - 30	31 - 40	41 - 50
Frequency	3	13	18	19	7

On the grid, draw a frequency polygon to show this information.



- 1) Work out
  - a)  $6 \times 0.2$
  - b)  $0.2 \times 0.3$
  - c)  $0.4 \times 7$
  - d)  $0.2 \times 0.8$
  - e)  $0.03 \times 0.9$
  - f)  $1.5 \times 0.2$
  
- 2) A box contains 7 books, each weighing 2.5 kg.  
Work out the total weight of the box.
  
- 3) Jim takes 13 boxes out of his van.  
The weight of each box is 25.5 kg.  
Work out the total weight of the 13 boxes.
  
- 4) Tim has a job which pays £6.85 per hour.  
If he works for 34 hours, one week, how much does he earn?
  
- 5) Sue has a part-time job and the hourly pay is £7.50 per hour.  
How much does she earn if she works for 8.5 hours, one week?
  
- 6) Fencing costs £13.25 per metre.  
How much does 12.5 m cost?



1) Work out

a)  $9 \div 0.3$

b)  $6 \div 0.1$

c)  $12 \div 0.4$

d)  $25 \div 0.5$

e)  $21 \div 0.3$

f)  $15 \div 0.2$

2) Work out

a)  $3.6 \div 0.4$

b)  $0.8 \div 0.2$

c)  $2.4 \div 0.4$

d)  $0.56 \div 0.08$

e)  $5.5 \div 0.05$

f)  $8.1 \div 0.09$

3) John takes boxes out of his van.

The total weight of the boxes is 4.9 kg

The weight of each box is 0.7 kg

Work out the number of boxes in John's van.

4) Mr Rogers bought a bag of elastic bands for £6

Each elastic band costs 12p.

Work out the number of elastic bands in the bag.

1) Work out the following:

a)  $2 - 7$

b)  $4 - 6$

c)  $1 - 8$

d)  $0 - 4$

2) Work out the following:

a)  $-3 + 2$

b)  $-7 + 5$

c)  $-3 + 8$

d)  $-9 + 11$

3) Work out the following:

a)  $-1 - 3$

b)  $-4 - 5$

c)  $-7 - 8$

d)  $-2 - 12$

4) Work out the following:

a)  $6 - -3$

b)  $-3 - -5$

c)  $-9 - -2$

d)  $1 - -13$

5) Work out the following:

a)  $-3 \times 4$

b)  $5 \times -2$

c)  $-4 \times -5$

d)  $-6 \times -3$

6) Work out the following:

a)  $12 \div -4$

b)  $-20 \div -2$

c)  $-15 \div 3$

d)  $-100 \div -5$

- 1) Put these fractions in order of size, smallest to largest.  
Show your working for each question.

a)  $\frac{1}{2}$        $\frac{1}{3}$

b)  $\frac{3}{5}$        $\frac{2}{3}$

c)  $\frac{1}{2}$        $\frac{3}{8}$

- 2) Put these fractions in order of size, smallest to largest.  
Show your working for each question.

a)  $\frac{1}{2}$        $\frac{1}{4}$        $\frac{3}{8}$

b)  $\frac{3}{5}$        $\frac{1}{2}$        $\frac{3}{4}$

c)  $\frac{5}{6}$        $\frac{2}{3}$        $\frac{3}{4}$

- 3) Put these fractions in order of size, smallest to largest.  
Show your working for each question.

a)  $\frac{2}{3}$        $\frac{7}{12}$        $\frac{3}{4}$        $\frac{5}{6}$

b)  $\frac{5}{8}$        $\frac{2}{3}$        $\frac{3}{24}$        $\frac{7}{12}$

c)  $\frac{6}{10}$        $\frac{4}{5}$        $\frac{5}{12}$        $\frac{8}{15}$

- 4) Ben spent his pocket money this way:

$\frac{7}{20}$  on magazines

$\frac{4}{10}$  on chocolates

$\frac{1}{4}$  on games

Order the items Ben bought by value, largest first.  
Show all your working.

## Adding and Subtracting Fractions

In all the questions on this page, please give your answers in their simplest form.

1) Work out the following:

a)  $\frac{1}{7} + \frac{3}{7}$

b)  $\frac{4}{9} + \frac{1}{9}$

2) Work out the following:

a)  $\frac{1}{5} + \frac{3}{4}$

b)  $\frac{3}{8} + \frac{1}{4}$

c)  $\frac{2}{3} + \frac{3}{10}$

d)  $\frac{1}{2} + \frac{2}{5}$

3) Work out the following:

a)  $\frac{2}{3} + \frac{1}{2}$

b)  $\frac{3}{5} + \frac{2}{3}$

c)  $\frac{5}{8} + \frac{3}{4}$

d)  $\frac{5}{7} + \frac{2}{5}$

4) Work out the following:

a)  $2\frac{1}{2} + 1\frac{3}{4}$

b)  $1\frac{2}{5} + \frac{2}{3}$

c)  $2\frac{1}{6} + 1\frac{1}{2}$

d)  $1\frac{3}{7} + \frac{2}{5}$

5) Work out the following:

a)  $\frac{3}{4} - \frac{1}{2}$

b)  $\frac{5}{7} - \frac{2}{3}$

c)  $\frac{5}{8} - \frac{1}{3}$

d)  $\frac{8}{9} - \frac{2}{3}$

6) Work out the following:

a)  $2\frac{1}{2} - 1\frac{3}{4}$

b)  $1\frac{2}{3} - \frac{3}{4}$

c)  $3\frac{2}{5} - 1\frac{1}{2}$

d)  $2\frac{3}{8} - \frac{3}{5}$

7) Ted received his pocket money on Friday.

He spent  $\frac{3}{5}$  of his pocket money on games.

He spent  $\frac{1}{10}$  of his pocket money on magazines.

What fraction of his pocket money did he have left?

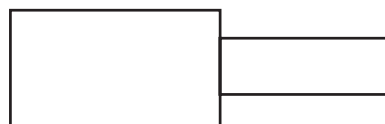
8) Maisie buys a bag of flour.

She uses  $\frac{1}{4}$  to bake a cake and  $\frac{2}{5}$  to make a loaf.

a) What fraction of the bag of flour was used?

b) What fraction of the bag of flour is left?

9) Work out the total length of this shape.  
Give your answer as a mixed number.



$\leftarrow 3\frac{1}{4} \text{ inches} \rightarrow$   $\leftarrow 2\frac{2}{3} \text{ inches} \rightarrow$

## Finding a Fraction of an Amount

1) Work out these amounts.

a)  $\frac{3}{4}$  of £20

b)  $\frac{2}{3}$  of 60 kg

c)  $\frac{3}{8} \times 24$

d)  $150 \times \frac{2}{3}$

e)  $\frac{2}{9}$  of 180 cm

f)  $49 \times \frac{4}{7}$

g)  $60 \times \frac{1}{4}$

h)  $\frac{5}{8}$  of £48

i)  $4000 \times \frac{7}{8}$

2) There are 600 apples on a tree and there are maggots in  $\frac{3}{5}$  of them.

How many apples have maggots in them?

3) Liz and Lee are travelling in a car from Glasgow to Poole (770 km).

At midday they had already travelled  $\frac{5}{7}$  of the total distance.

What distance, in km, had they travelled by midday?

4) A digital camera that cost £49 was sold on eBay for  $\frac{3}{7}$  of the original price.

What was the selling price?

5) Yesterday Thomas travelled a total of 175 miles.

He travelled  $\frac{2}{5}$  of this distance in the morning.

How many miles did he travel during the rest of the day?

6) Debra received her £15 pocket money on Saturday.

She spent  $\frac{1}{3}$  of her pocket money on magazines.

She spent  $\frac{2}{5}$  of her pocket money on a necklace.

How much of the £15 did she have left?

*In all the questions on this page, please give your answers in their simplest form.*

1) Work out the following:

a)  $\frac{1}{2} \times \frac{1}{2}$

b)  $\frac{2}{3} \times \frac{1}{3}$

c)  $\frac{3}{5} \times \frac{2}{7}$

d)  $\frac{4}{7} \times \frac{5}{9}$

2) Work out the following:

a)  $\frac{1}{2} \times \frac{2}{3}$

b)  $\frac{3}{4} \times \frac{8}{11}$

c)  $\frac{2}{9} \times \frac{3}{4}$

d)  $\frac{4}{5} \times \frac{1}{12}$

3) Work out the following:

a)  $1\frac{1}{2} \times \frac{1}{3}$

b)  $\frac{2}{3} \times 2\frac{2}{5}$

c)  $3\frac{1}{2} \times 1\frac{1}{2}$

d)  $1\frac{2}{7} \times 3\frac{1}{3}$

*In all the questions on this page, please give your answers in their simplest form.*

1) Work out the following:

a)  $\frac{2}{5} \div \frac{3}{4}$

b)  $\frac{1}{7} \div \frac{3}{5}$

c)  $\frac{4}{9} \div \frac{1}{2}$

d)  $\frac{3}{10} \div \frac{5}{9}$

2) Work out the following:

a)  $\frac{1}{2} \div \frac{1}{3}$

b)  $\frac{3}{7} \div \frac{4}{7}$

c)  $\frac{1}{9} \div \frac{2}{3}$

d)  $\frac{2}{5} \div \frac{3}{10}$

3) Work out the following:

a)  $1\frac{1}{3} \div \frac{1}{4}$

b)  $\frac{3}{5} \div 2\frac{2}{3}$

c)  $3\frac{2}{3} \div 1\frac{1}{5}$

d)  $4\frac{1}{2} \div 1\frac{1}{2}$

1)  $6 \times 5 + 2$

2)  $2 + 6 \times 5$

3)  $35 - 4 \times 3$

4)  $48 \div (14 - 2)$

5)  $27 \div (3 + 6)$

6)  $27 \div 3 + 6$

7)  $(9 + 2) \times 2 + 5$

8)  $4 \times (1 + 4) - 6$

9)  $6 \times 4 - 3 \times 5$

10)  $\frac{9+3}{4+2}$

11)  $\frac{23+9}{7-3}$

12)  $\frac{7-2^2}{4^2-15}$

13)  $\frac{5^2+3}{2 \times 7}$

14)  $\frac{5 \times 6 - 4}{13}$

15)  $\frac{8 \times 2 - 4}{3 + 1^2}$

16)  $\frac{12 - 3 \times 2}{14 \div 7}$

17)  $\frac{20 - 3^2}{10 - (5 + 4)}$

18)  $\frac{3 + 9 \times 8}{1 + 6 \times 4}$





- 1) Use your calculator to work out

$$\frac{23.7 \times 14.2}{8.4 \times 3.2}$$

Write down all the figures on your calculator display.



- 2) Use your calculator to work out

$$\frac{\sqrt{21.4}}{5.7 - 2.35}$$

Write down all the figures on your calculator display.



- 3) Work out  $\frac{5.8 + 4.65}{3.1^2 + 1.62}$

Write down all the figures on your calculator display.



- 4) Use your calculator to work out the value of

$$\frac{9.2 \times 16.3}{9.4 - 5.71}$$

Write down all the digits from your calculator.  
Give your answer as a decimal.



- 5) Use your calculator to work out

$$\frac{3}{2.1 + 3.45}$$

Write down all the figures on your calculator display.  
You must give your answer as a decimal.



- 6) Use your calculator to work out

$$\frac{15^2 - 12^2}{\sqrt{9.6 - 3.87}}$$

Write down all the figures on your calculator display.  
You must give your answer as a decimal.



- 7) Use a calculator to work out

$$\sqrt{\frac{22.4 \times 13.9}{3.6}}$$

Write down all the figures on your calculator display.

1) Tony buys

4 kg of potatoes at £1.60 per kilogram

and

2 kg of onions at £1.80 per kilogram.

She pays with a £20 note.

How much change should she receive?

2)

Bags of sweets
£1.50 per bag
Buy 3, get 1 free

How many bags of sweets can you buy for £9?



3)

**Cinema Prices**

Adult	£2.99
Child	£2.30
Family ticket (2 adults and 2 children)	£9.00

a) 1 adult and 7 children went to the cinema.

How much did they pay altogether?

b) 2 adults and 2 children went to the cinema and bought a family ticket.

How much did they save altogether?

- 1) List the first seven prime numbers.
- 2) Express the following numbers as the product of their prime factors:
  - a) 12
  - b) 20
  - c) 30
  - d) 24
- 3) Express the following numbers as the product of their prime factors:
  - a) 64
  - b) 100
  - c) 150
- 4) Express the following numbers as the product of their prime factors:
  - a) 175
  - b) 192
  - c) 315
- 5) The number 96 can be written as  $2^m \times n$ , where  $m$  and  $n$  are prime numbers.  
Find the value of  $m$  and the value of  $n$ .
- 6) The number 75 can be written as  $5^x \times y$ , where  $x$  and  $y$  are prime numbers.  
Find the value of  $x$  and the value of  $y$ .

- 1) What is the value of  $5^2$ ?
- 2) What is the value of  $8^2$ ?
- 3) These are the first five square numbers: 1, 4, 9, 16, 25
  - a) What is the sixth square number?
  - b) What is the 10th square number?
- 4) Which square number lies between 60 and 70?
- 5) What is the value of  $2^3$ ?
- 6) What is the value of  $4^3$ ?
- 7) Work out  $1^3 + 2^3 + 3^3$
- 8) Work out  $\sqrt{25}$
- 9) Work out  $\sqrt{49}$
- 10) Work out the value of  $\sqrt{121} \times \sqrt{121}$
- 11) Match together cards with the same answer

$9^2$	$\sqrt{9}$	81	$5^3$
$2^5$	125	32	3

1) Evaluate the following:

a)  $2^3$

b)  $3^2$

c)  $10^4$

2) Evaluate the following:

a)  $2^8$

b)  $6^4$

c)  $5^6$

3) Find the value of

a)  $2^4 + 3^2$

b)  $5^2 - 2^3$

c)  $1^2 + 2^2 + 3^2$

4) Find the value of

a)  $5^4 + 6^3$

b)  $3^4 \times 2^5$

c)  $9^3 - 6^3$

5) Find the value of

$$2^2 + 3^2 + 5^2 + 7^2 + 11^2 + 13^2 + 17^2$$

Write the following fractions as decimals

1)  $\frac{3}{10}$

2)  $\frac{7}{10}$

3)  $\frac{9}{100}$

4)  $\frac{1}{2}$

5)  $\frac{3}{4}$

6)  $\frac{2}{5}$

7)  $\frac{7}{20}$

8)  $\frac{1}{3}$

9)  $\frac{1}{8}$

10)  $\frac{5}{8}$

1) Write the following fractions as decimals and percentages:

eg.  $\frac{1}{10} \xrightarrow{1 \div 10} 0.1 \xrightarrow{0.1 \times 100} 10\%$

a)  $\frac{3}{10} =$

b)  $\frac{1}{5} =$

c)  $\frac{2}{5} =$

d)  $\frac{1}{4} =$

e)  $\frac{3}{4} =$

f)  $\frac{1}{2} =$

g)  $\frac{1}{3} =$

2) Fill in the blanks in the table below:

Fraction	Decimal	Percentage
$\frac{6}{10}$		
	0.2	
	0.9	
		40%
		25%
$\frac{4}{5}$		
$\frac{12}{100}$		
	$0.\dot{3}$	
		70%

1) Write down the reciprocal of

a) 8

b) 3

c) 1

d) 12

2) Write down the reciprocal of

a)  $\frac{1}{2}$

b)  $\frac{1}{3}$

c)  $\frac{4}{3}$

d)  $\frac{5}{8}$

3) Write down the reciprocal of

a) 0.1

b) 0.5

c) 0.2

4) Why can't we have a reciprocal of 0?



## Percentage of an Amount with a Calculator



1) Work out:

- a) 21% of £340
- b) 64% of £1080
- c) 36% of £800
- d) 98% of £13



2) Work out:

- a) 17.5% of £58
- b) 20% of £5.40
- c) 61.7% of £2000
- d) 17.5% of £68.40



3) A computer costs £406 plus VAT at 20%.

Work out the total cost of the computer.



4) A car is usually priced at £9800 but now has a discount of 8%.

What is the new price of the car?



5) 9500 people attend a festival and 22% of them are children.

How many children are at the festival?



6) 65% of a car, by weight, is steel and iron.

If a car weighs 1100 kg, what is the weight of steel and iron in the car?



7) Tony earns £17800 per year and receives a 3.8% pay rise.

How much does he now earn?

- 1) Work out:
  - a) 10% of £170
  - b) 10% of £6800
  - c) 10% of £923
  - d) 10% of £16
  
- 2) Work out:
  - a) 20% of £60
  - b) 30% of £90
  - c) 15% of £800
  - d) 15% of £68
  
- 3) Work out:
  - a) 35% of £80
  - b) 90% of £160
  - c) 17.5% of £600
  - d) 17.5% of £850
  
- 4) Work out:
  - a) 15% of £4.60
  - b) 40% of £2.80
  - c) 17.5% of £3.20
  - d) 97.5% of £24
  
- 5) The normal price of a jacket is £54.  
In a sale, the price is reduced by 30%  
What is the sale price?
  
- 6) A football costs £14 plus 20% VAT.  
How much is the football?



1) Write the following as percentages, giving all your answers to 1 decimal place.

- a) 12 out of 34
- b) 62 out of 85
- c) 113 out of 153
- d) 2150 out of 3452



2) Sarah sat a Science test and got a score of 64 marks out of 112 possible marks.  
What was her mark as a percentage?  
Give your answer to 1 decimal place.



3) In a class of 32 students, 18 of them are boys.  
What percentage of the class are boys?  
Give your answer to 1 decimal place.



4) In a French class there are 13 girls and 6 boys.  
What percentage of the class are girls?  
Give your answer to 1 decimal place.



5) A new car usually costs £8500.  
Henry gets a discount of £1000.  
What is the discount as a percentage of the usual cost?  
Give your answer to 1 decimal place.



6) Write out £148 as a percentage of £600.  
Give your answer to 1 decimal place.



7) In a wood there are 200 oak trees, 650 silver birch trees and 400 wild cherry trees.  
What percentage of the trees are oak trees?



8) In England in 2010 there were 68820 deaths caused by cancer.  
Of these deaths, 37500 were caused by smoking.  
What percentage of deaths due to cancer were caused by smoking?  
Give your answer to 1 decimal place.

- 1) Write the following as percentages.
  - a) 12 out of 50
  - b) 15 out of 25
  - c) 8 out of 10
  - d) 11 out of 20
  - e) 4 out of 5
  - f) 32 out of 40
  - g) 12 out of 80
  - h) 640 out of 800
  - i) 36 out of 60
  
- 2) Tim got 17 out of 20 in a French test.  
Write 17 out of 20 as a percentage.
  
- 3) Write £19 as a percentage of £25
  
- 4) Work out £14 as a percentage of £40
  
- 5) A baker burnt 12 loaves out of the 200 loaves he baked.  
What percentage of the 200 loaves did he burn?
  
- 6) What is £380 as a percentage of £400?
  
- 7) What is £22 as a percentage of £40?
  
- 8) If there are 9 girls and 11 boys in a class, what percentage of the class are girls?

## Percentages



- 1) Find the following to the nearest penny:
  - a) 23% of £670
  - b) 12% of £580
  - c) 48% of £64
  - d) 13% of £7.50
  - e) 87% of £44
  - f) 15.7% of £7000
  - g) 23.8% of £980
  - h) 34% of £16.34
  - i) 48.6% of £971.26
  - j) 78.24% of £12.82
  - k) 42.15% of £7876.42
  - l) 0.57% of £60000

- 2) Find the following:
  - a) 10% of £700
  - b) 10% of £400
  - c) 10% of £350
  - d) 10% of £530
  - e) 10% of £68
  - f) 10% of £46
  - g) 10% of £6.50
  - h) 10% of £12.20
  - i) 20% of £600
  - j) 30% of £900
  - k) 60% of £800
  - l) 20% of £650
  - m) 40% of £320
  - n) 15% of £300
  - o) 15% of £360
  - p) 65% of £12000
  - q) 45% of £64
  - r) 85% of £96
  - s) 17.5% of £800
  - t) 17.5% of £40
  - u) 17.5% of £8.80



- 3) Change the following to percentages, giving all answers to 1 decimal place:
  - a) 6 out of 28
  - b) 18 out of 37
  - c) 42 out of 83
  - d) 24 out of 96
  - e) 73 out of 403
  - f) 234 out of 659
  - g) 871 out of 903
  - h) 4.7 out of 23
  - i) 6.9 out of 79
  - j) 14.8 out of 23.6
  - k) 65.8 out of 203.7

- 4) Change the following to percentages:
  - a) 46 out of 100
  - b) 18 out of 50
  - c) 7 out of 25
  - d) 23 out of 25
  - e) 9 out of 20
  - f) 16 out of 20
  - g) 7 out of 10
  - h) 9.5 out of 10
  - i) 10 out of 40
  - j) 16 out of 40
  - k) 30 out of 40
  - l) 12 out of 40
  - m) 28 out of 80
  - n) 32 out of 80
  - o) 60 out of 80
  - p) 3 out of 5
  - q) 4 out of 5
  - r) 15 out of 75
  - s) 24 out of 75
  - t) 30 out of 75

- 5) A shop gives a discount of 20% on a magazine that usually sells for £2.80. Work out the discount in pence.



- 6) A television costs £596 plus VAT at 17.5%.  
Work out the cost of the television including VAT.



- 7) Peter has 128 trees in his garden.  
16 of the trees are pear trees.  
What percentage of the trees in his garden are pear trees?



- 8) Jane scored 27 out of 42 in a Maths test and 39 out of 61 in a Science test.  
What were her percentages in both subjects to 1 decimal place?

- 9) In class 9A there are 7 girls and 18 boys.  
What percentage of the class are girls?

- 10) A shop decides to reduce all the prices by 15%.  
The original price of a pair of trainers was £70. How much are they after the reduction?



- 11) VAT at 17.5% is added to the price of a car. Before the VAT is added it cost £18000.  
How much does it cost with the VAT?

## Rounding to Significant Figures

1) Round the following numbers to 1 significant figure:

- a) 428
- b) 783
- c) 5608
- d) 3 521
- e) 21 999
- f) 793 041

2) Round the following numbers to 2 significant figures:

- a) 846
- b) 2 647
- c) 3 552
- d) 46 817
- e) 89 711
- f) 195 084

3) Round the following numbers to 3 significant figures:

- a) 91 249
- b) 64 182
- c) 223 058
- d) 389 512
- e) 7 761 223
- f) 4 997 124



4) Work out the following and give your answer to 3 significant figures:

- a)  $216 \times 348$
- b)  $7721 \times 609$
- c)  $8714 \times 2198$

5) Round the following numbers to 1 significant figure:

- a) 0.00618
- b) 0.00482
- c) 0.00006492
- d) 0.004981

6) Round the following numbers to 2 significant figures:

- a) 0.035812
- b) 0.00082477
- c) 0.0038611
- d) 0.000037211

7) Round the following numbers to 3 significant figures:

- a) 0.00143229
- b) 0.000721981
- c) 0.0000044251
- d) 0.000668821

8) Round the following numbers to 3 significant figures:

- a) 47.84122
- b) 9.778112
- c) 12.35913



9) Work out the following and give your answer to 3 significant figures:

- a)  $15 \div 0.38$
- b)  $0.31 \div 0.16$
- c)  $208 \times 366$

1) Work out an estimate for  $\frac{304 \times 9.96}{0.51}$

2) Work out an estimate for  $\frac{6.7 \times 192}{0.051}$

3) Work out an estimate for  $\frac{32 \times 4.92}{0.21}$

4) Work out an estimate for  $\frac{3880}{236 \times 4.85}$

5) Work out an estimate for  $\frac{7.18 \times 19.7}{0.47}$

## Exchanging Money



- 1) Lance goes on holiday to France.  
The exchange rate is  $\text{£}1 = 1.15$  Euros.

He changes  $\text{£}350$  into Euros.

- a) How many Euros should he get?

In France, Lance buys a digital camera for 115 Euros.

- b) Work out the cost of the camera in pounds.



- 2) Whilst on holiday in Spain, Gemma bought a pair of sunglasses for 77 Euros.  
In England, an identical pair of sunglasses costs  $\text{£}59.99$ .

The exchange rate is  $\text{£}1 = 1.40$  Euros.

In which country were the glasses the cheapest, and by how much?

*Show all your working.*



- 3) Luke buys a pair of trainers in Switzerland.  
He can pay either 86 Swiss Francs or 56 Euros.

The exchange rates are:

$\text{£}1 = 2.10$  Swiss Francs

$\text{£}1 = 1.40$  Euros

Which currency should he choose to get the best price, and how much would he save?

*Give your answer in pounds (£).*



- 4) The exchange rate in London is  $\text{£}1 = \text{€}1.14$   
The exchange rate in Paris is  $\text{€}1 = \text{£}0.86$

Tony wants to change some pounds into euros.

In which of these cities would Tony get the most euros?

*All working must be shown.*



1) Expand these brackets

a)  $2(x + 3)$

b)  $3(2x + 4)$

c)  $5(3p - 2q)$

d)  $4(x^2 + 2y^2)$

e)  $6(r - r^2)$

2) Expand these brackets

a)  $x(x - 2)$

b)  $x(3x + 5)$

c)  $p(3p - 7q)$

d)  $y(y + 6y^2)$

e)  $x(r + r^2)$

3) Expand these brackets

a)  $2x(x - 5)$

b)  $4x(2x + 3)$

c)  $5p(4p - 2q)$

d)  $2y(3y + 4x^2)$

e)  $x(x + r^2)$

4) Expand these brackets

a)  $x(x^2 - 2)$

b)  $3x(2x^3 + 1)$

c)  $5p^2(4p - 2)$

d)  $2y^2(3y^3 + 4y)$

e)  $2xy(x + y^2)$

1) Factorise

a)  $2x + 4$

b)  $2y + 10$

c)  $3x + 12$

d)  $3x - 6$

e)  $5x - 15$

2) Factorise

a)  $p^2 + 7p$

b)  $x^2 + 4x$

c)  $y^2 - 2y$

d)  $p^2 - 5p$

e)  $x^2 + x$

3) Factorise

a)  $2x^2 + 6x$

b)  $2y^2 - 8y$

c)  $5p^2 + 10p$

d)  $7c^2 - 21c$

e)  $6x^2 + 9x$

4) Factorise

a)  $2x^2 - 4xy$

b)  $2t^2 + 10tu$

c)  $6x^2 - 8xy$

d)  $3x^2y^2 + 9xy$

## Substitution

1)  $y = 5x$

- a) Work out the value of  $y$  when  $x = 3$   
b) Work out the value of  $y$  when  $x = -2$

2)  $y = 2x + 7$

- a) Work out the value of  $y$  when  $x = 4$   
b) Work out the value of  $y$  when  $x = -3$

3)  $y = 2x + 4t$

$x = 6$

$t = 1$

Work out the value of  $y$ .

4)  $y = 2a - 3b$

$a = 4$

$b = -2$

Work out the value of  $y$ .

5)  $v = 3a + 5b$

$a = 6$

$b = -3$

Work out the value of  $v$ .

6)  $y = x^2$

- a) Work out the value of  $y$  when  $x = 6$   
b) Work out the value of  $y$  when  $x = -4$

7)  $y = 2x^2$

- a) Work out the value of  $y$  when  $x = 5$   
b) Work out the value of  $y$  when  $x = -3$

8)  $y = 3x^2 + 2x$

- a) Work out the value of  $y$  when  $x = 2$   
b) Work out the value of  $y$  when  $x = -4$



9)  $v = u^2 + 5as$

$u = 6$

$a = 2.5$

$s = 9$

Work out the value of  $v$ .



10)  $y = p - 2qx^2$

$p = -10$

$q = 2$

$x = -5$

Work out the value of  $y$ .



11)  $v^2 = u^2 + 2as$

$u = 6$

$a = 2.5$

$s = 9$

Work out the value of  $v$ .



12)  $v^2 = u^2 + 2as$

$u = 3$

$a = 9.8$

$s = 12$

Work out the value of  $v$ .

Give your answer correct to 1 decimal place



13)  $s = ut + 0.5at^2$

$a = 9.8$

$t = 5$

$u = 7$

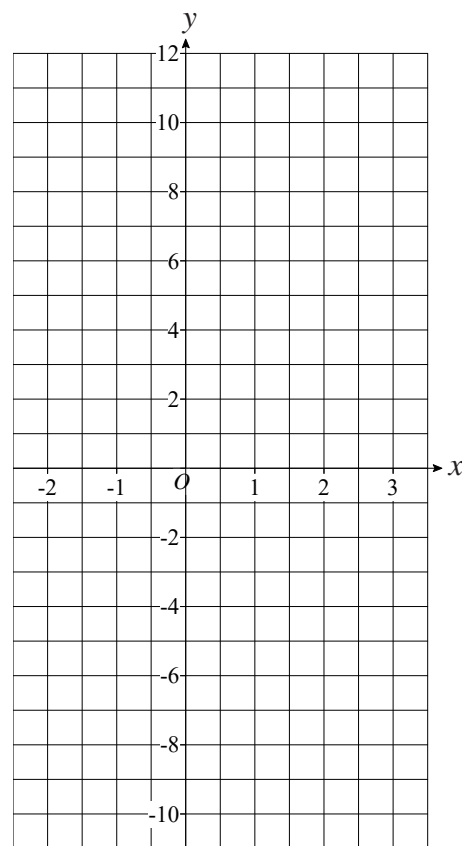
Work out the value of  $s$ .

# Straight Line Graphs

- 1) a) Complete the table of values for  $y = 4x - 2$

$x$	-2	-1	0	1	2	3
$y$	-10		-2			10

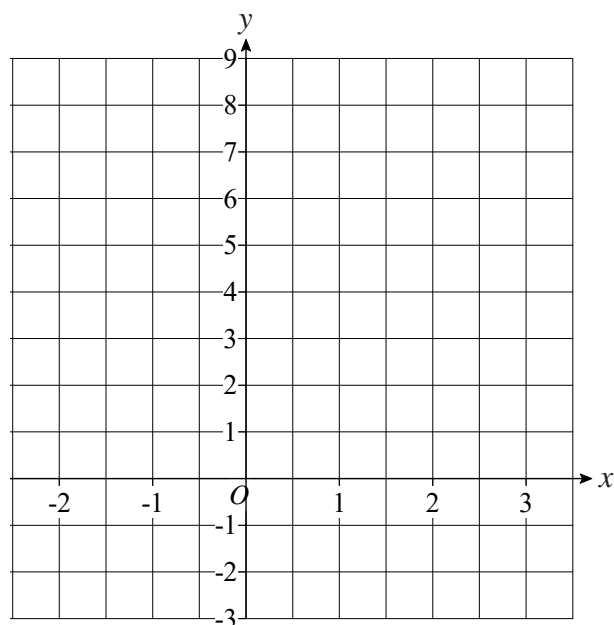
- b) On the grid, draw the graph of  $y = 4x - 2$ , for values of  $x$  from -2 to 3.  
c) Use the graph to find the value of  $y$  when  $x = 2.5$   
d) Use the graph to find the value of  $x$  when  $y = -8$



- 2) a) Complete the table of values for  $y = 2x + 2$

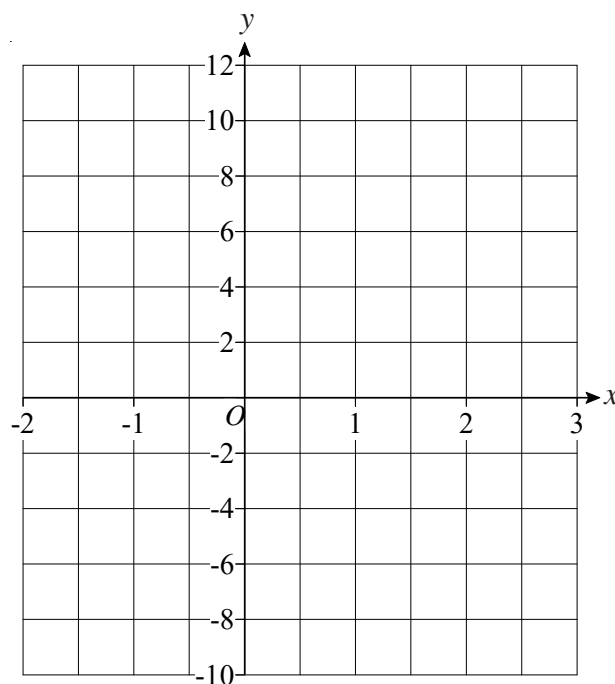
$x$	-2	-1	0	1	2	3
$y$		0	2			

- b) On the grid, draw the graph of  $y = 2x + 2$ .



# Straight Line Graphs

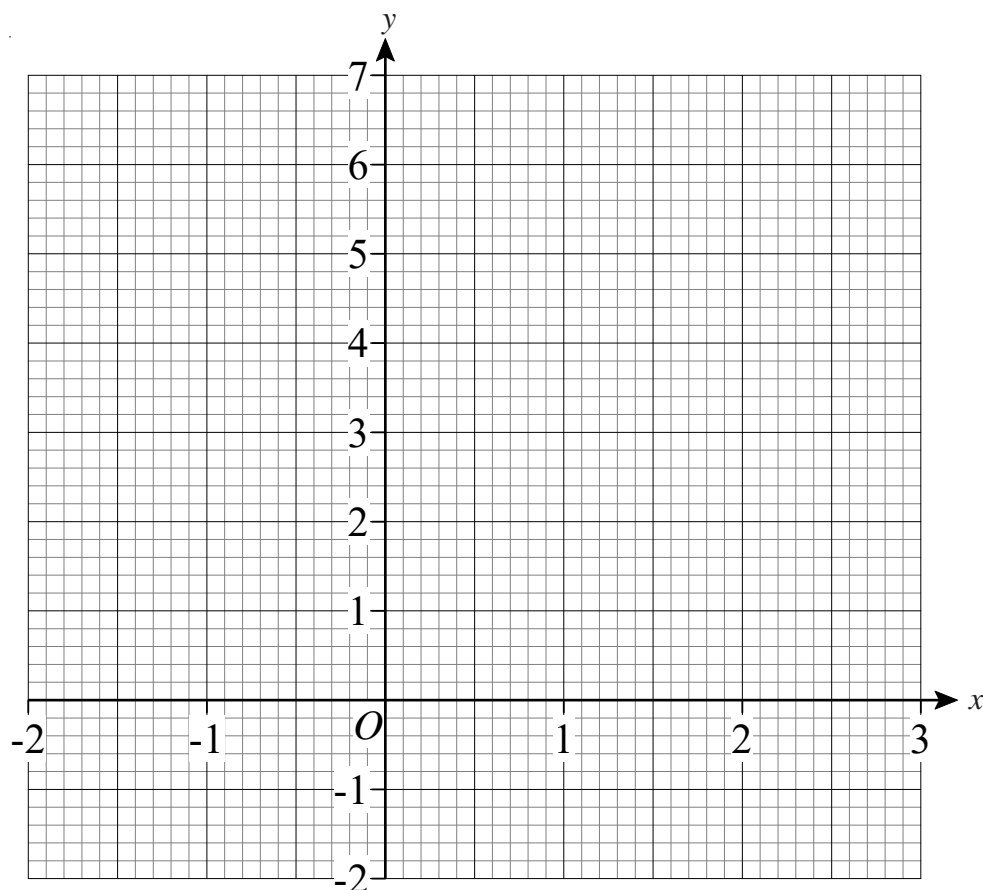
- 1) On the grid, draw the graph of  $y = 2x - 4$



- 2) a) Complete the table of values for  $3x + 2y = 6$

$x$	-2	-1	0	1	2	3
$y$		4.5	3			-1.5

- b) On the grid, draw the graph of  $3x + 2y = 6$



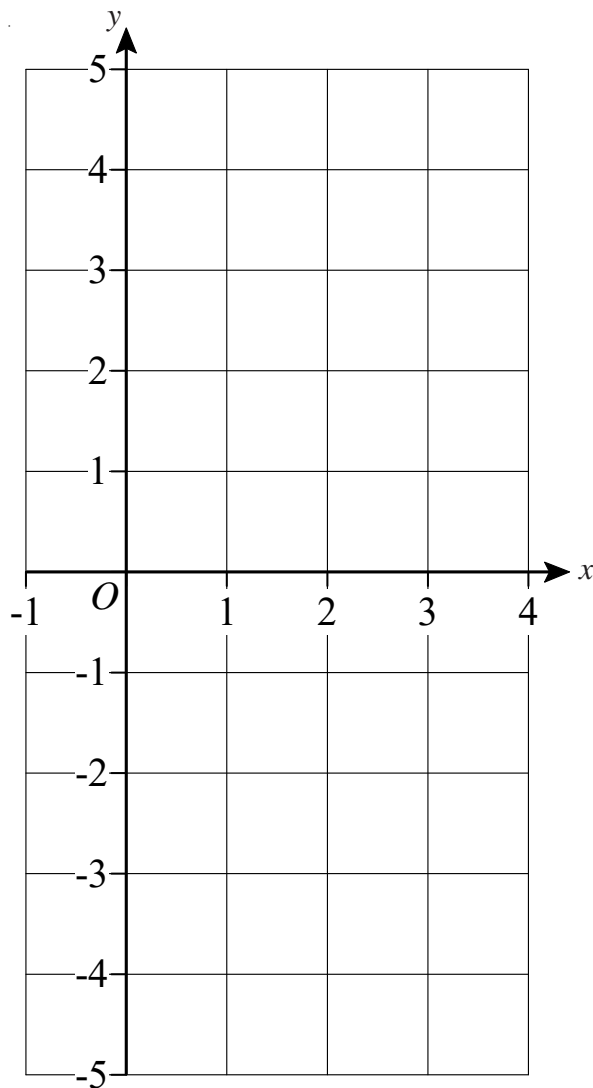
- c) Find the gradient of the graph of  $3x + 2y = 6$ .

## Straight Line Graphs

- 1) a) Complete the table of values for  $y = 2x - 3$

$x$	-1	0	1	2	3	4
$y$				1		

- b) Using the axes on the right draw the graph of  $y = 2x - 3$
- c) Use your graph to work out the value of  $y$  when  $x = 2.5$
- d) Use your graph to work out the value of  $x$  when  $y = 4.5$



- 2) a) Complete the table of values for  $y = 2 - x$

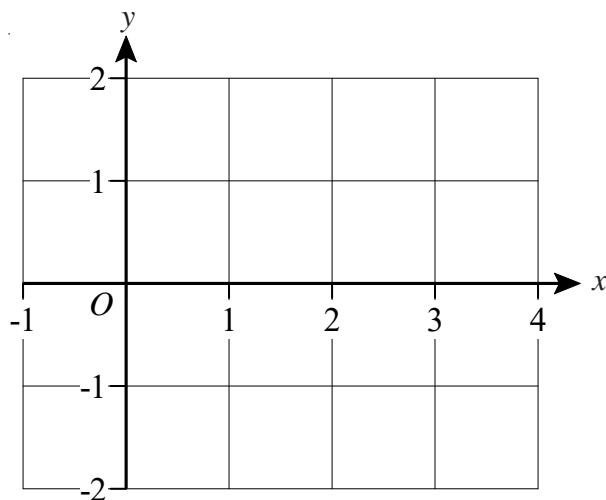
$x$	-1	0	1	2	3	4
$y$					-1	

- b) Using the axes on the right, again, draw the graph of  $y = 2 - x$

- 3) a) Complete the table of values for  $y = \frac{1}{2}x - 1$

- b) Draw the graph of  $y = \frac{1}{2}x - 1$

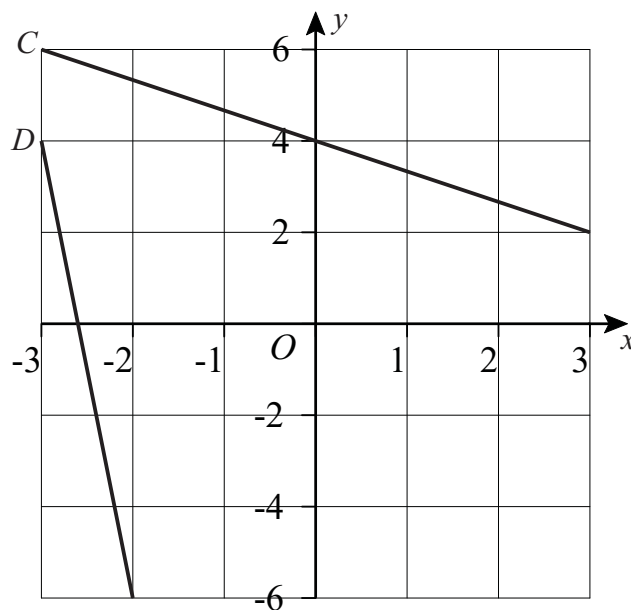
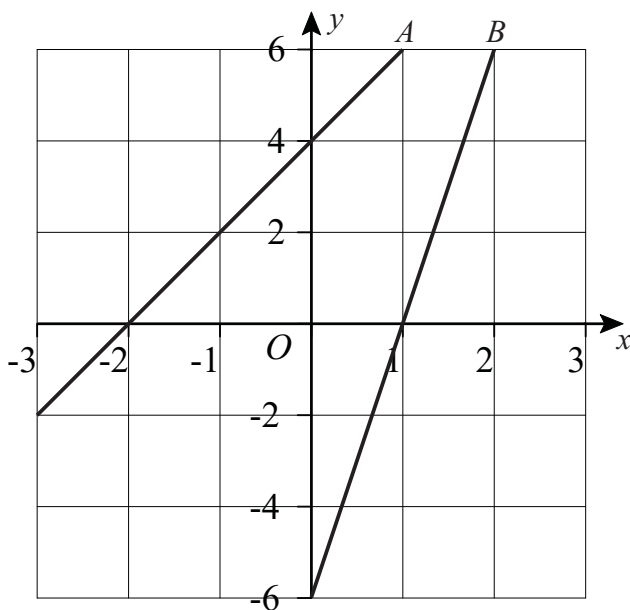
$x$	-1	0	1	2	3	4
$y$				0		



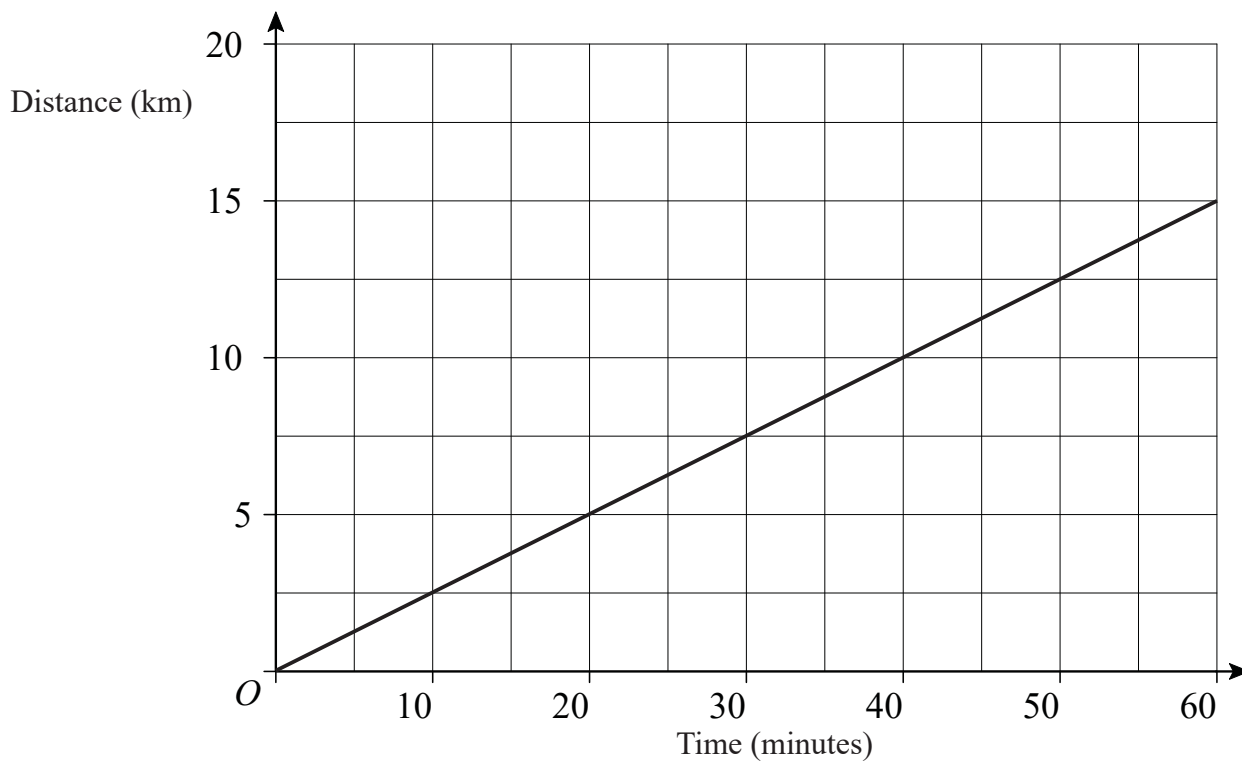
- c) Use your graph to find the value of  $y$  when  $x = 3.5$

## The Gradient of a Line

- 1) Find the gradient of lines  $A$ ,  $B$ ,  $C$  and  $D$ .



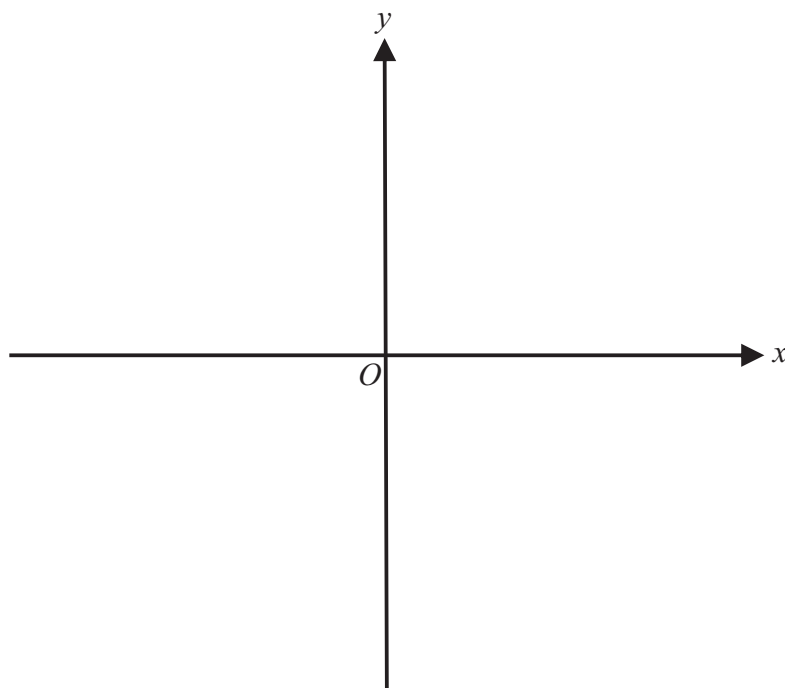
- 2) The graph shows how Meg cycles at a constant speed for 60 minutes.



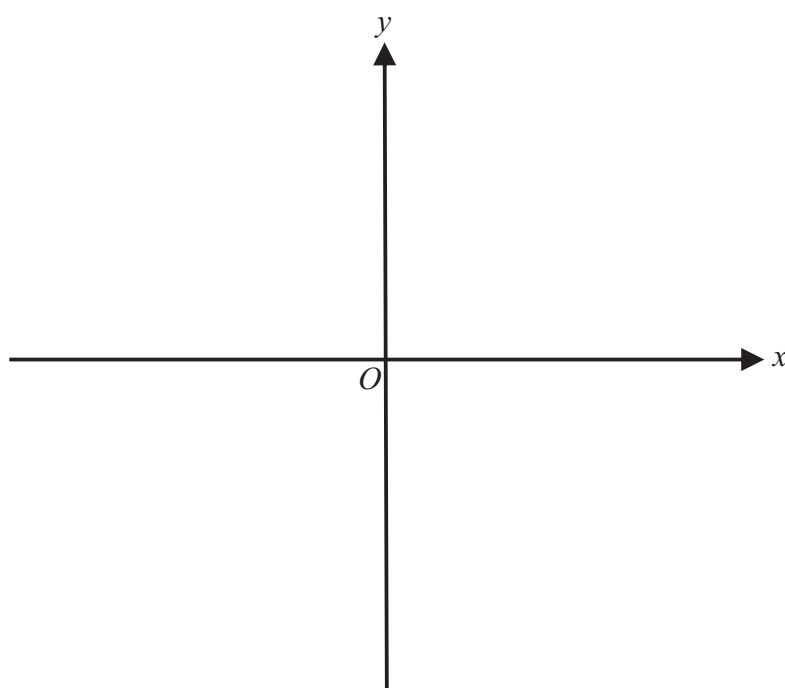
- Find the gradient of the line.
- What does the gradient show?

## Sketching Functions

- 1) a) Sketch the graph of  $y = 3x - 4$  on the axes, showing clearly where it crosses the  $y$ -axis.  
b) Sketch the graph of  $y = -2x + 3$  on the axes, showing clearly where it crosses the  $y$ -axis.



- 2) a) Sketch the graph of  $y = x^2 + 2$  on the axes, showing clearly where it crosses the  $y$ -axis.  
b) Sketch the graph of  $y = -x^2 - 1$  on the axes, showing clearly where it crosses the  $y$ -axis.





## Solving Equations - Introduction

1) Solve

- a)  $x + 3 = 8$
- b)  $x + 1 = 13$
- c)  $x - 4 = 10$
- d)  $x - 8 = 9$
- e)  $x + 7 = 21$
- f)  $x - 6 = 33$
- g)  $16 = x + 2$
- h)  $11 = x - 7$
- i)  $14 = 3 + x$
- j)  $5 = x - 12$

2) Solve

- a)  $x + 2 = 9$
- b)  $x + 1 = 16$
- c)  $x - 3 = 14$
- d)  $x - 8 = 7$
- e)  $x + 5 = 29$
- f)  $x - 8 = 35$
- g)  $21 = x + 3$
- h)  $18 = x - 6$
- i)  $15 = 7 + x$
- j)  $9 = x - 13$

3) Solve

- a)  $2x = 8$
- b)  $5x = 30$
- c)  $40 = 4x$
- d)  $24 = 8x$
- e)  $\frac{x}{4} = 7$
- f)  $\frac{x}{2} = 9$
- g)  $3 = \frac{x}{5}$
- h)  $6 = \frac{x}{6}$
- i)  $2x = 68$
- j)  $\frac{x}{8} = 7$

4) Solve

- a)  $2x = 6$
- b)  $6x = 30$
- c)  $50 = 2x$
- d)  $24 = 6x$
- e)  $\frac{x}{4} = 8$
- f)  $\frac{x}{2} = 10$
- g)  $7 = \frac{x}{5}$
- h)  $9 = \frac{x}{6}$
- i)  $2x = 82$
- j)  $\frac{x}{8} = 11$

5) Solve

- a)  $y + 12 = 20$
- b)  $\frac{d}{3} = 9$
- c)  $m - 10 = 13$
- d)  $7k = 35$
- e)  $11 + c = 24$
- f)  $60 = 10p$
- g)  $8 = r - 19$
- h)  $7 = \frac{c}{11}$
- i)  $72 = 9q$
- j)  $37 = 26 + x$

6) Solve

- a)  $y + 14 = 26$
- b)  $\frac{d}{3} = 12$
- c)  $m - 10 = 17$
- d)  $9k = 63$
- e)  $15 + c = 29$
- f)  $40 = 10p$
- g)  $9 = r - 17$
- h)  $6 = \frac{c}{11}$
- i)  $54 = 6q$
- j)  $34 = 27 + x$

1) Solve the following equations.

a)  $2x - 7 = 11$

b)  $5x + 3 = 43$

2) Solve the following equations.

a)  $\frac{x}{5} + 1 = 7$

b)  $\frac{x}{2} - 6 = 2.5$

3) Solve the following equations.

a)  $2(4x - 1) = 46$

b)  $6(2x + 7) = 48$

4) Solve the following equations.

a)  $3\left(\frac{x}{7} + 2\right) = 6$

b)  $2\left(\frac{5x}{3} - 1\right) = 8$

1) Make the variable shown in brackets the subject of the formula in each case.

a)  $x = y + 7$  ( $y$ )

b)  $y = x - 2$  ( $x$ )

c)  $p = q + 12$  ( $q$ )

d)  $q = p - 25$  ( $p$ )

e)  $u = 8 + v$  ( $v$ )

f)  $v = u - 1$  ( $u$ )

g)  $a + 4 = b$  ( $a$ )

h)  $b - 6 = a$  ( $b$ )

i)  $9 + c = d$  ( $c$ )

j)  $d + 10 = c$  ( $d$ )

3) Make the variable shown in brackets the subject of the formula in each case.

a)  $5y = x$  ( $y$ )

b)  $p = 3q$  ( $q$ )

c)  $11u = v$  ( $u$ )

d)  $a = 15b$  ( $b$ )

e)  $\frac{x}{2} = y$  ( $x$ )

f)  $\frac{p}{10} = q$  ( $p$ )

g)  $u = \frac{v}{6}$  ( $v$ )

h)  $b = \frac{a}{7}$  ( $a$ )

i)  $c = 4d$  ( $d$ )

j)  $\frac{c}{8} = d$  ( $c$ )

5) Make the variable shown in brackets the subject of the formula in each case.

a)  $p - 7 = q$  ( $p$ )

b)  $\frac{v}{9} = u$  ( $v$ )

c)  $y = 3 + x$  ( $x$ )

d)  $c = d - 14$  ( $d$ )

e)  $m = 2n$  ( $n$ )

f)  $a + 1 = b$  ( $a$ )

g)  $6q = r$  ( $q$ )

h)  $x = \frac{y}{3}$  ( $y$ )

i)  $8 + c = d$  ( $c$ )

j)  $\frac{b}{10} = a$  ( $b$ )

- 1) Make  $x$  the subject of the formula  $w = 5x + 2$
  
- 2) Make  $x$  the subject of the formula  $y = 2x - 6$
  
- 3) Make  $x$  the subject of the formula  $2w = 3y + \frac{x}{5}$
  
- 4) Make  $t$  the subject of the formula  $a = 2(b + 3t) + 1$
  
- 5) Make  $x$  the subject of the formula  $y = 5 + \sqrt{x}$
  
- 6) Make  $t$  the subject of the formula  $w = x^2 + t$
  
- 7) Make  $n$  the subject of the formula  $m = 3n^2 - p$
  
- 8) Make  $q$  the subject of the formula  $2(5q^2 + 1) = c$

## Generate a Sequence from the $n$ th Term

- 1) The  $n$ th term of a number sequence is  $2n + 5$

Write down the first three terms of the sequence.

- 2) The  $n$ th term of a number sequence is  $3n - 1$

Write down the first four terms of the sequence.

- 3) The  $n$ th term of a number sequence is  $3n + 2$

Write down the first four terms of the sequence.

- 4) The  $n$ th term of a number sequence is  $5n - 7$

Write down the first four terms of the sequence.

- 5) The  $n$ th term of a number sequence is  $n^2$

Write down the first three terms of the sequence.

- 6) The  $n$ th term of a number sequence is  $n^2 + 3$

Write down the first three terms of the sequence.

- 7) The  $n$ th term of a number sequence is  $11 - n^2$

a) Find the third term of this sequence.

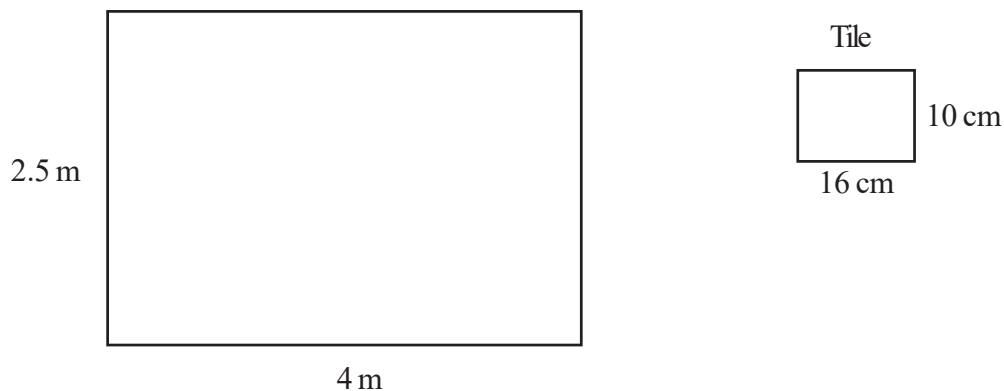
b) Find the fifth term of this sequence.

- 8) The  $n$ th term of a number sequence is  $n^2 + n$

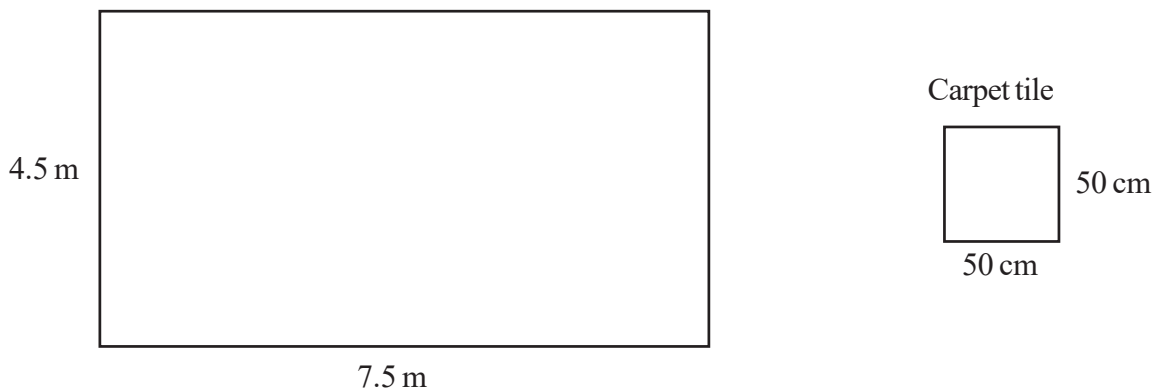
a) Find the third term of this sequence.

b) Find the fifth term of this sequence.

- 1) Change  $9 \text{ m}^2$  into  $\text{cm}^2$
- 2) How many square metres are there in 5 square kilometres?
- 3) Change  $4 \text{ cm}^2$  into  $\text{mm}^2$
- 4) Convert  $6.5 \text{ m}^2$  into  $\text{mm}^2$
- 5) Change  $2 \text{ m}^3$  into  $\text{cm}^3$
- 6) How many cubic millimetres are there in 3 cubic centimetres?
- 7) Change  $7 \text{ m}^3$  into  $\text{mm}^3$
- 8) A tiler wants to tile a rectangular wall which measures 4 m by 2.5 m.  
Each tile measures 16 cm by 10 cm.  
How many tiles will he need for the wall?

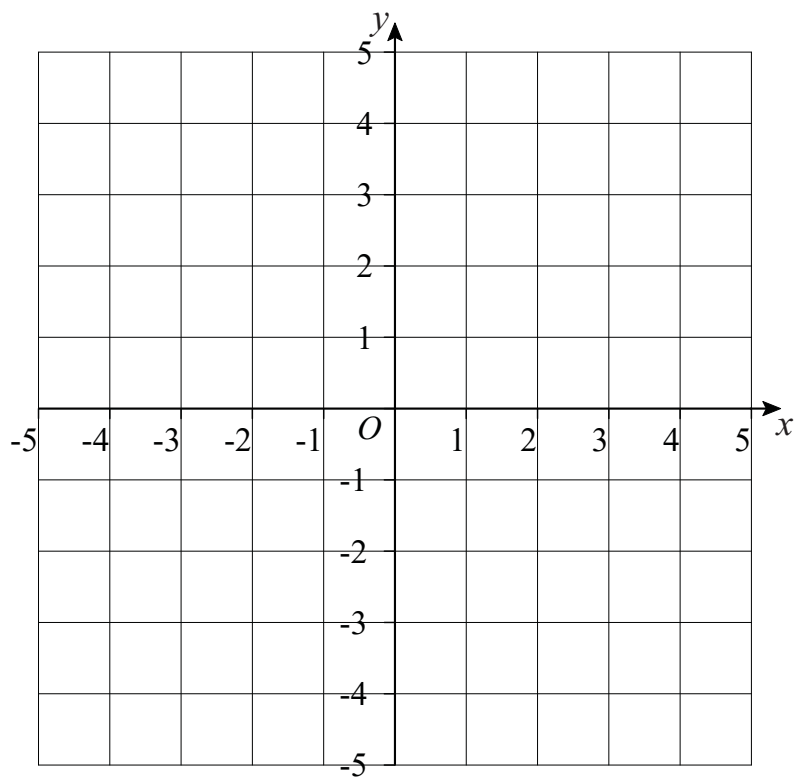


- 9) A carpet-fitter is laying carpet tiles on a rectangular floor which measures 7.5 m by 4.5 m.  
Each carpet tile measures 50 cm by 50 cm.  
How many carpet tiles will he need for the floor?



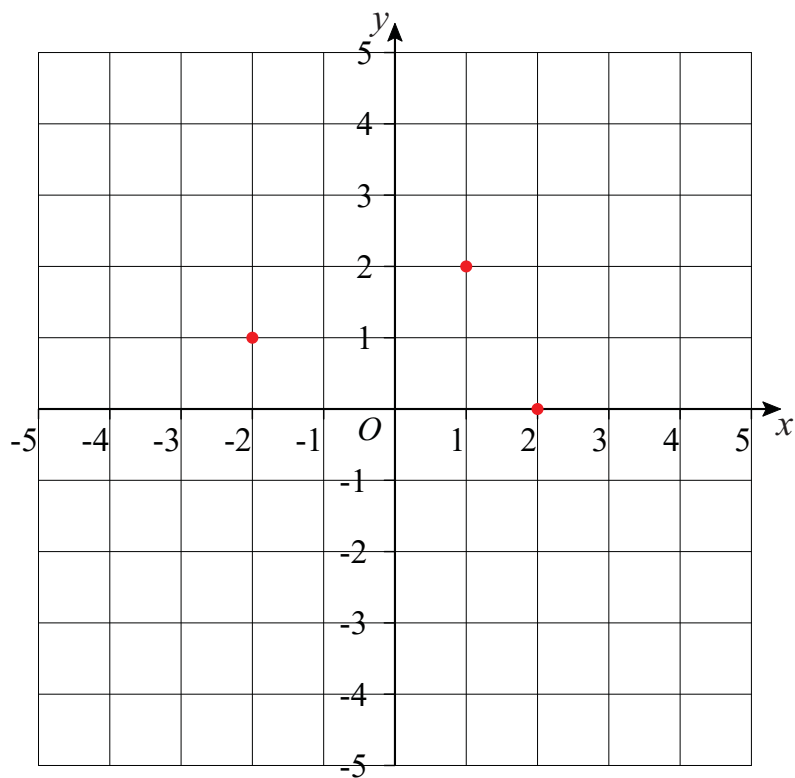
- 1) The points  $A(3, 0)$ ,  $B(2, 4)$  and  $C(-3, 1)$  are three corners of a parallelogram.

What are the coordinates of the 4th corner?

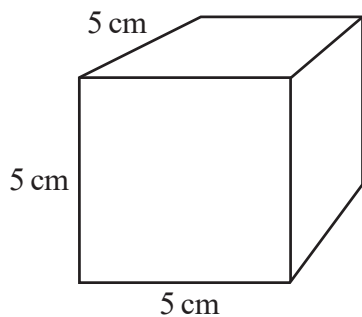


- 2) The diagram shows 3 vertices of a parallelogram.

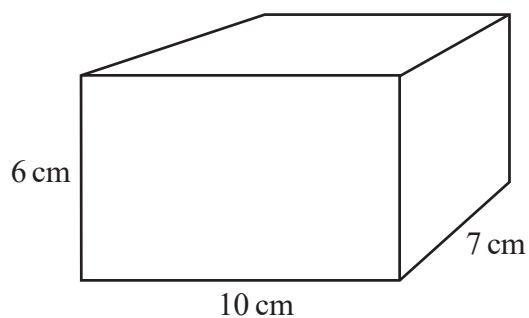
Write down the coordinates of all the possibilities for the 4th vertex.



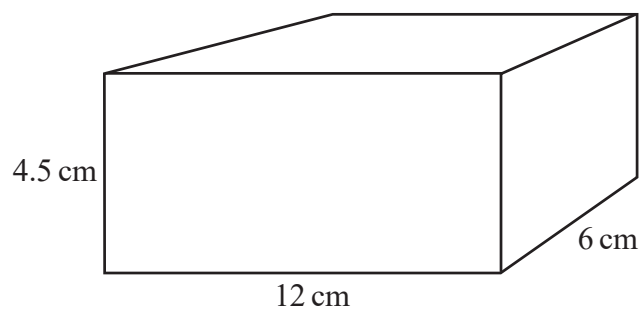
- 1) A cube has sides of length 5 cm.  
Find the total surface area of the cube.



- 2) A cuboid has sides of length 10 cm, 6cm and 7 cm.  
Find the total surface area of the cuboid.



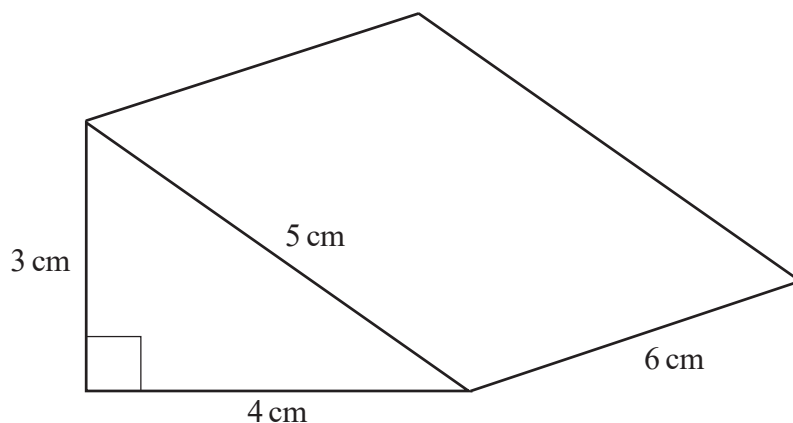
- 3) A cuboid has sides of length 12 cm, 4.5cm and 6 cm.  
Find the total surface area of the cuboid.



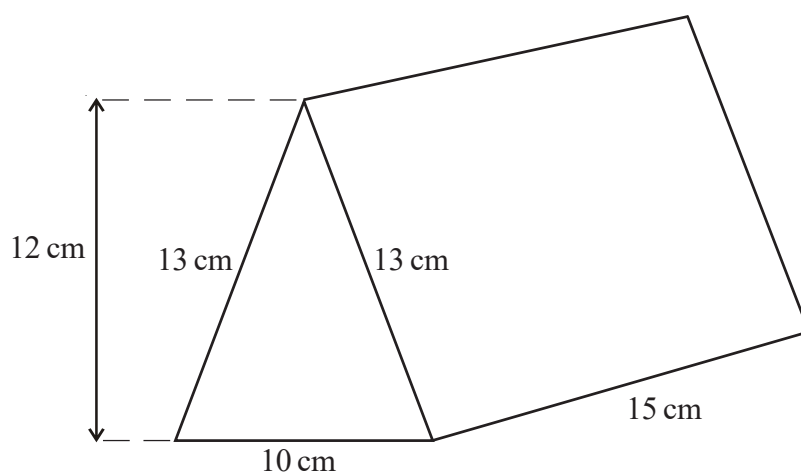


# Surface Area of a Prism - Triangular Prisms

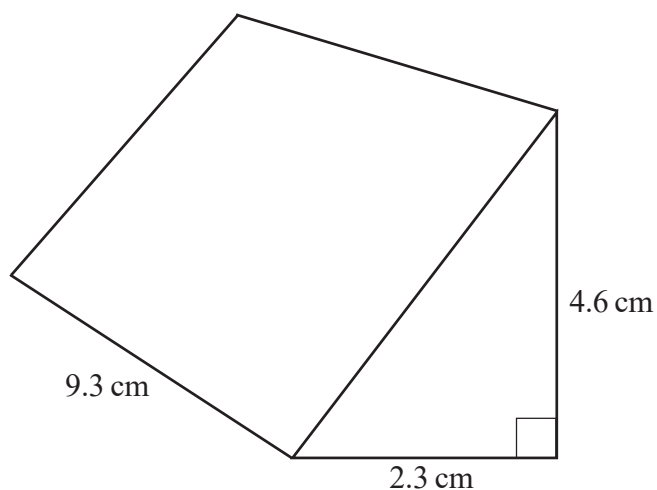
- 1) Find the surface area of this triangular prism.



- 2) Find the surface area of this triangular prism.

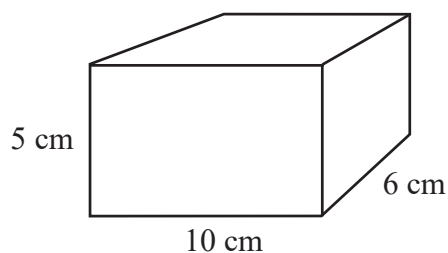


- 3) With the aid of Pythagoras' Theorem, find the surface area of this triangular prism.  
Give your answer correct to 2 significant figures.

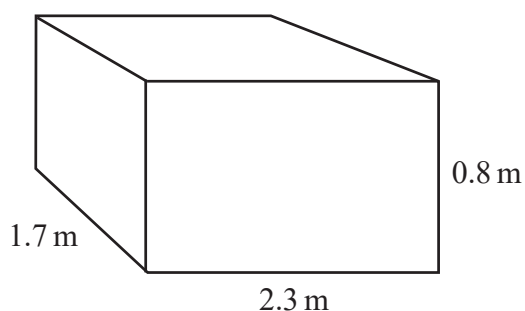


## Volume of a Cuboid

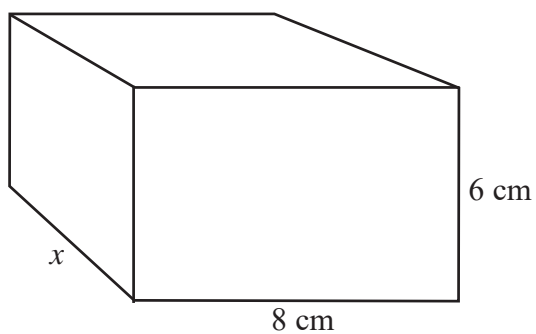
- 1) Find the volume of this cuboid.



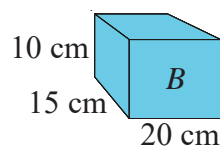
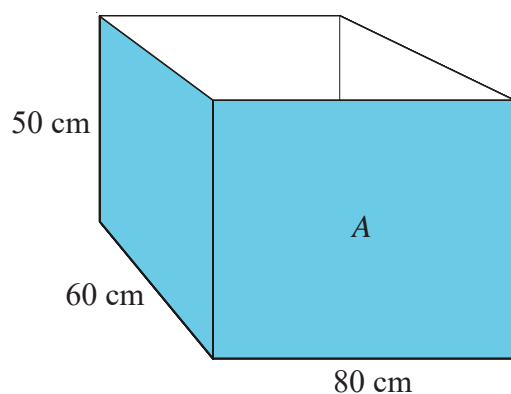
- 2) Find the volume of this cuboid.



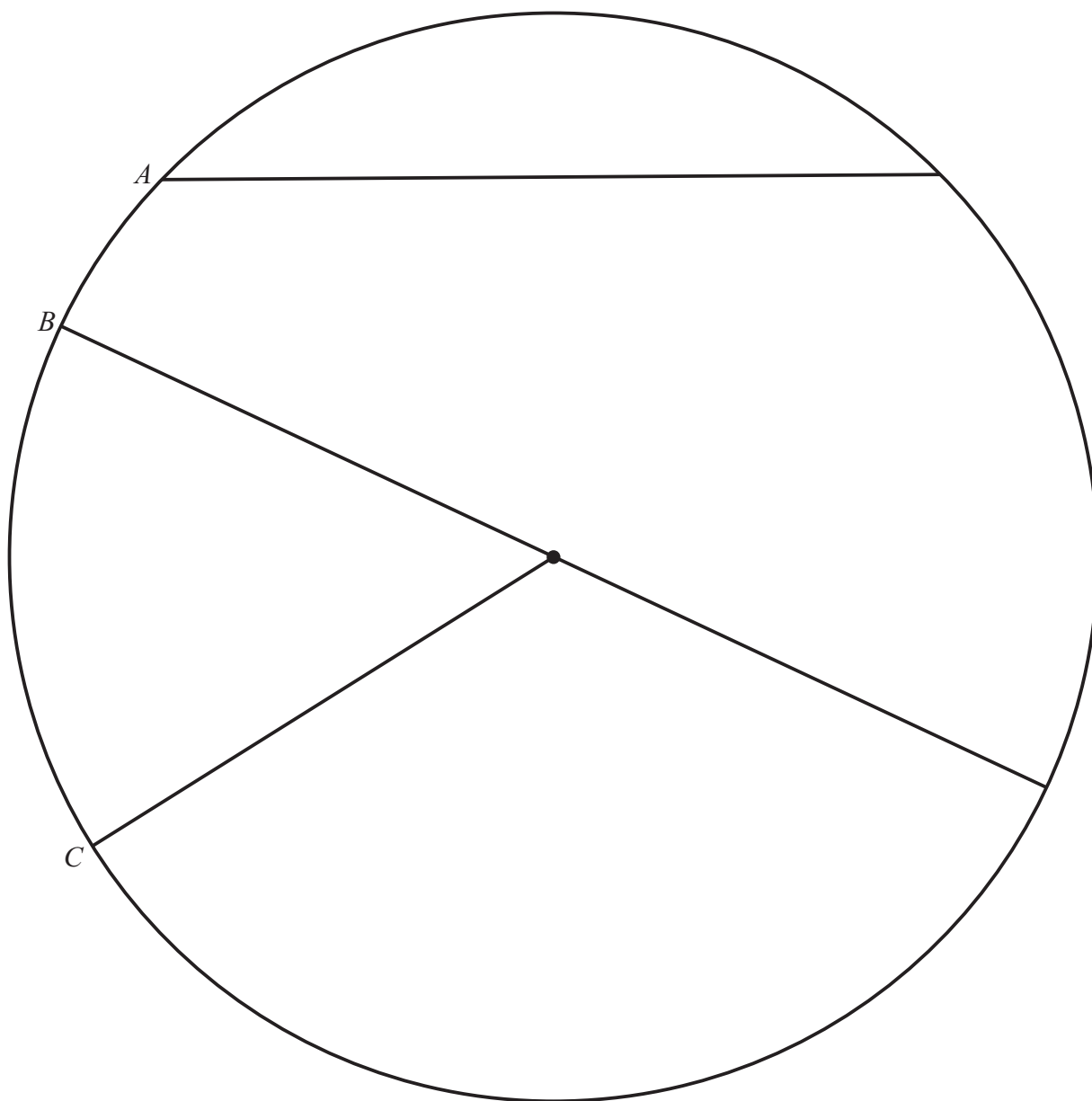
- 3) The volume of this cuboid is  $480 \text{ cm}^3$ .  
Find the length of the side marked  $x$ .



- 4) Boxes  $A$  and  $B$  are both cuboids.  
How many of box  $B$  could be packed into box  $A$ ?

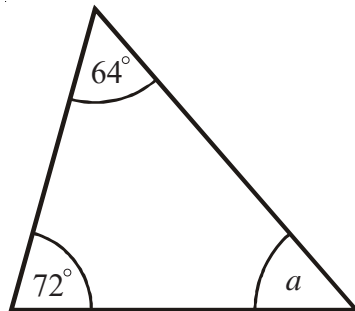


- 1) In the circle, write the correct names for line  $A$ ,  $B$  and  $C$ .

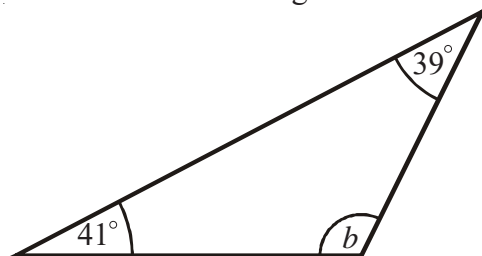


- 2) What is the special name given to the perimeter of a circle?

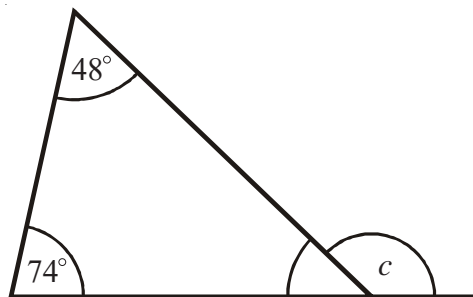
- 1) Work out the size of angle  $a$ .



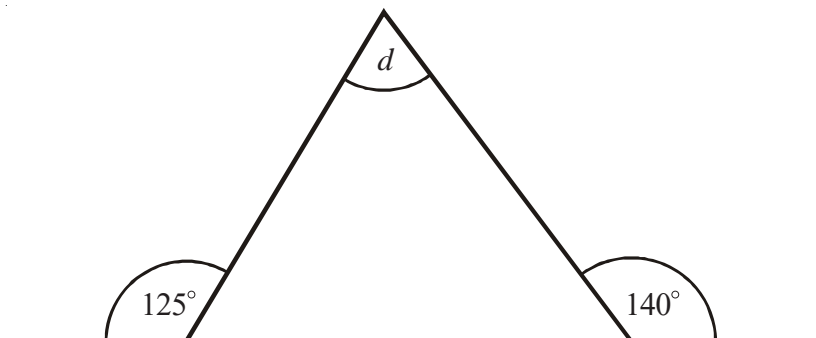
- 2) Work out the size of angle  $b$ .



- 3) Work out the size of angle  $c$ .



- 4) Work out the size of angle  $d$ .



## Properties of Special Triangles

- 1)  $ABC$  is a triangle.

a) Find the size of angle  $A$ .

- b) Triangle  $ABC$  is equilateral.

Explain why.

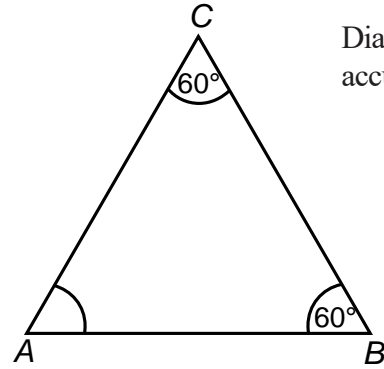


Diagram **NOT** accurately drawn

- 2)  $BCD$  is a triangle.

$ABC$  is a straight line.

Angle  $CBD = 70^\circ$ .

$BD = CD$ .

- a) (i) Work out the value of  $x$ .

(ii) Give a reason for your answer.

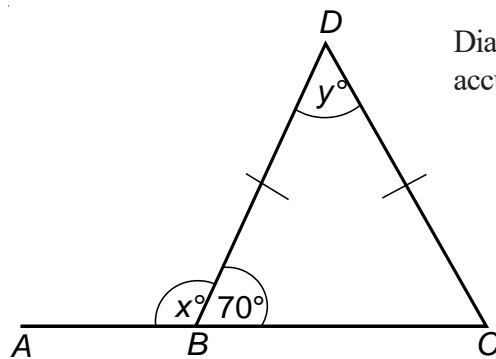


Diagram **NOT** accurately drawn

- b) (i) Work out the value of  $y$ .

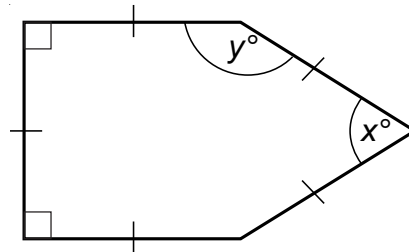
(ii) Give reasons for your answer.

- 3) The diagram shows a 5-sided shape.

All the sides of the shape are equal in length.

- a) (i) Find the value of  $x$ .

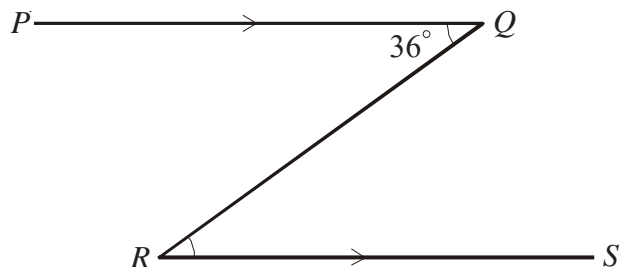
(ii) Give a reason for your answer.



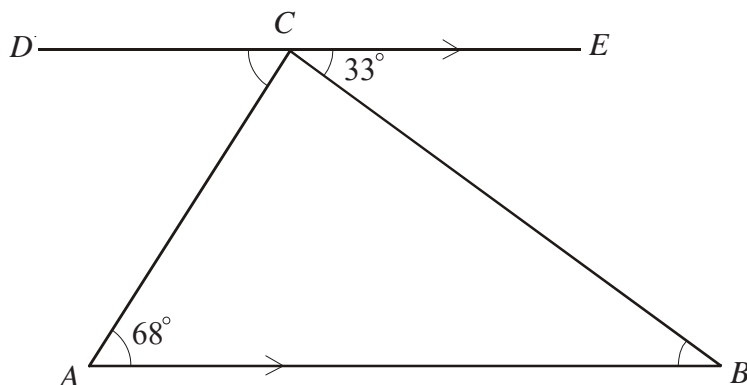
- b) (i) Work out the value of  $y$ .

(ii) Explain your answer.

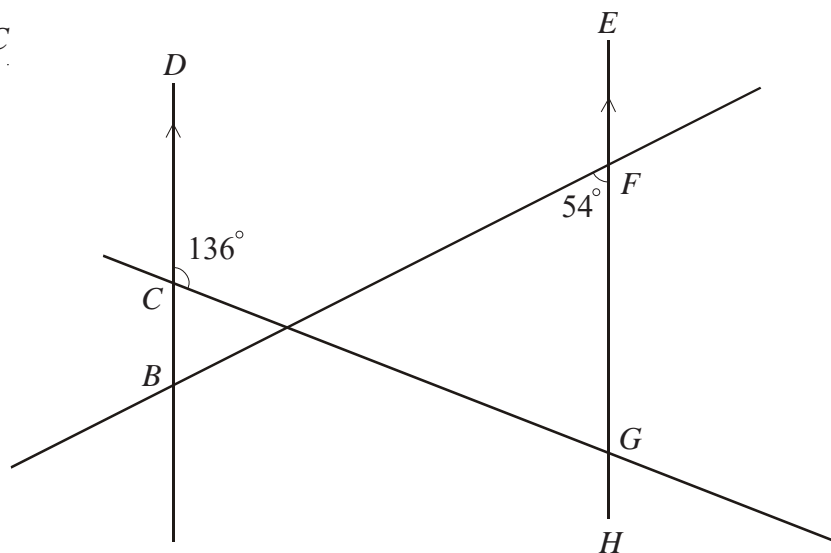
- 1) Line  $PQ$  is parallel to line  $RS$ .  
 If angle  $PQR$  is equal to  $36^\circ$   
 a) What is the size of angle  $QRS$ ?  
 b) Give a reason for your answer.



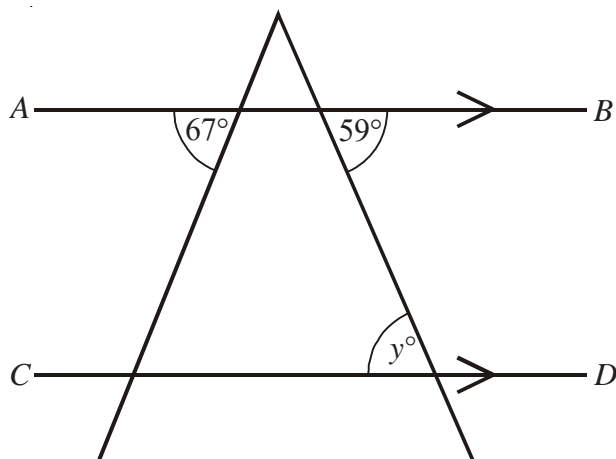
- 2) Line  $DCE$  is parallel to line  $AB$   
 a) Find the size of angle  $ABC$   
 b) Find the size of angle  $DCA$   
 c) Calculate the size of angle  $ACB$



- 3) a) Find the size of angle  $DBF$   
 b) Find the size of angle  $HGC$



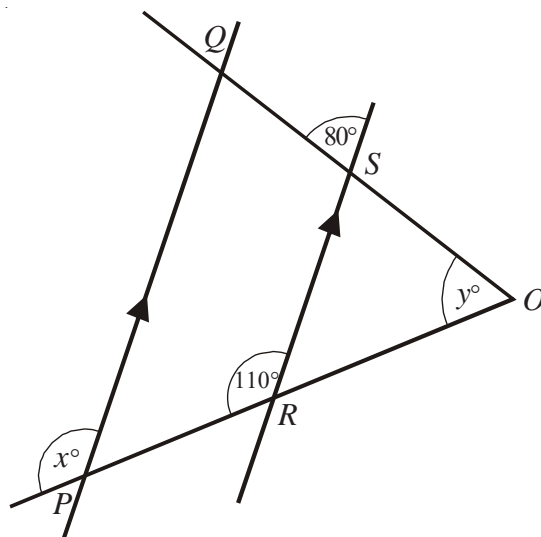
1)



$AB$  is parallel to  $CD$ .

- Write down the value of  $y$ .
- Give a reason for your answer.

2)



$PQ$  is parallel to  $RS$ .

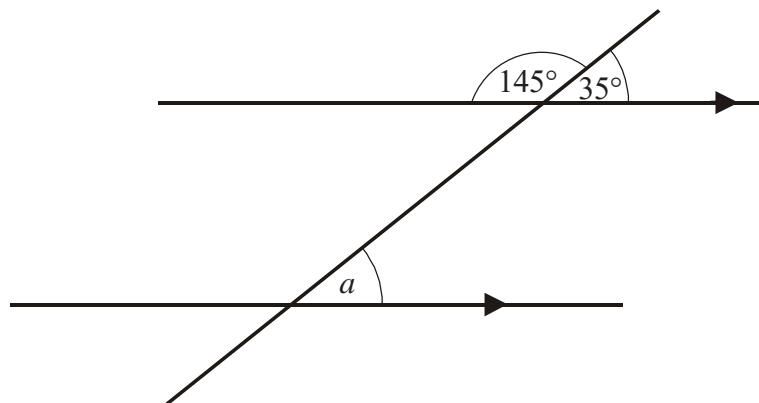
$OSQ$  and  $ORP$  are straight lines.

- Write down the value of  $x$ .
  - Give a reason for your answer.

- Work out the value of  $y$ .

# Angles and Parallel Lines

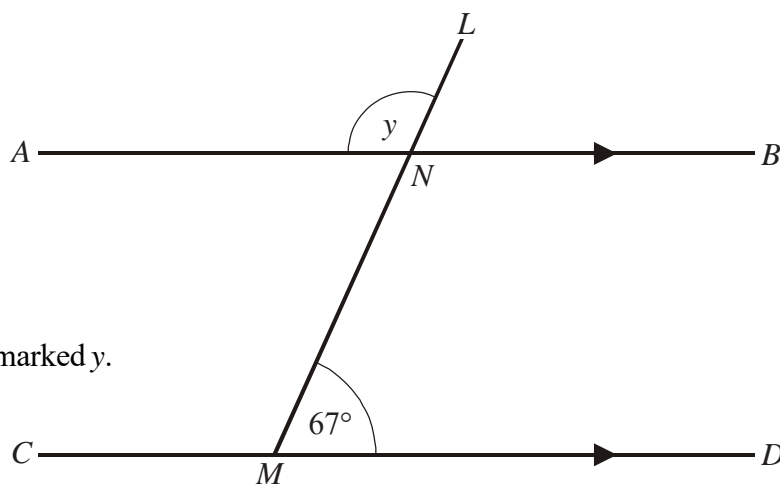
1)



(i) Write down the size of the angle marked  $a$ .

(ii) Give a reason for your answer.

2)



$ANB$  is parallel to  $CMD$ .

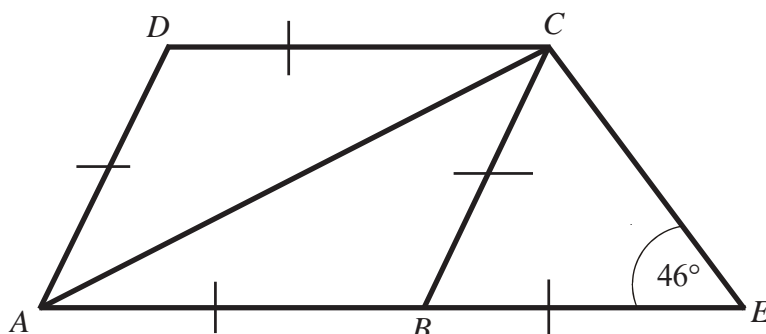
$LNM$  is a straight line.

Angle  $LMD = 67^\circ$

(i) Work out the size of the angle marked  $y$ .

(ii) Give reasons for your answer.

3)



$ABCD$  is a rhombus.

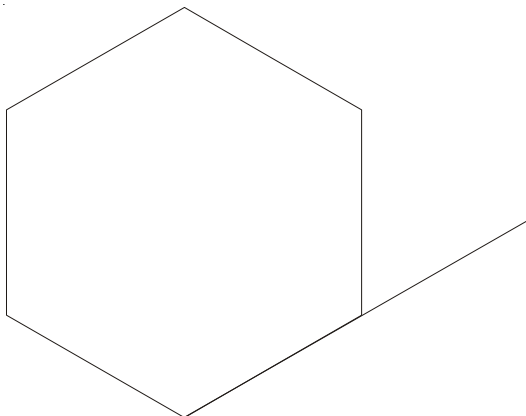
$BCE$  is an isosceles triangle.

$ABE$  is a straight line.

Work out the size of angle  $DCA$ .

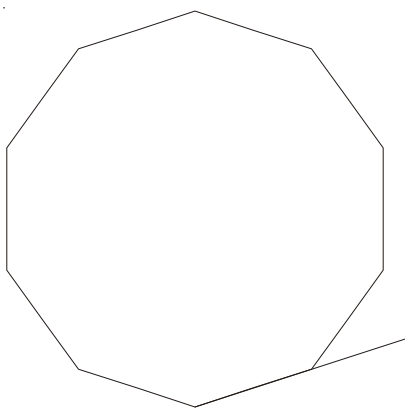


1)



- a) Work out the size of an **exterior** angle of a regular hexagon.
- b) Work out the size of an **interior** angle of a regular hexagon.

2)



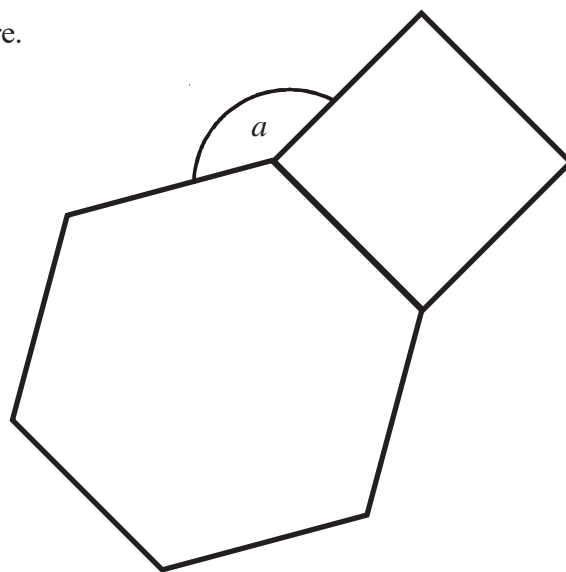
- a) Name the regular polygon, above.
- b) Work out the size of an **exterior** angle and of an **interior** angle for this polygon.

- 3) The size of each **exterior** angle of a regular polygon is  $40^\circ$ .  
Work out the number of sides of the regular polygon.
- 4) The size of each **interior** angle of a regular polygon is  $120^\circ$ .  
Work out the number of sides of the regular polygon.

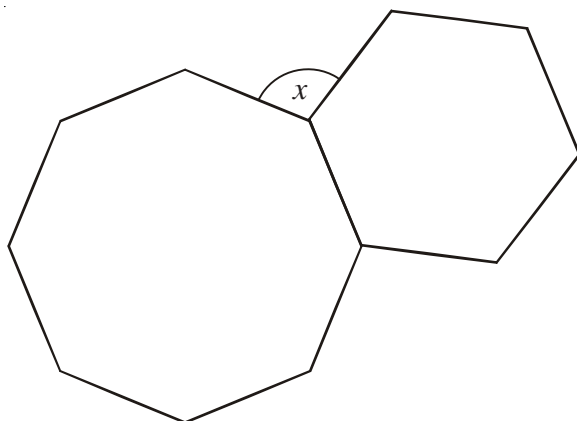


- 1) The diagram shows a regular hexagon and a square.

Calculate the size of the angle  $a$ .



- 2)



The diagram shows a regular octagon and a regular hexagon.

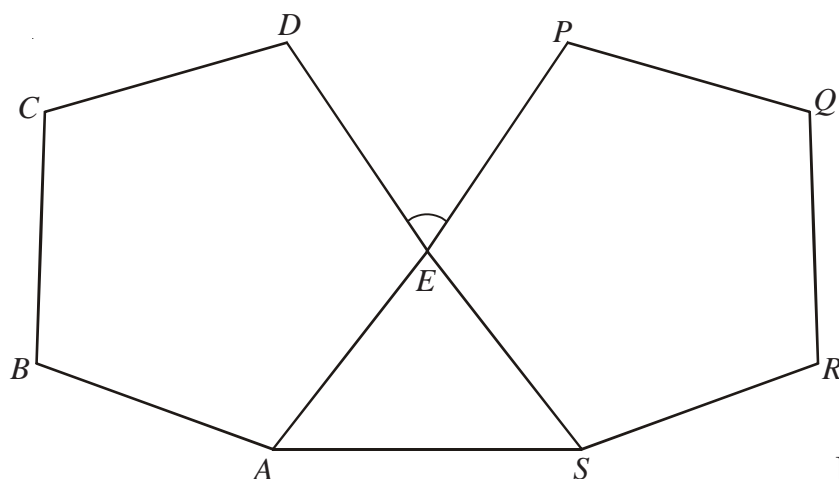
Work out the size of angle  $x$ .



- 3)  $ABCDE$  and  $PQRSE$  are regular pentagons.

$AES$  is an equilateral triangle.

Work out the size of angle  $DEP$ .



## Two-Way Tables

- 1) Billy has been carrying out a survey.  
He asked 100 people the type of water they like to drink (still, sparkling or both).  
Here are part of his results:

	Still	Sparkling	Both	Total
Male	26			53
Female		20	10	
Total			16	100

- a) Complete the two-way table.
- b) How many males were in the survey?
- c) How many females drink only still water?
- d) How many people drink only sparkling water?
- 2) 90 students each study one of three languages.  
The two-way table shows some information about these students.

	French	German	Spanish	Total
Female				
Male		7		
Total	20	18		90

- 50 of the 90 students are male.  
29 of the 50 male students study Spanish.
- a) Complete the two-way table.
- b) How many females study French?
- c) How many people study Spanish?
- 3) Karen asks 100 students if they like milk, plain or white chocolates best.  
36 of the students are girls.  
19 of these girls like milk chocolates best.  
16 boys like white chocolates best.  
8 out of the 24 students who like plain chocolates best are girls.  
Work out the number of students who like milk chocolates the best.



- 1) Kaya made a list of his homework marks.

3    2    3    4    1    4    5    4

- Write down the mode of Kaya's marks.
- Work out his mean homework mark.

- 2) Lydia rolled an 8-sided dice ten times.  
Here are her scores.

5    1    2    5    3    8    6    6    3    2

- Work out Lydia's median score.
- Work out the mean of her scores.



- 3) In a two-week period, a train was this many minutes late each day:

3    0    0    0    7    4    5    2    0    1    14    0    5    1

- What was the mean average number of minutes late?
- What was the median average number of minutes late?



- 4) Two small Year 10 classes, Set A and Set B, sat the same Science test.

Set A had these scores for the test:

63%, 71%, 48%, 95%, 46%, 82%, 77%, 36%, 73%

Set B had these scores:

58%, 63%, 85%, 61%, 59%, 38%, 90%, 84%, 75%, 48%

How much bigger was Set B's mean average score than Set A's mean average score?  
Give your answer correct to 1 decimal place.



- 5) A rugby team played six games.

The mean score for the six games is 15

The rugby team played one more game.

The mean score for all seven games is 16

Work out the number of points the team scored in the seventh game.

- 1) Ahmad does a statistical experiment.  
He throws a dice 600 times.  
He scores one, 200 times.  
Is the dice fair? Explain your answer
  
- 2) Chris has a biased coin.  
The probability that the biased coin will land on a tail is 0.3  
Chris is going to flip the coin 150 times.  
Work out an estimate for the number of times the coin will land on a tail.
  
- 3) On a biased dice, the probability of getting a six is  $\frac{2}{3}$ .  
The dice is rolled 300 times.  
Work out an estimate for the number of times the dice will land on a six.
  
- 4) On a biased dice, the probability of getting a three is 0.5  
The dice is rolled 350 times.  
Work out an estimate for the number of times the dice will land on a three.
  
- 5) Jenny throws a biased dice 100 times.  
The table shows her results.

Score	Frequency
1	15
2	17
3	10
4	24
5	18
6	16

- a) She throws the dice once more.  
Find an estimate for the probability that she will get a four.
  
- b) If the dice is rolled 250 times, how many times would you expect to get a five?

- 1) Two dice are rolled and their scores are multiplied together.
- a) Complete the possibility space to show all the possible results.

		First dice					
		1	2	3	4	5	6
Second dice	1						
	2						
	3				12		
	4						
	5						
	6			18			

- b) What is the probability of getting a result that is an even number?
- 2) Suppose there are three cards:

A **black card** that is black on both sides,

A **white card** that is white on both sides,

A **mixed card** that is black on one side and white on the other side.

All the cards are placed into a hat and one is taken out at random.

It is placed on a table and the side facing up is black.

What is the probability that the other side of the card is also black?

1) Write as a power of 8

a)  $8^4 \times 8^3$

b)  $8^{12} \div 8^7$

2) Write as a power of 3

a)  $3^2 \times 3^9$

b)  $3^{10} \div 3^3$

3) Simplify

a)  $k^5 \times k^2$

b)  $x^4 \div x^2$

c)  $\frac{k^{11}}{k^6}$

d)  $(k^8)^2$

4) Simplify

eg.  $(2xy^3)^4 = 2xy^3 \times 2xy^3 \times 2xy^3 \times 2xy^3 = 16x^4y^{12}$

a)  $(2xy^5)^3$

b)  $(2x^2y^2)^3$

c)  $(4xy^4)^2$

d)  $(3xy^2)^4$

5)  $2^x \times 2^y = 2^{10}$

and

$2^x \div 2^y = 2^2$

Work out the value of  $x$  and the value of  $y$ .

6)  $5^x \times 5^y = 5^{12}$

and

$5^x \div 5^y = 5^6$

Work out the value of  $x$  and the value of  $y$ .

7)  $a = 2^x$ ,  $b = 2^y$

Express in terms of  $a$  and  $b$

a)  $2^{x+y}$

b)  $2^{2x}$

c)  $2^{3y}$

d)  $2^{x+2y}$

1) a) Simplify  $d \times d \times d \times d$

b) Simplify  $t \times t^2$

c) Simplify  $m^5 \div m^3$

2) a) Simplify  $(2x^2)^3$

b) Simplify  $3x^2 \times 4x^5y^4$

3) a) Simplify  $t^4 \times t^5$

b) Simplify  $x^8 \div x^5$

c) Simplify  $(c^4)^3$

4) a) Simplify  $x^6 \times x^2$

b) Simplify  $\frac{x^8}{x^3}$

c) Simplify  $(2t)^3$

d) Simplify  $3x^2y \times 4x^5y^4$

5) a) Simplify  $x^3 \times x^4$

b) Simplify  $t^7 \div t^3$

c) Simplify  $4x^2y^4 \times 3xy^2$

6) a) Simplify  $x \times x \times x \times x$

b) Simplify  $2x \times 3y$



1) Change the following to normal (or ordinary) numbers.

a)  $4.3 \times 10^4$

c)  $7.03 \times 10^3$

e)  $1.01 \times 10^4$

b)  $6.79 \times 10^6$

d)  $9.2 \times 10^2$

f)  $4 \times 10^5$

2) Change the following to normal (or ordinary) numbers.

a)  $4.3 \times 10^{-4}$

c)  $7.03 \times 10^{-3}$

e)  $1.01 \times 10^{-4}$

b)  $6.79 \times 10^{-6}$

d)  $9.2 \times 10^{-2}$

f)  $4 \times 10^{-5}$

3) Change the following to standard form.

a) 360

c) 520 000

e) 1 003

b) 8 900

d) 60000

f) 6 450 000

4) Change the following to standard form.

a) 0.071

c) 0.00076

e) 0.00009

b) 0.0008

d) 0.0928

f) 0.00000173

5) Work out the following, giving your answer in standard form.

a)  $3\ 000 \times 5\ 000$

d)  $5 \times 4 \times 10^3$

g)  $7 \times 10^2 \times 3 \times 10^{-4}$

b)  $240 \times 0.0002$

e)  $\frac{8 \times 10^4}{4 \times 10^2}$

h)  $2 \times 3.6 \times 10^{-5}$

c)  $9 \times 1.1 \times 10^7$

f)  $9 \times 10^2 \times 2 \times 10^{-5}$

i)  $6 \times 4.1 \times 10^3$

## Highest Common Factor (HCF)

- 1) Find the Highest Common Factor of 16 and 24.
  
- 2) Find the Highest Common Factor of 21 and 28.
  
- 3) Find the Highest Common Factor of 60 and 150.
  
- 4) Find the Highest Common Factor of 96 and 108.
  
- 5)
  - (i) Write 42 and 63 as products of their prime factors.
  - (ii) Work out the Highest Common Factor of 42 and 63.

## Lowest Common Multiple (LCM)

- 1) Find the Lowest Common Multiple of 20 and 60.
  
- 2) Find the Lowest Common Multiple of 28 and 72.
  
- 3) Find the Lowest Common Multiple of 70 and 240.
  
- 4) Find the Lowest Common Multiple of 35 and 55.
  
- 5)
  - (i) Write 42 and 63 as products of their prime factors.
  - (ii) Work out the Lowest Common Multiple of 42 and 63.

- 1) a) Express 84 as a product of its prime factors.  
b) Find the Highest Common Factor (HCF) of 84 and 35.

- 2) Express 72 as the product of its prime factors.

- 3) Express 180 as the product of its prime factors.

- 4) a) Express 66 as a product of its prime factors.  
b) Express  $132^2$  as a product of its prime factors.



- 5) Express 252 as a product of its prime factors.



- 6) Find the Lowest Common Multiple (LCM) of 24 and 36.



- 7) a) Write 56 as a product of its prime factors.  
b) Find the Highest Common Factor (HCF) of 56 and 42.



- 8) a) Express 45 as a product of its prime factors.  
b) Find the Highest Common Factor (HCF) of 45 and 30.



- 9) a) Find the Highest Common Factor (HCF) of 24 and 30.  
b) Find the Lowest Common Multiple (LCM) of 4, 5 and 6.

1) A silver necklace has a mass of 123 grams, correct to the nearest gram.

- Write down the least possible mass of the necklace.
- Write down the greatest possible mass of the necklace.

2) Each of these measurements was made correct to one decimal place.

Write the maximum and minimum possible measurement in each case.

- |           |           |                |              |
|-----------|-----------|----------------|--------------|
| a) 4.6 cm | b) 0.8 kg | c) 12.5 litres | d) 25.0 km/h |
| e) 10.3 s | f) 36.1 m | g) 136.7 m/s   | h) 0.1 g     |



3) Each side of a regular octagon has a length of 20.6 cm, correct to the nearest millimetre.

- Write down the least possible length of each side.
- Write down the greatest possible length of each side.
- Write down the greatest possible perimeter of the octagon.

4) A girl has a pen that is of length 12 cm, measured to the nearest centimetre.

Her pencil case has a diagonal of length 12.5 cm, measured to the nearest millimetre.

Explain why it might not be possible for her to fit the pen in the pencil case.



5) A square has sides of length 7 cm, correct to the nearest centimetre.

- Calculate the lower bound for the perimeter of the square.
- Calculate the upper bound for the area of the square.

## Sharing Using Ratio

- 1) Tom and Julie share £48 in the ratio 5 : 3  
Work out how much more money Tom gets than Julie gets.
- 2) Ben and Sue share £60 in the ratio 2 : 3  
Work out how much each person gets.
- 3) A box contains milk chocolates and plain chocolates only.  
The number of milk chocolates to the number of plain chocolates is in the ratio 2 : 1  
There are 24 milk chocolates.  
Work out the total number of chocolates.
- 4) Andy, Ben and Claire share £54  
Ben gets three times as much money as Andy.  
Claire gets twice as much money as Ben.

How much money does Claire get?



- 5) There are some marbles in a bag.  
18 of the marbles are blue.  
12 of the marbles are red.
  - a) Write down the ratio of the number of blue marbles to the number of red marbles.  
Give your ratio in its simplest form.

There are some apples and pears in a box.  
The total number of apples and pears is 54.  
The ratio of the number of apples to the number of pears is 1 : 5  
b) Work out the number of pears in the box.

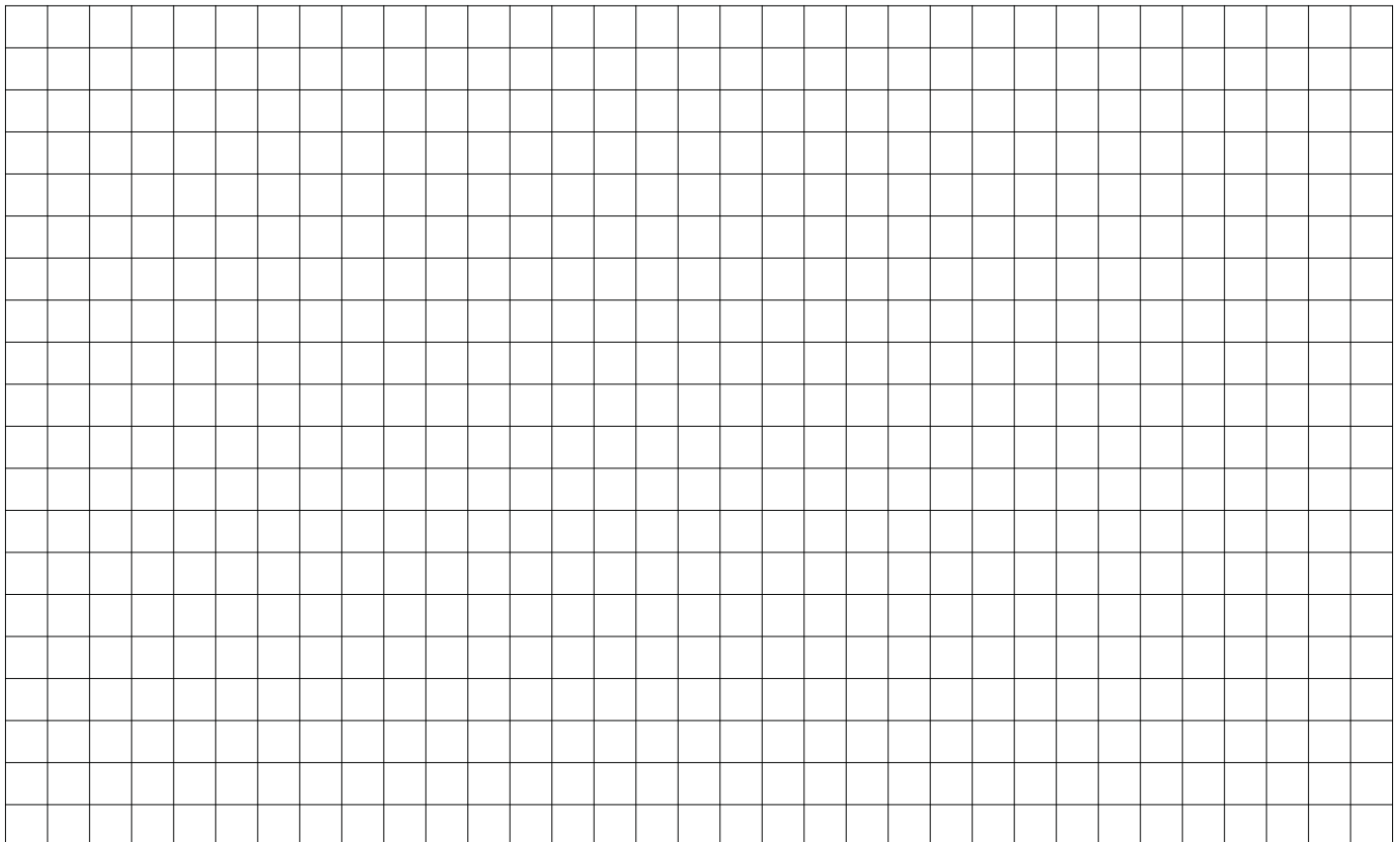


- 6) A piece of string is 180 cm long.  
Jim cuts it into three pieces in the ratio 2 : 3 : 4  
Work out the length of the longest piece.



- 7) Sally is 13 years old.  
Tammy is 12 years old.  
Danny is 10 years old.  
  
Sally, Tammy and Danny share £28 in the ratio of their ages.  
Tammy gives a third of her share to her mother.  
How much should Tammy now have?

- 1) In a box of chocolates, the ratio of plain chocolates to milk chocolates is 2 : 5.
  - a) What fraction of the chocolates are plain ones?
  - b) What fraction of the chocolates are milk ones?
  
- 2) If the ratio of  $x : y$  is 3 : 7, which of the following statements are correct?
  - a)  $x$  is  $\frac{3}{7}$  of  $(x + y)$
  - b)  $x$  is  $\frac{3}{10}$  of  $(x + y)$
  - c)  $y$  is  $\frac{7}{10}$  of  $x$
  - d)  $y$  is  $\frac{7}{10}$  of  $(x + y)$
  
- 3) Pounds can be converted to kilograms using the ratio 11 : 5.
  - a) Use the squares, below, to draw a conversion graph to illustrate this.
  - b) Convert 24 pounds to kilograms.
  - c) Convert 14 kilograms to pounds.



## Increase/Decrease by a Percentage

- 1) Increase:
 

a) 500 by 10%	c) 80 by 15%
b) 320 by 10%	d) 75 by 20%
  
- 2) Decrease:
 

a) 400 by 10%	c) 140 by 15%
b) 380 by 10%	d) 35 by 20%
  
- 3) The price of a laptop is increased by 15%.  
The old price of the laptop was £300.  
Work out the new price.
  
- 4) The price of a £6800 car is reduced by 10%.  
What is the new price?



- 5) Increase:
 

a) 65 by 12%	c) 600 by 17.5%
b) 120 by 23%	d) 370 by 17.5%



- 6) Decrease:
 

a) 42 by 15%	c) 52 by 8.5%
b) 79 by 12%	d) 8900 by 18%



- 7) The price of a mobile phone is £78.40 plus VAT.  
VAT is charged at a rate of 17.5%.  
What is the total price of the mobile phone?



- 8) In a sale, normal prices are reduced by 7%.  
The normal price of a camera is £89.  
Work out the sale price of the camera.



- 9) A car dealer offers a discount of 20% off the normal price of a car, for cash.  
Peter intends to buy a car which usually costs £6800.  
He intends to pay by cash.  
Work out how much he will pay.



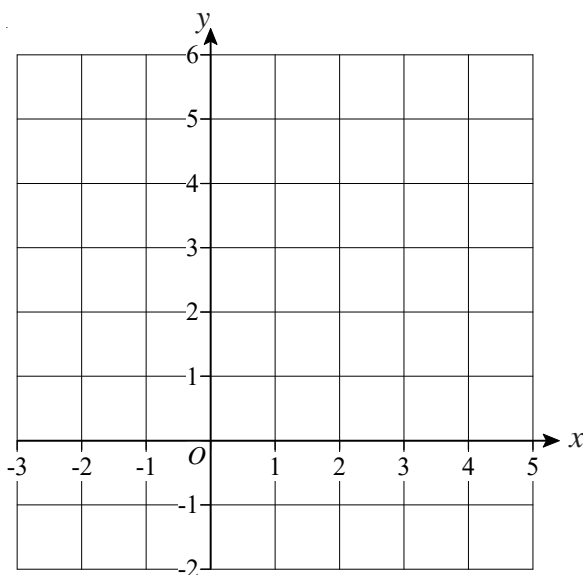
- 10) A month ago, John weighed 97.5 kg.  
He now weighs 4.5% more.  
Work out how much John now weighs.  
Give your answer to 1 decimal place.




- 1) Meg has £1200 in her savings account.  
The account pays 5% simple interest per year.  
  
How much interest will she earn in 4 years?
  
- 2) Dan has £4000 in his savings account.  
This account pays 2% interest per year.  
  
How much interest will he earn in 6 years?
  
- 3) Chris borrows £6000 at a simple interest rate of 10% per year.  
He pays the money back after 4 years.  
  
How much does he pay back in total?
  
- 4) Lisa borrows £3000 at a simple interest rate of 2.5% per year.  
She pays the money back after 3 years.  
  
How much does she pay back in total?
  
- 5) Kate borrows £2000 at a simple interest rate of 16% per year.  
She pays the money back after 3 months.  
  
How much does she pay back in total?
  
- 6) Neil invested £8000 in a savings account for 2 years.  
He earned £640 simple interest over the two years.  
  
What was the interest rate?

## Midpoint of a Line on a Graph

- 1) Find the midpoint of  $A$  and  $B$  where  $A$  has coordinates  $(-2, 5)$  and  $B$  has coordinates  $(4, -1)$ .



- 2) Find the midpoint of  $A$  and  $B$  where  $A$  has coordinates  $(2, 0)$  and  $B$  has coordinates  $(8, 6)$ .
- 3) Find the midpoint of  $A$  and  $B$  where  $A$  has coordinates  $(-4, -2)$  and  $B$  has coordinates  $(2, 4)$ .
- 4) Find the midpoint of  $A$  and  $B$  where  $A$  has coordinates  $(-3, -2)$  and  $B$  has coordinates  $(7, 5)$ .
- 5) Find the midpoint of  $A$  and  $B$  where  $A$  has coordinates  $(2, -5)$  and  $B$  has coordinates  $(7, 4)$ .
- 6) Find the midpoint of  $A$  and  $B$  where  $A$  has coordinates  $(-7, -4)$  and  $B$  has coordinates  $(-2, -1)$ .
- 7) The midpoint of  $A$  and  $B$  is at  $(1, 3)$ .  
The coordinates of  $A$  are  $(-2, 4)$ .  
Work out the coordinates of  $B$ .
- 8)  The midpoint of  $A$  and  $B$  is at  $(3.5, 2.5)$ .  
The coordinates of  $A$  are  $(2, 5)$ .  
Work out the coordinates of  $B$ .

## Expanding and Simplifying Brackets

1) Expand these brackets

- a)  $2(x + 3)$
- b)  $3(2x + 4)$
- c)  $5(3p - 2q)$
- d)  $4(x^2 + 2y^2)$
- e)  $6(r - r^2)$

2) Expand these brackets

- a)  $x(x - 2)$
- b)  $x(3x + 5)$
- c)  $p(3p - 7q)$
- d)  $y(y + 6y^2)$
- e)  $x(r + r^2)$

3) Expand these brackets

- a)  $2x(x - 5)$
- b)  $4x(2x + 3)$
- c)  $5p(4p - 2q)$
- d)  $2y(3y + 4x^2)$
- e)  $x(x + r^2)$

4) Expand these brackets

- a)  $x(x^2 - 2)$
- b)  $3x(2x^3 + 1)$
- c)  $5p^2(4p - 2)$
- d)  $2y^2(3y^3 + 4y)$
- e)  $2xy(x + y^2)$

5) Expand and simplify

- a)  $2(x + y) + 3(x + y)$
- b)  $3(2x + y) + 2(5x + 3y)$
- c)  $5(x + y) + 3(2x + y)$
- d)  $3(2c + d) + 2(c + d)$
- e)  $4(2p + q) + 3(2p + q)$

6) Expand and simplify

- a)  $2(x + y) + 3(x - y)$
- b)  $5(2x + y) + 2(3x - 2y)$
- c)  $4(x - y) + 3(2x + y)$
- d)  $6(2c - d) + 2(c - d)$
- e)  $2(5p - q) + 3(p - 2q)$

7) Expand and simplify

- a)  $3(x + 2y) - 3(x - y)$
- b)  $5(2x - y) - 2(3x - 2y)$
- c)  $7(x - 2y) - 3(2x + y)$
- d)  $6(2x - y) - 2(x + 2y)$
- e)  $2(5p - q) - (p - 3q)$

## Expanding and Simplifying Brackets

1) Expand and simplify

a)  $(x + 3)(x + 2)$

b)  $(x + 5)(x + 3)$

c)  $(x + 1)(x + 4)$

d)  $(x + 6)(x + 4)$

e)  $(x + 5)(x + 7)$

2) Expand and simplify

a)  $(x + 5)(x - 2)$

b)  $(x - 7)(x + 2)$

c)  $(x - 1)(x + 3)$

d)  $(x + 4)(x - 3)$

e)  $(x - 5)(x + 5)$

3) Expand and simplify

a)  $(x - 3)(x - 4)$

b)  $(x - 2)(x - 6)$

c)  $(x - 1)(x - 1)$

d)  $(x - 7)(x - 2)$

e)  $(x - 4)(x - 5)$

4) Expand and simplify

a)  $(x - 7)(x + 1)$

b)  $(p - 6)(p + 4)$

c)  $(e - 3)(e - 7)$

d)  $(x + 8)(x + 1)$

e)  $(x - 5)(x - 5)$

5) Expand and simplify

a)  $(2x + 3)(2x + 1)$

b)  $(3p - 4)(2p + 5)$

c)  $(e - 3)(3e - 4)$

d)  $(4x - 6)(2x + 1)$

e)  $(2x - 3)(2x + 3)$

6) Expand and simplify

a)  $(2x + y)(3x + 2y)$



b)  $(3p - 2q)(4p + 5q)$

c)  $(4e - 3f)(2e - 2f)$

d)  $(6x - y)(6x + y)$

e)  $(3x - 2y)(x - 5y)$

## Solving Equations

- 1) Solve  $2x - 3 = 17$
- 2) Solve  $3x + 2 = 14$
- 3) Solve  $5x - 7 = 33$
- 4) Solve  $4x + 7 = 19$
- 5) Solve  $x + x + x + x = 20$
- 6) Solve  $x + 3x = 24$
- 7) Solve  $2(x + 3) = 8$
- 8) Solve  $2(3x - 4) = 22$
- 9) Solve  $5(t - 1) = 20$
- 10) Solve  $3(2x + 5) = 36$
- 11) Solve  $2x + 7 = x + 11$
- 12) Solve  $5y - 2 = 3y + 10$
- 13) Solve  $2x + 1 = 5x - 20$
- 14) Solve  $p - 3 = 3p - 11$
- 15) Solve  $2d + 5 = 20 - 3d$
- 16) Solve  $4 - e = 2e - 8$
- 17) Solve  $2(x + 3) = x + 9$
- 18) Solve  $x - 7 = 3(2x - 4)$
- 19) Solve  $5(x + 3) = 2(x + 6)$
- 20) Solve  $4(2y + 1) = 2(12 - y)$
- 21) Solve  $7 - 3x = 2(x + 1)$
- 22) Solve  $\frac{x}{2} = 5$
- 23) Solve  $\frac{x}{5} = 6$
- 24) Solve  $\frac{2x}{3} = 4$
- 25) Solve  $\frac{5x}{2} = 15$
- 26) Solve  $\frac{x - 2}{3} = 1$
- 27) Solve  $\frac{x + 5}{2} = 7$
- 28) Solve  $\frac{2x + 1}{4} = 2$
- 29) Solve  $\frac{5x - 3}{3} = 4$
- 30) Solve  $\frac{x + 2}{3} = x + 4$
-  31) Solve  $\frac{3x - 1}{4} = 2x - 3$
-  32) Solve  $\frac{4x + 3}{5} = \frac{2x - 1}{2}$

- 1) Make  $c$  the subject of the formula.

$$a = b + cd$$

- 2) Make  $t$  the subject of the formula.

$$u = v + 2t$$

- 3) Make  $n$  the subject of the formula.

$$M = 3n + 5$$

- 4) Make  $z$  the subject of the formula.

$$x = 3y + z$$

- 5)  $r = 5s + 3t$

a) Make  $t$  the subject of the formula.

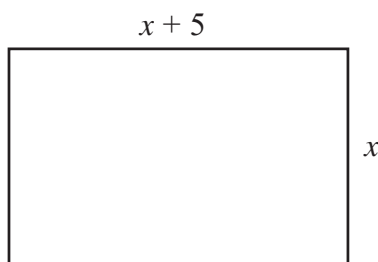
b) Make  $s$  the subject of the formula.

- 6) Rearrange  $y = 3x + 1$  to make  $x$  the subject.

- 7) Rearrange  $y = \frac{1}{2}x + 2$  to make  $x$  the subject.

- 8) Rearrange  $y = \frac{1}{3}x + 1$  to make  $x$  the subject.

- 1) The width of a rectangle is  $x$  centimetres.  
The length of the rectangle is  $(x + 5)$  centimetres.



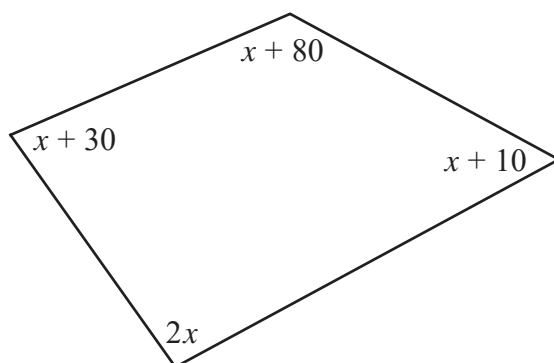
- a) Find an expression, in terms of  $x$ , for the perimeter of the rectangle.  
Give your answer in its simplest form.

The perimeter of the rectangle is 38 centimetres.

- b) Work out the length of the rectangle.



2)



*Diagram **NOT** accurately drawn*

The sizes of the angles, in degrees, of the quadrilateral are

$x + 10$   
 $2x$   
 $x + 80$   
 $x + 30$

- a) Use this information to write down an equation in terms of  $x$ .  
b) Use your answer to part (a) to work out the size of the smallest angle of the quadrilateral.



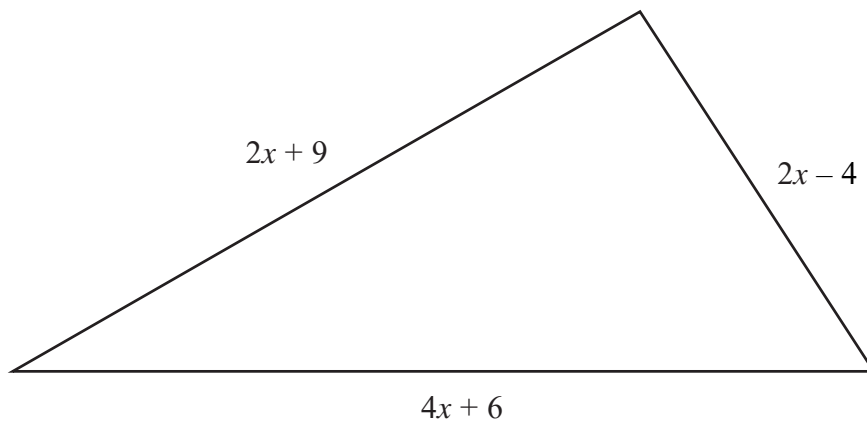
- 3) Sarah buys 6 cups and 6 mugs

A cup costs  $\pounds x$

A mug costs  $\pounds (x + 3)$

- a) Write down an expression, in terms of  $x$ , for the total cost, in pounds, of 6 cups and 6 mugs.  
b) If the total cost of 6 cups and 6 mugs is  $\pounds 48$ , write an equation in terms of  $x$ .  
c) Solve your equation to find the cost of a cup and the cost of a mug.

1)



In the diagram, all measurements are in centimetres.

The lengths of the sides are

$$\begin{aligned} 2x + 9 \\ 2x - 4 \\ 4x + 6 \end{aligned}$$

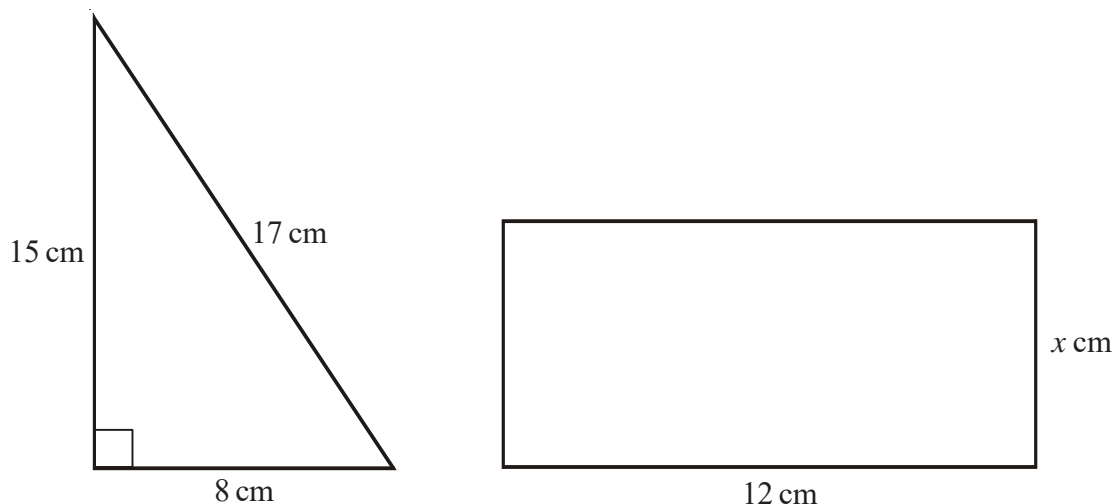
- a) Find an expression, in terms of  $x$ , for the perimeter of the triangle.  
Give your expression in its simplest form.

The perimeter of the triangle is 39 cm.

- b) Find the value of  $x$ .



- 2) The diagram shows a right-angled triangle and a rectangle.



The area of the right-angled triangle is equal to the area of the rectangle.

Find the value of  $x$ .



## Forming Formulae and Equations

- 1) A shop sells small boxes and large boxes for storing CDs.

A small box stores  $x$  CDs.

A large box stores  $y$  CDs.

Emma buys 8 small boxes and 5 large boxes.

Emma can store a total of  $T$  CDs in these boxes.

Write down a formula for  $T$  in terms of  $x$  and  $y$ .

- 2) Batteries are sold in packets and boxes.

Each packet contains 4 batteries.

Each box contains 20 batteries.

Tony buys  $p$  packets of batteries and  $b$  boxes of batteries.

Tony buys a total of  $N$  batteries.

Write down a formula for  $N$  in terms of  $p$  and  $b$ .

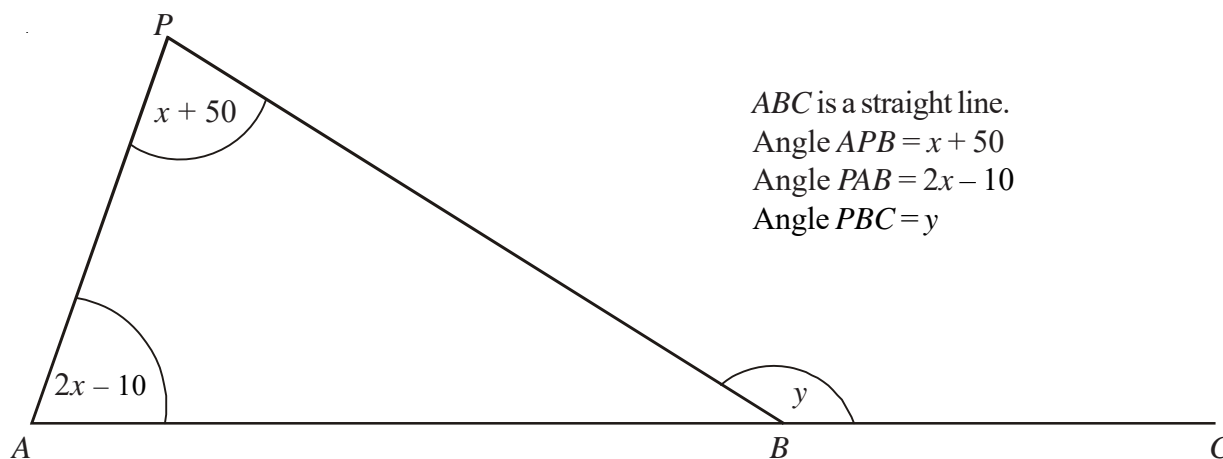
- 3) Compasses cost  $c$  pence each.

Rulers cost  $r$  pence each.

Write down an expression for the total cost, in pence, of 2 compasses and 4 rulers.



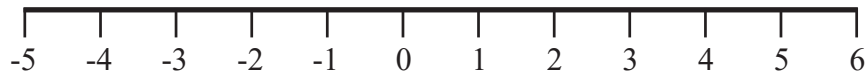
4)



- a) Show that  $y = 3x + 40$   
 Give reasons for each stage of your working.
- b) Given that  $y$  equals 145 degrees
- Work out the value of  $x$ .
  - Work out the size of the largest angle in triangle  $APB$ .

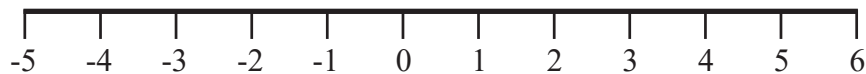
- 1) Represent this inequality on the number line

$$-3 < x \leq 2$$

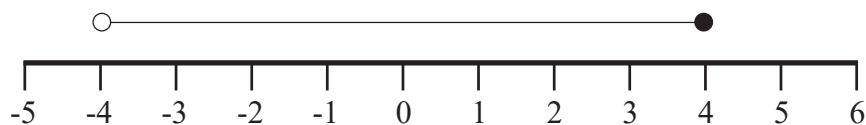


- 2) Represent this inequality on the number line

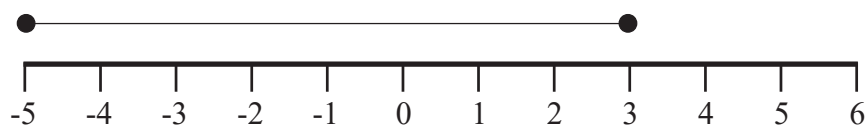
$$-1 \leq x < 5$$



- 3) Write down the inequality shown



- 4) Write down the inequality shown



- 5) If  $y$  is an integer, write down all the possible values of

$$-2 < y \leq 5$$

- 6) If  $x$  is an integer, write down all the possible values of

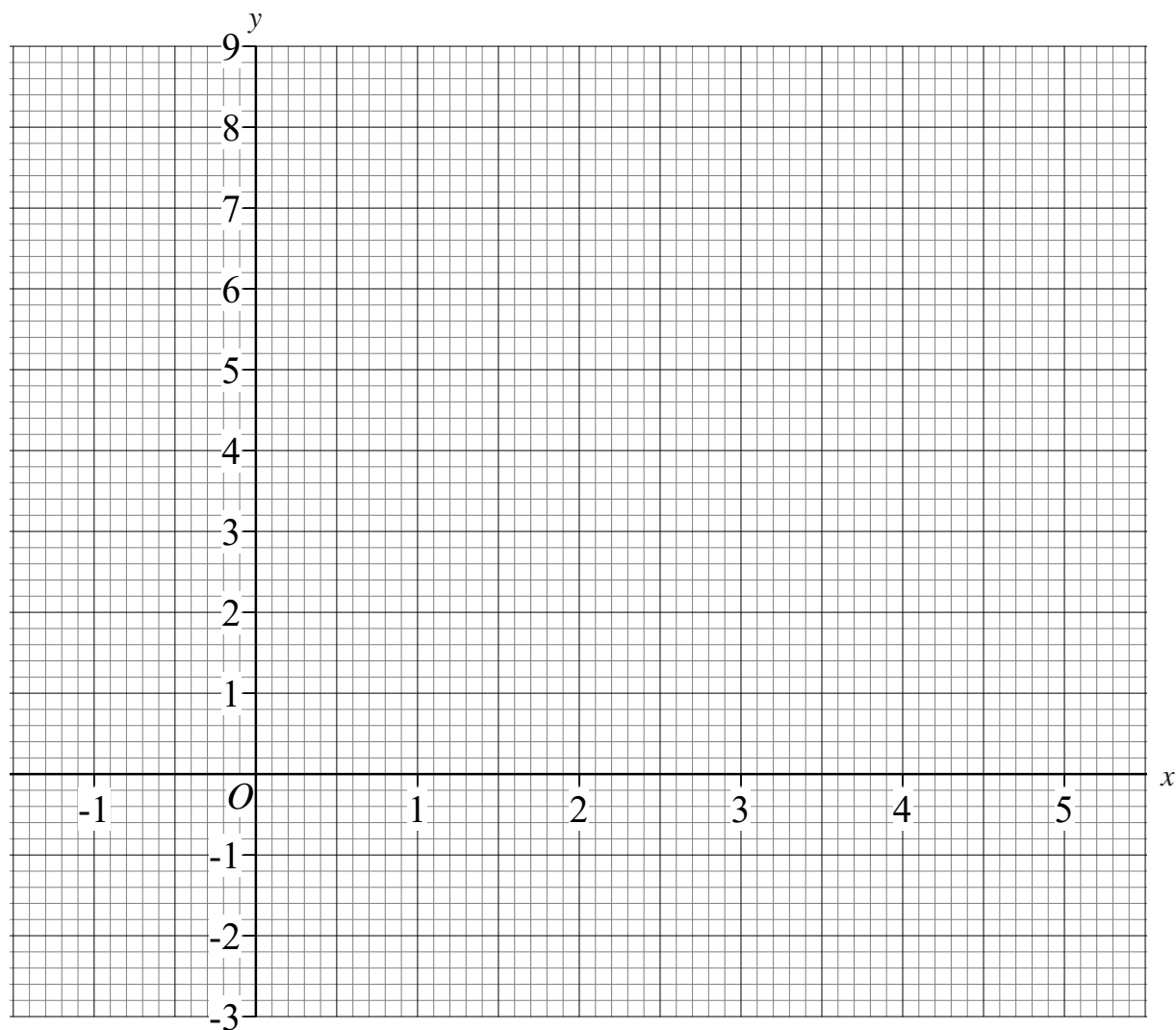
$$-9 < x < -5$$

## Drawing Quadratic Graphs

1) Complete the table of values for  $y = x^2 - 4x + 3$

$x$	-1	0	1	2	3	4	5
$y$		3	0		0		8

On the grid, draw the graph of  $y = x^2 - 4x + 3$

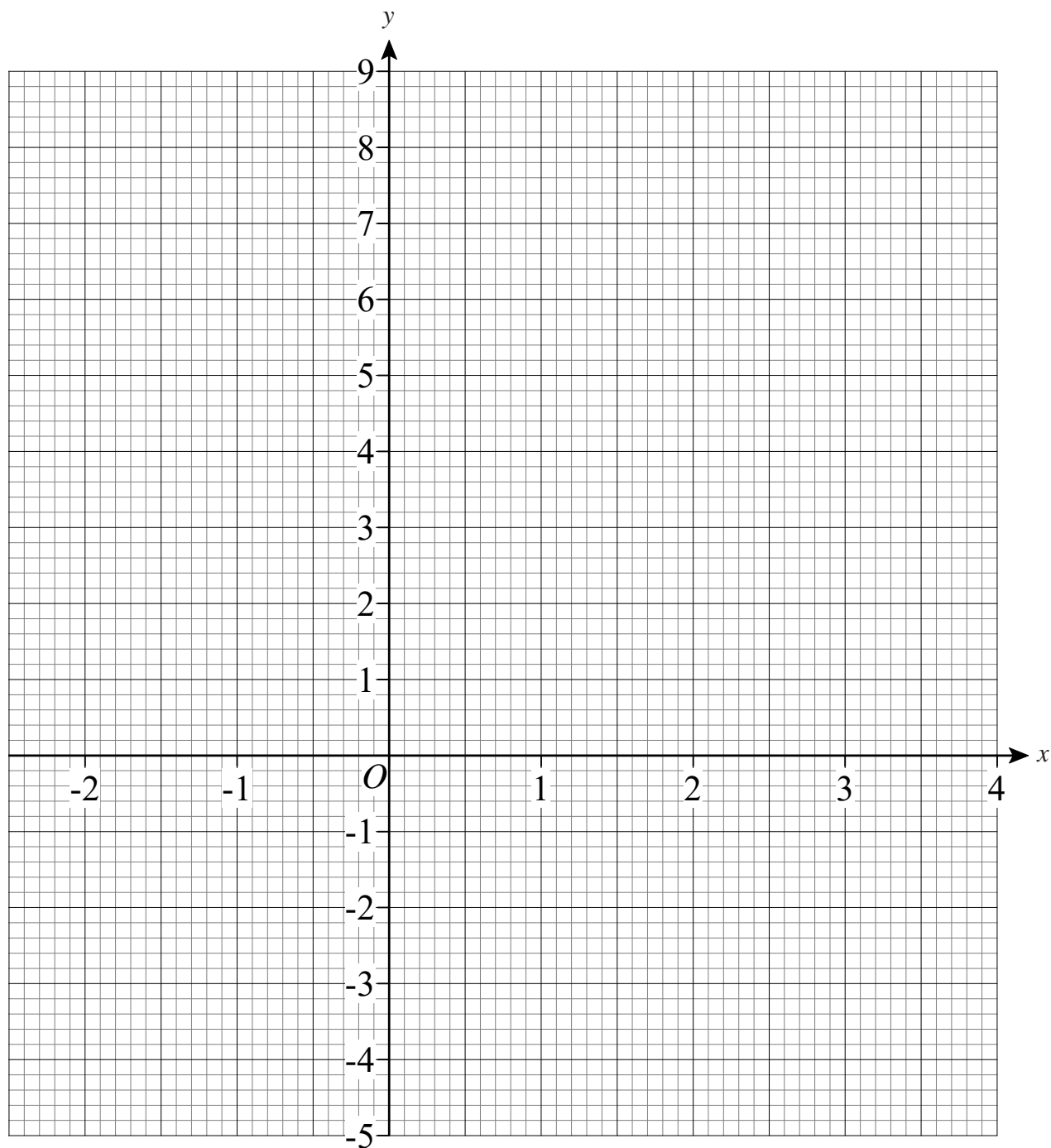


## Drawing Quadratic Graphs

- 1) a) Complete the table of values for  $y = x^2 - 3x - 2$

x	-2	-1	0	1	2	3	4
y		2	-2	-4		-2	

- b) On the grid, draw the graph of  $y = x^2 - 3x - 2$



- c) Use your graph to estimate the values of  $x$  when  $y = -1$

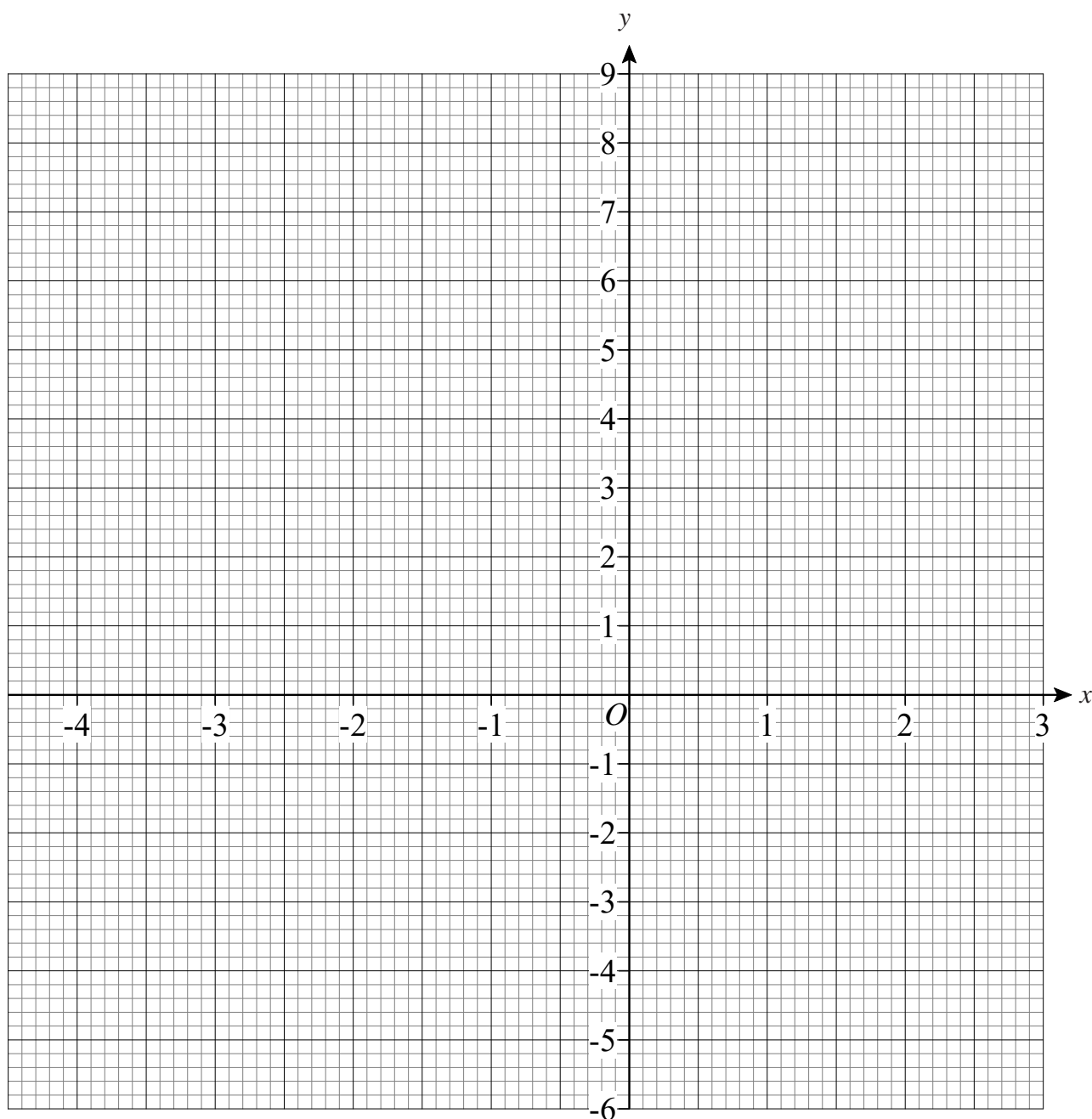
## Drawing Quadratic Graphs



1) a) Complete the table of values for  $y = x^2 + x - 4$

$x$	-4	-3	-2	-1	0	1	2	3
$y$	8		-2	-4				8

b) On the grid, draw the graph of  $y = x^2 + x - 4$



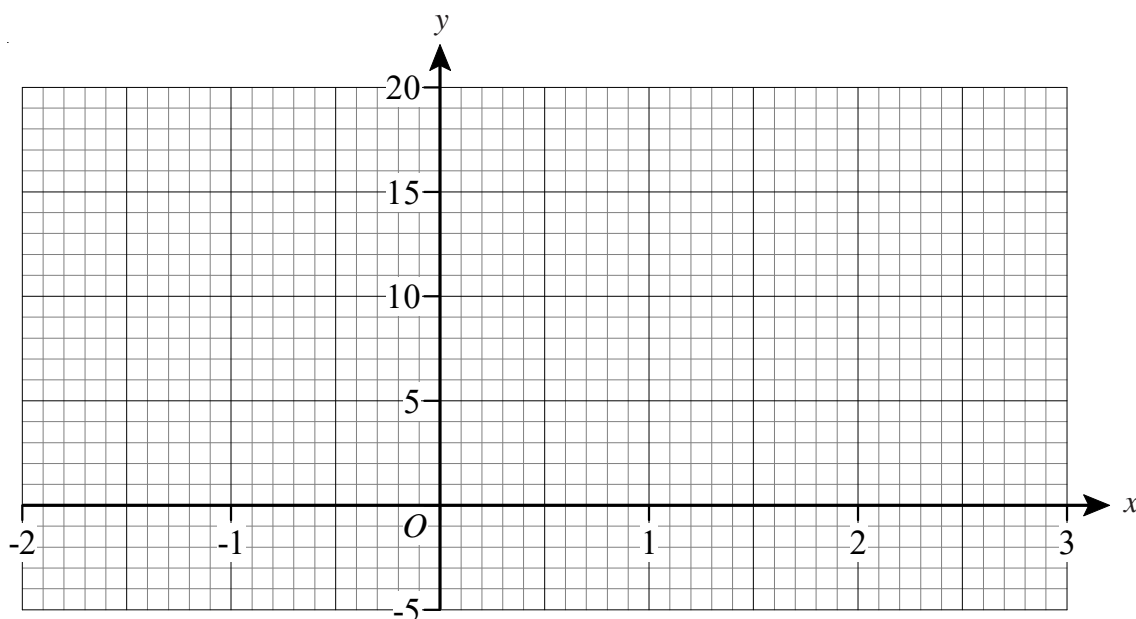
## Drawing Quadratic Graphs



- 1) a) Complete the table of values for  $y = 2x^2 - 3x$

$x$	-2	-1	0	1	2	3
$y$	14		0			9

- b) On the grid, draw the graph of  $y = 2x^2 - 3x$  for values of  $x$  from -2 to 3



- c) Use the graph to find the value of  $y$  when  $x = -1.5$

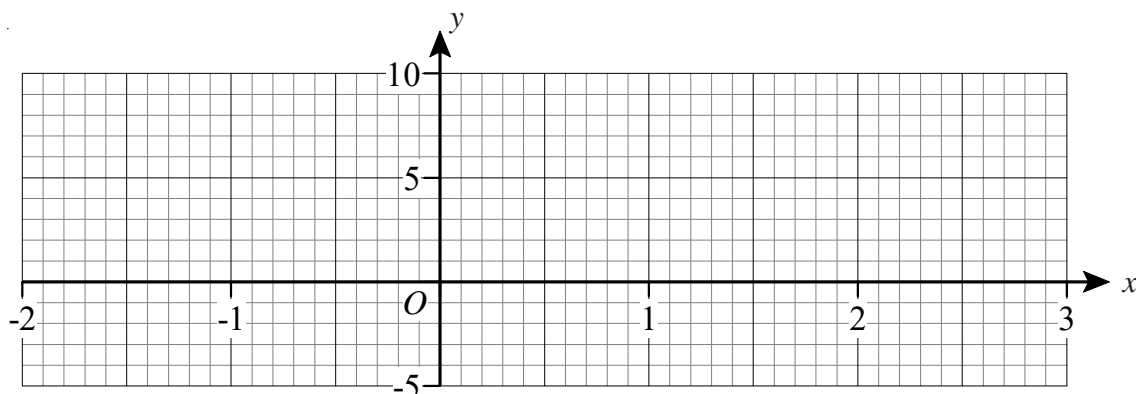
- d) Use the graph to find the values of  $x$  when  $y = 4$



- 2) a) Complete the table of values for  $y = x^2 - 2x$

$x$	-2	-1	0	1	2	3
$y$	8		0			

- b) On the grid, draw the graph of  $y = x^2 - 2x$  for values of  $x$  from -2 to 3

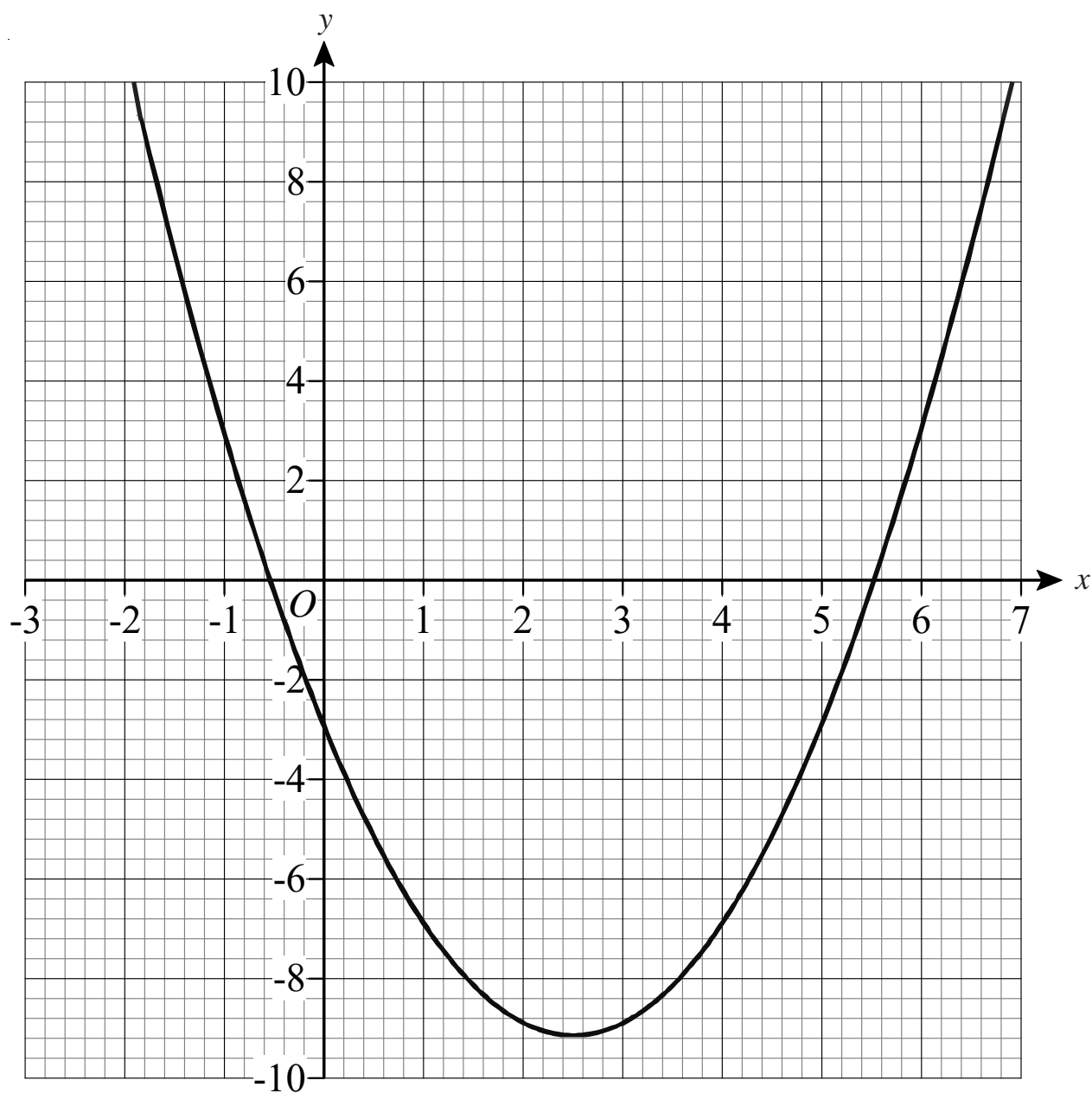


- c) (i) On the same axes draw the straight line  $y = 2.5$

- (ii) Write down the values of  $x$  for which  $x^2 - 2x = 2.5$

## Drawing Quadratic Graphs

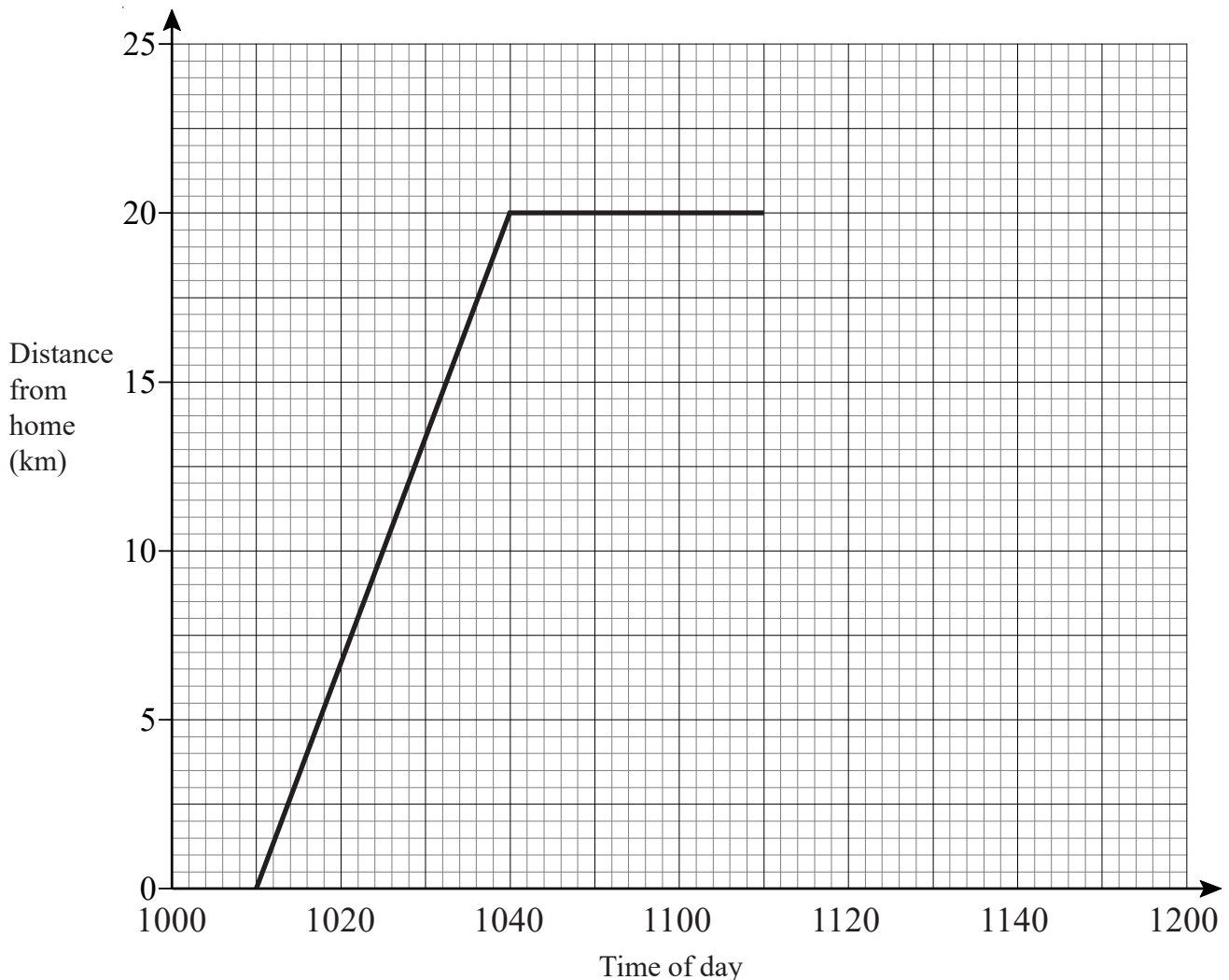
- 1) The diagram shows the graph of  $y = x^2 - 5x - 3$



- a) Use the graph to find estimates for the solutions of
- $x^2 - 5x - 3 = 0$
  - $x^2 - 5x - 3 = 6$
- b) Use the graph to find estimates for the solutions of the simultaneous equations
- $$y = x^2 - 5x - 3$$
- $$y = x - 4$$

## Distance-Time Graphs

- 1) Sarah travelled 20 km from home to her friend's house.  
She stayed at her friend's house for some time before returning home.  
Here is the travel graph for part of Sarah's journey.



a) At what time did Sarah leave home?

b) How far was Sarah from home at 10 30?

Sarah left her friend's house at 11 10 to return home.

c) Work out the time in minutes Sarah spent at her friend's house.

Sarah returned home at a steady speed.

She arrived home at 11 50

d) Complete the travel graph.

e) Work out Sarah's average speed on her journey from her home to her friend's house.  
Give your answer in kilometres per hour.

f) Work out Sarah's average speed on her journey home from her friend's house.  
Give your answer in kilometres per hour.



- 1) Here are the first five terms of an arithmetic sequence.

1      3      5      7      9

Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.

- 2) Here are the first five terms of an arithmetic sequence.

6      10      14      18      22

Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.

- 3) Here are the first five terms of an arithmetic sequence.

1      4      7      10      13

Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.

- 4) Here are the first five terms of an arithmetic sequence.

7      12      17      22      27

Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.

- 5) Here are the first five terms of an arithmetic sequence.

8      6      4      2      0

Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.

- 1) Here are the first four terms of an arithmetic sequence.

4      7      10      13

Find an expression, in terms of  $n$ , for the  $n$ th term of the sequence.

- 2) The  $n$ th term of a number sequence is  $n^2 + 3$   
Write down the first three terms of the sequence.

- 3) Here are the first five terms of an arithmetic sequence.

2      7      12      17      22

- a) Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.
- b) An expression for the  $n$ th term of another sequence is  $11 - n^2$
- (i) Find the third term of this sequence.
- (ii) Find the fifth term of this sequence.

- 4) The  $n$ th term of a sequence is  $2n^2$
- (i) Find the 4th term of the sequence.
- (ii) Is the number 400 a term of the sequence?
- Give reasons for your answer.

- 1) The  $n$ th term of a number sequence is given by  $4n + 1$
- a) Work out the first **two** terms of the number sequence.

Here are the first four terms of another number sequence.

1   4   7   10

- b) Find, in terms of  $n$ , an expression for the  $n$ th term of this number sequence.

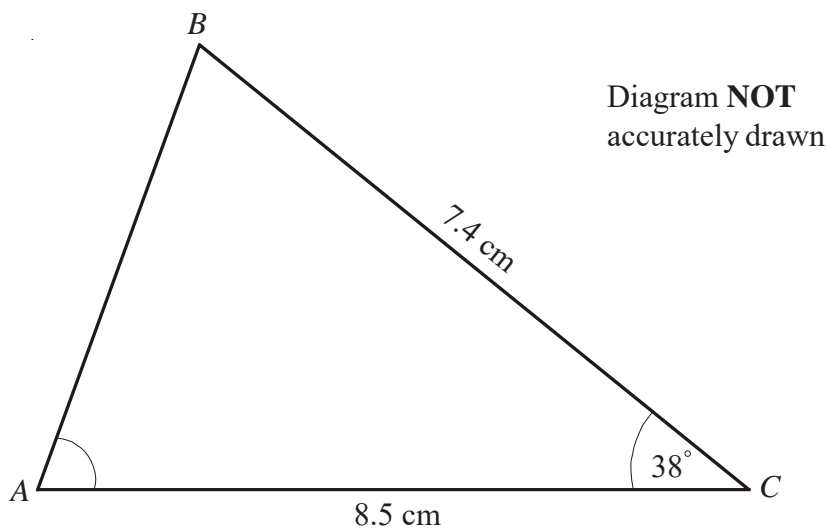
- 2) Here is a number pattern.

Line Number			
<b>1</b>	$1^2 + 3^2$	$2 \times 2^2 + 2$	10
<b>2</b>	$2^2 + 4^2$	$2 \times 3^2 + 2$	20
<b>3</b>	$3^2 + 5^2$	$2 \times 4^2 + 2$	34
<b>4</b>			
.			
.			
<b>10</b>			

- a) Complete Line Number 4 of the pattern.
- b) Complete Line Number 10 of the pattern.
- c) Use the number pattern to find the answer to  $999^2 + 1001^2$

## Drawing a Triangle Using Compasses

- 1) The diagram shows a sketch of triangle  $ABC$ .



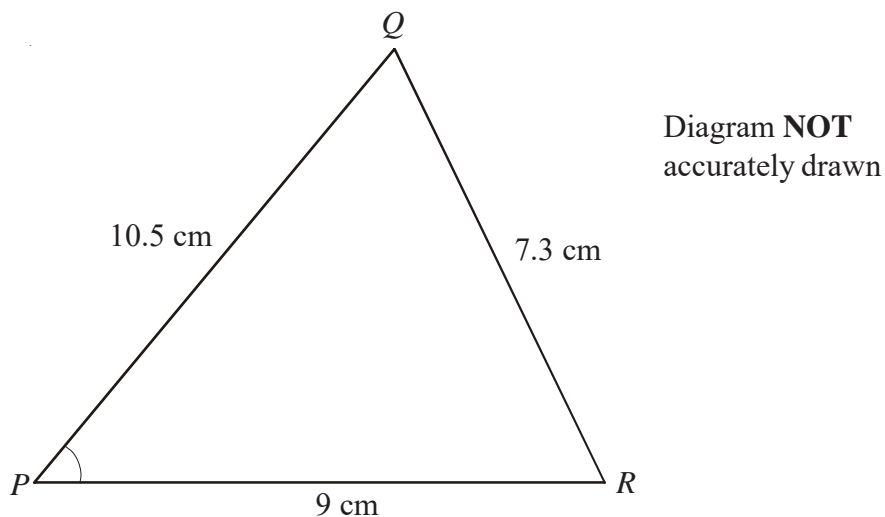
$$BC = 7.4 \text{ cm}$$

$$AC = 8.5 \text{ cm}$$

$$\text{Angle } C = 38^\circ$$

- Make an accurate drawing of triangle  $ABC$ .
  - Measure the size of angle  $A$  on your diagram.
- 2) Use ruler and compasses to **construct** an equilateral triangle with sides of length 6 centimetres.  
You must show all construction lines.

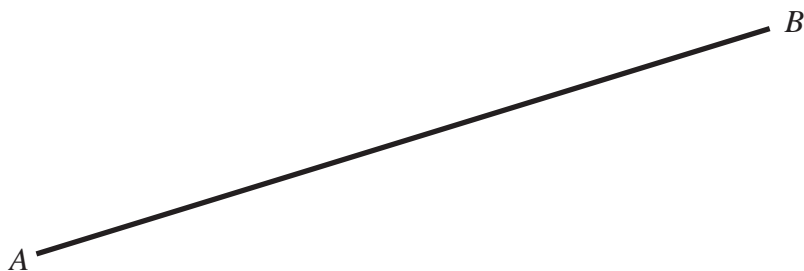
- 3) The diagram shows a sketch of triangle  $PQR$ .



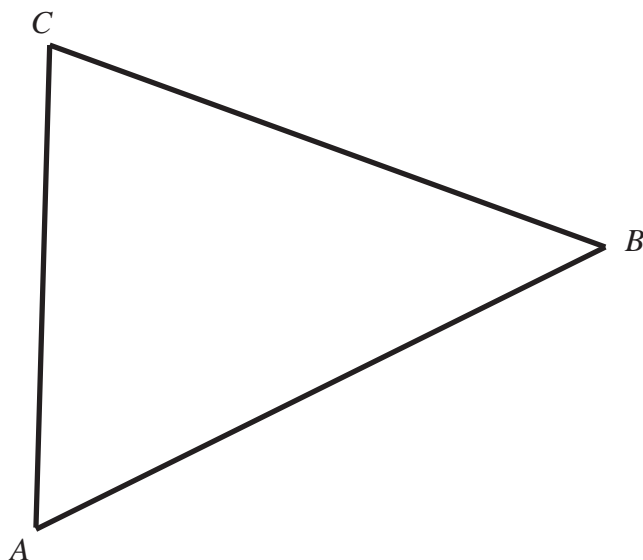
- Use ruler and compasses to make an accurate drawing of triangle  $PQR$ .
- Measure angle  $P$ .

## Bisecting a Line

- 1) Use ruler and compasses to bisect the line segment  $AB$ .  
You must show all construction lines.



- 2) Using ruler and compasses
- a) Bisect line  $AB$
  - b) Bisect line  $BC$
  - c) Bisect line  $AC$
  - d) Place your compass point where your three lines cross\*  
Now open them out until your pencil is touching vertex  $A$ .  
Draw a circle using this radius.



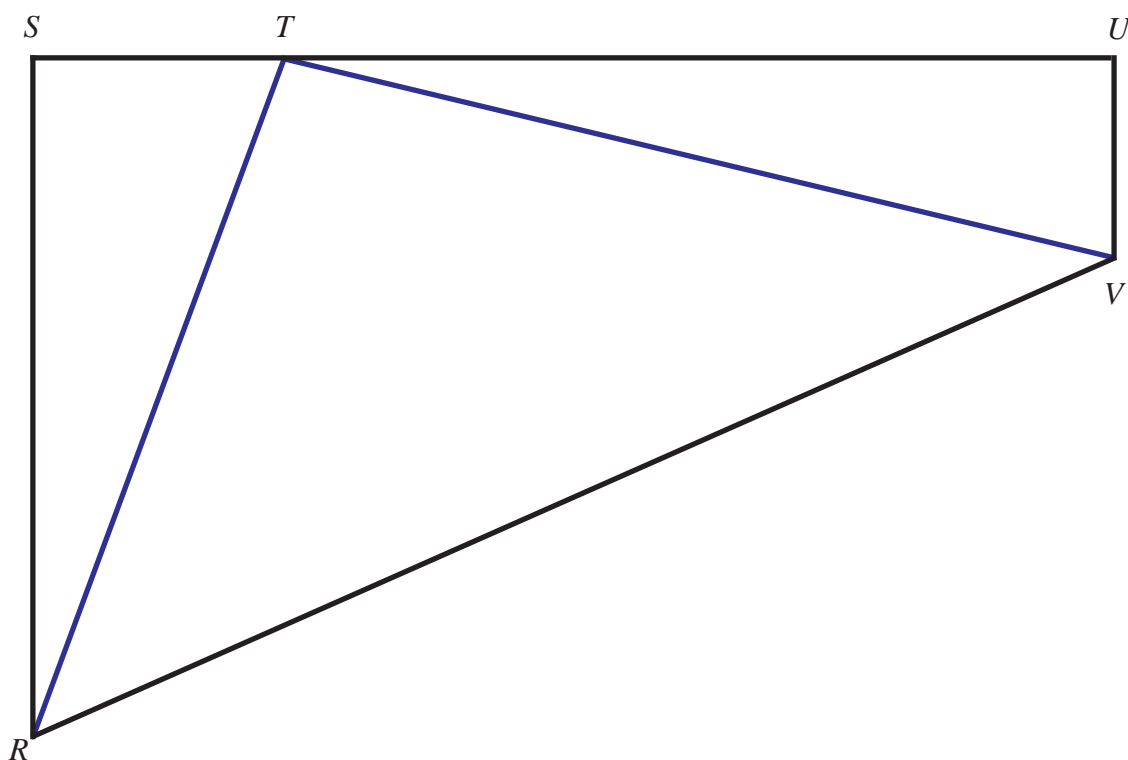
\* If your three lines don't cross at a point then you have a mistake somewhere or just haven't been accurate enough.

## Bisecting an Angle

- 1) Using ruler and compasses, bisect angle  $ABC$ .



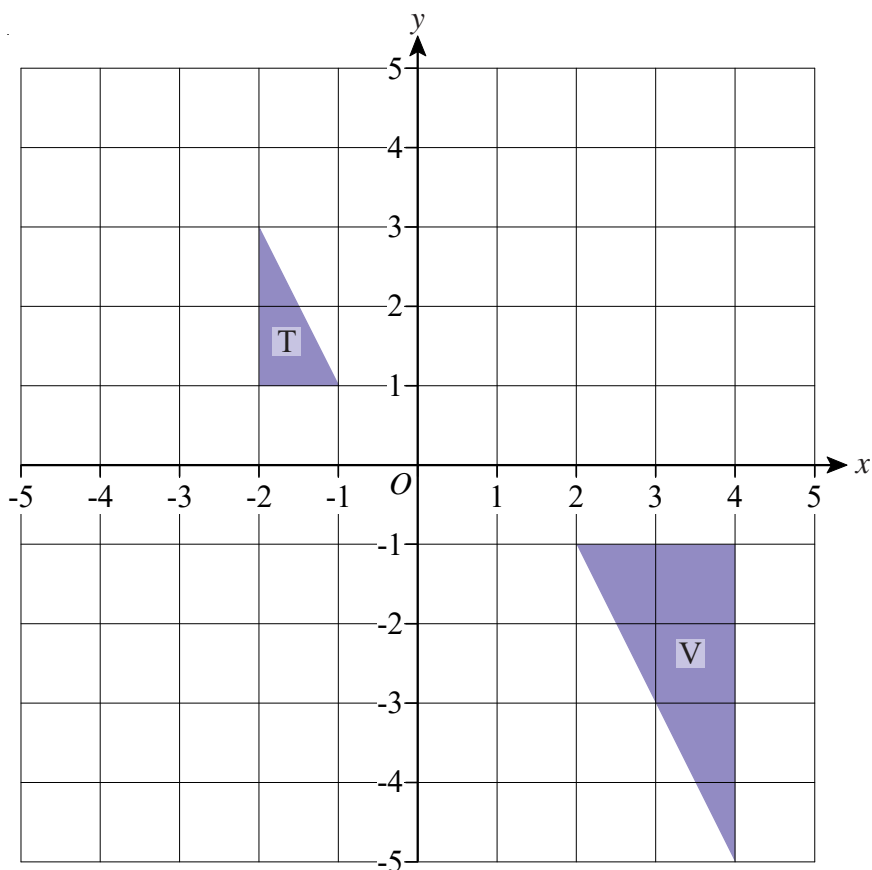
- 2) The diagram below shows the plan of a park.  
The border of the park is shown by the quadrilateral  $RSTUV$



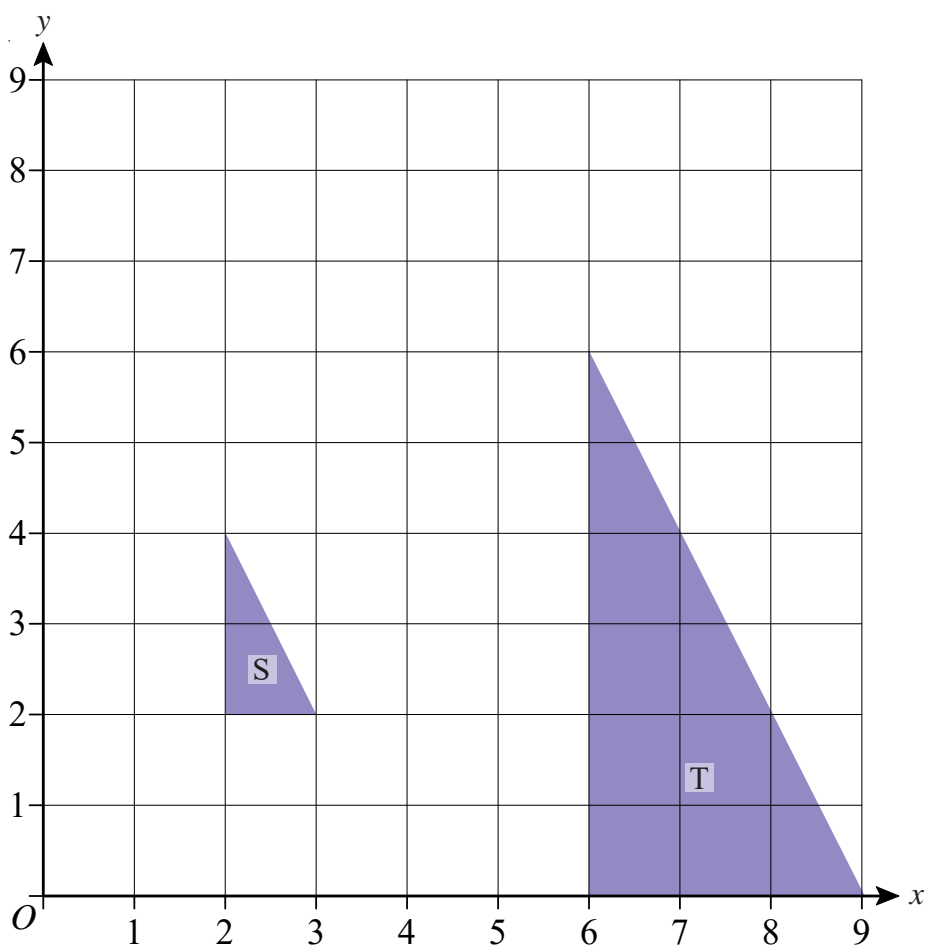
There are two paths in the park. One is labelled  $TR$  and the other  $TV$   
A man walks in the park so that he is always the same distance from both paths.  
Using ruler and compasses show exactly where the man can walk.

# Enlargements

- 1) a) Enlarge triangle T by scale factor 2 using point  $(-5, 2)$  as the centre of enlargement.  
Label your new triangle U.
- b) Enlarge triangle V by scale factor a half using the point  $(-2, -3)$  as the centre of enlargement.  
Label your new triangle W.

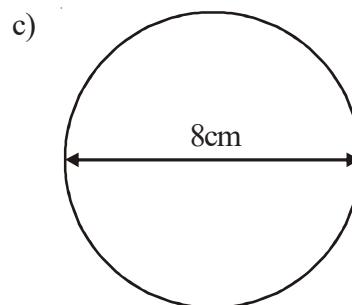
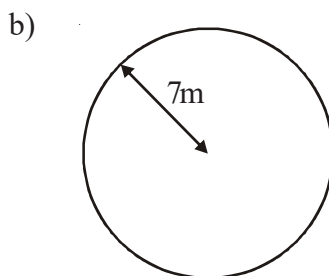
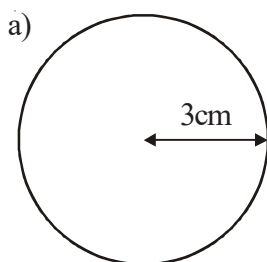


- 2) Describe fully the single transformation which maps triangle S to triangle T.

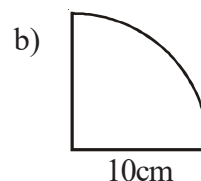
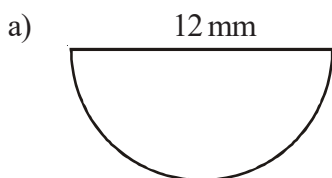




1) Find the areas of the following shapes.



2) Work out the areas of the following shapes.



3) The **radius** of the top of a circular table is 60 cm.  
The table also has a circular base with **diameter** 30 cm.

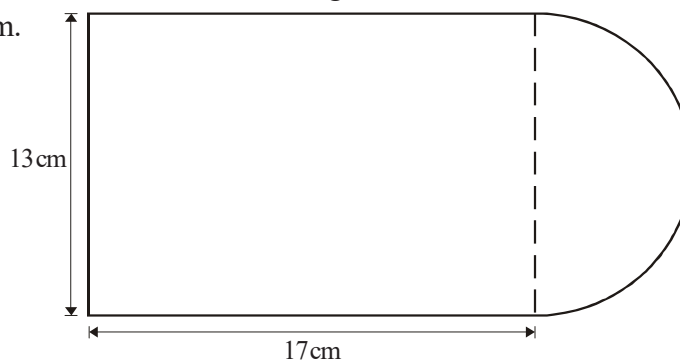
a) Work out the area of the top of the table.

b) Work out the area of the base of the table.



4) The diagram shows a shape, made from a semi-circle and a rectangle.  
The diameter of the semi-circle is 13 cm.  
The length of the rectangle is 17 cm.

Calculate the area of the shape.  
Give your answer correct to  
3 significant figures.

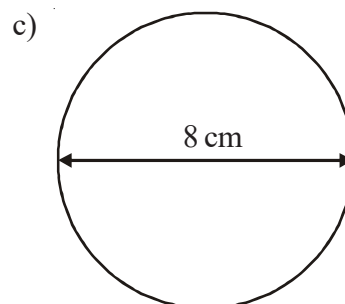
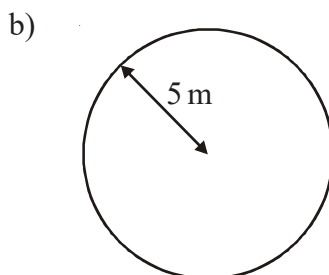
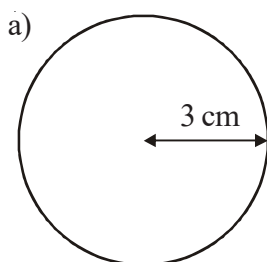




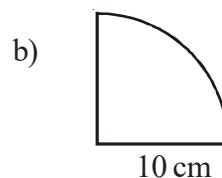
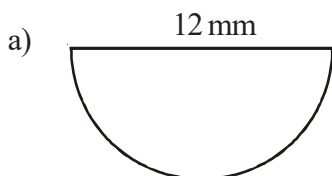
## Circumference of a Circle



- 1) Find the circumference of the following shapes.



- 2) Work out the perimeter of the following shapes.



- 3) The **radius** of the top of a circular table is 60 cm.  
The table also has a circular base with **diameter** 30 cm.

a) Work out the circumference of the top of the table.

Let  $\pi$  be 3.14

b) Work out the circumference of the base of the table.

Let  $\pi$  be 3.14

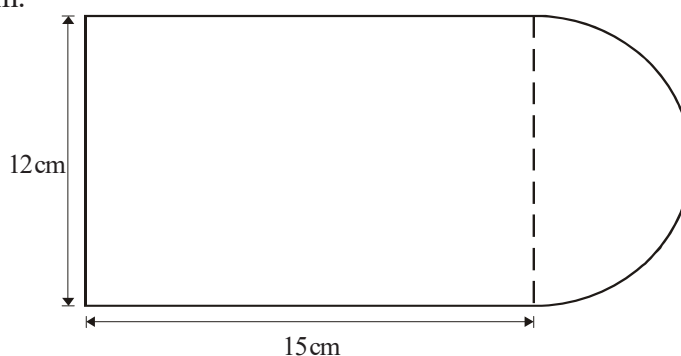


- 4) The diagram shows a shape, made from a semi-circle and a rectangle.  
The diameter of the semi-circle is 12 cm.  
The length of the rectangle is 15 cm.

Calculate the perimeter of the shape.

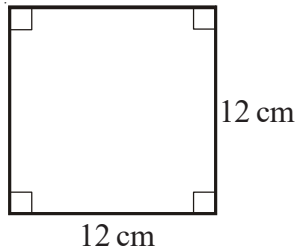
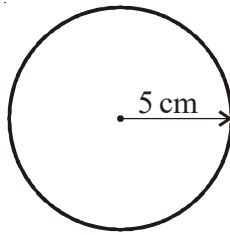
Give your answer correct to

3 significant figures.



## Area and Circumference of a Circle

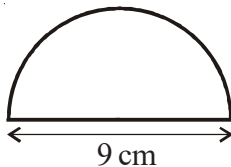
- 1) A circle has a radius of 5 cm.  
A square has sides of length 12 cm.



Work out the difference between the area of the circle and the area of the square if you take  $\pi$  to be 3.



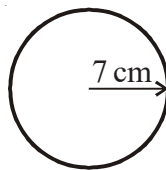
- 2) Here is a tile in the shape of a semi-circle.



The diameter of the semi-circle is 9 cm.  
Work out the perimeter of the tile.  
Give your answer correct to two decimal places.



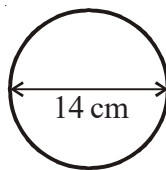
- 3) A circle has a radius of 7 cm.



Work out the area of the circle.  
Give your answer correct to three significant figures.



- 4) A circle has a diameter of 14 cm.

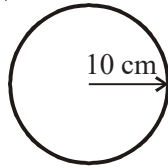


Work out the circumference of the circle.  
Give your answer correct to three significant figures.

## Area and Circumference of a Circle



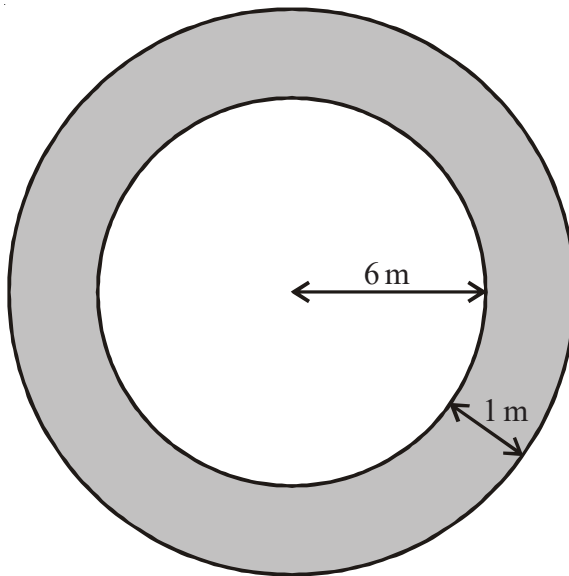
- 1) The radius of a circle is 10 cm.



Work out the area of this circle.



- 2) The diagram shows a circular pond with a path around it.



The pond has a radius of 6 m.

The path has a width of 1 m.

Work out the area of the path.

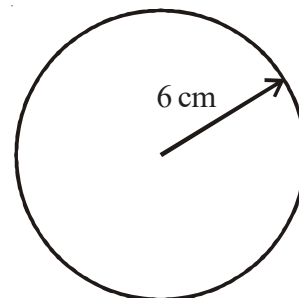
Give your answer correct to 3 significant figures.



- 3) The diagram shows a CD which has a radius of 6 cm.

a) Work out the circumference of the CD.

Give your answer correct to 3 significant figures.



CDs of this size are cut from rectangular sheets of plastic.

Each sheet is 1 metre long and 50 cm wide.

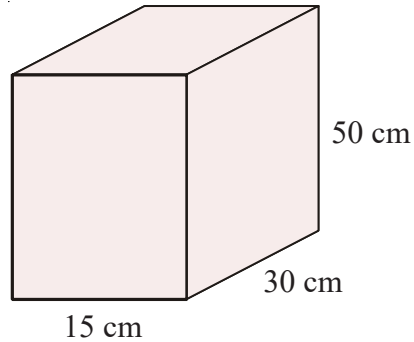
- b) Work out the greatest number of CDs which can be cut from one rectangular sheet.

## Volume of a Prism

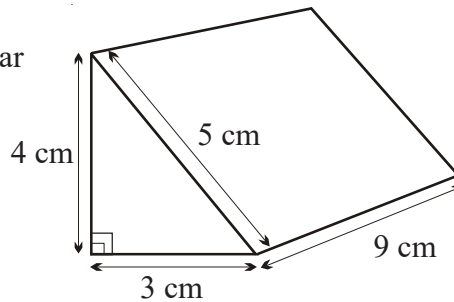


- 1) The diagram shows a cuboid.

Work out the volume of the cuboid.

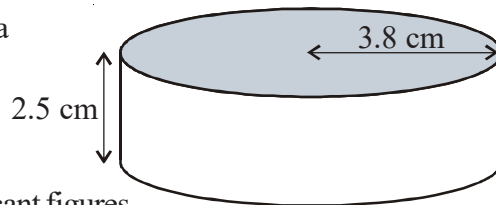


- 2) Calculate the volume of this triangular prism.



- 3) An ice hockey puck is in the shape of a cylinder with a radius of 3.8 cm and a thickness of 2.5 cm.

Work out the volume of the puck.  
Give your answer correct to 3 significant figures.

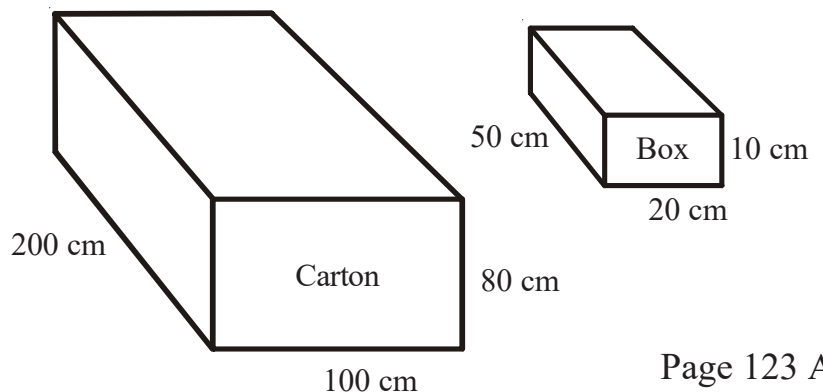


- 4) A cuboid has:      a volume of  $80\text{cm}^3$   
                             a length of 5 cm  
                             a width of 2 cm

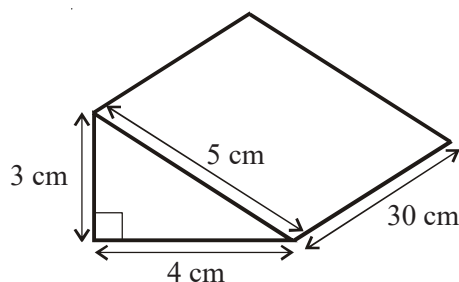
Work out the height of the cuboid.



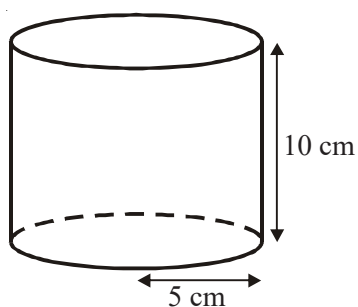
- 5) Work out the maximum number of boxes which can fit in the carton.



1) Work out the volume of the prism.



2)

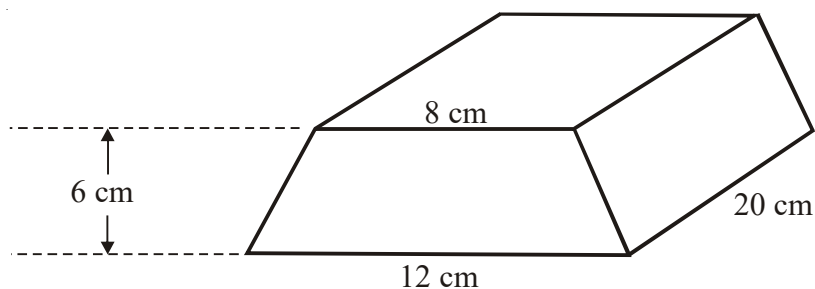


A solid cylinder has a radius of 5 cm and a height of 10 cm.

Work out the volume of the cylinder.

Give your answer correct to 3 significant figures.

3)



The diagram shows a solid prism made from metal.

The cross-section of the prism is a trapezium.

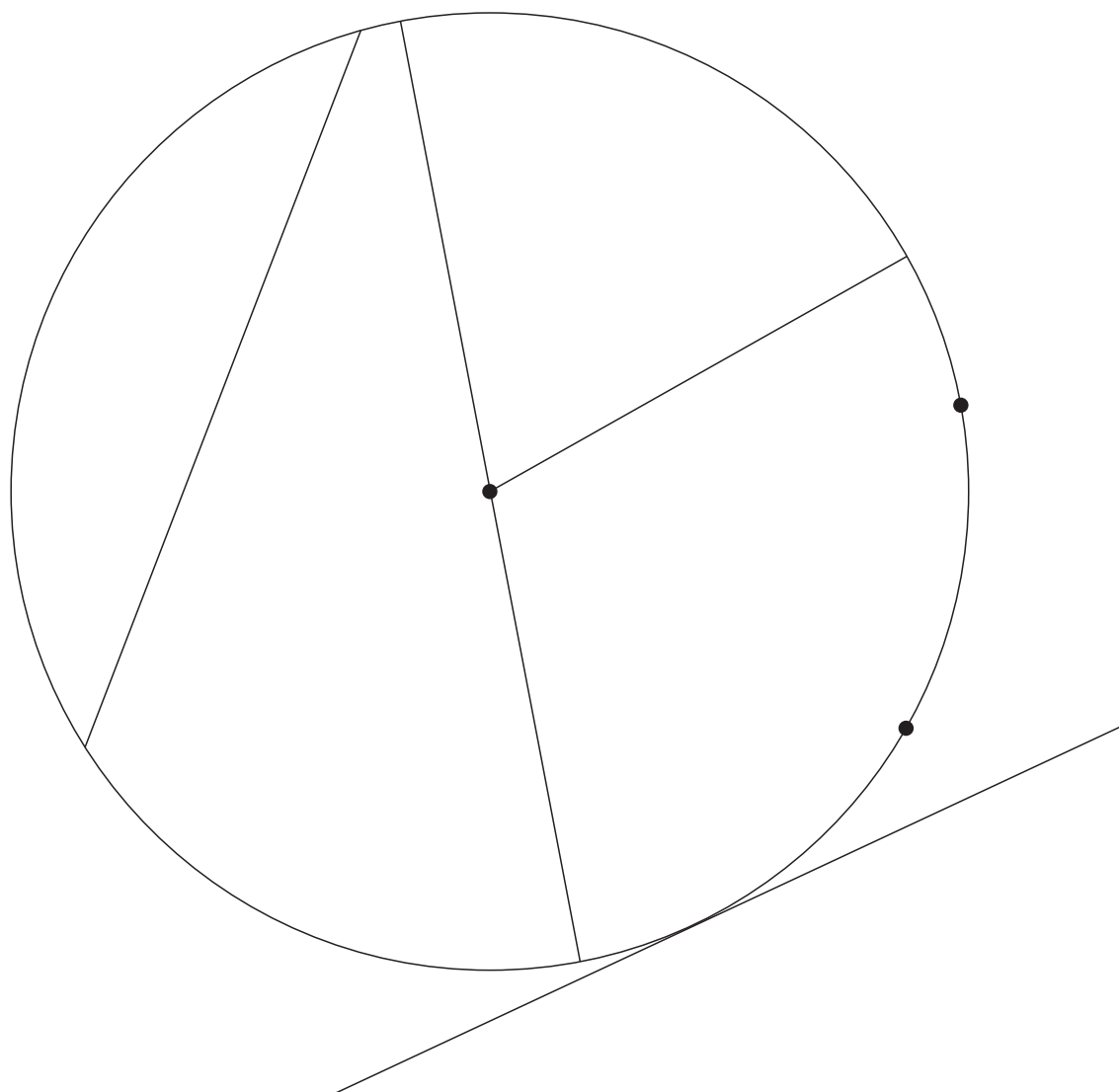
Find the volume of the prism.

You must state your units.

# Tangents, Arcs, Sectors and Segments

Tangent
Radius
Minor sector
Minor segment
Arc
Diameter
Chord
Circumference

On the diagram, mark on all of the words from the box in an appropriate place.



## Compound Units



- 1) Jane runs 200 metres in 21.4 seconds.

Work out Jane's average speed in metres per second.

Give your answer correct to 1 decimal place.



- 2) A car travels at a steady speed and takes five hours to travel 310 miles.

Work out the average speed of the car in miles per hour.



- 3) A plane flies 1440 miles at a speed of 240 mph.

How long does it take?



- 4) A marathon runner runs at 7.6 mph for three and a half hours.

How many miles has he run?



- 5) A car takes 15 minutes to travel 24 miles.

Find its speed in **mph**.



- 6) A cyclist takes 10 minutes to travel 2.4 miles.

Calculate the average speed in mph.



- 7) Tony went on holiday to Miami.  
He travelled from London by plane.

The distance from London to Miami is 7120 km.

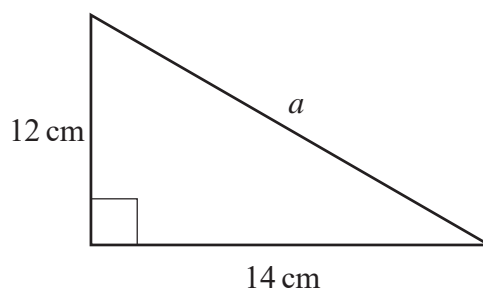
The plane journey took 8 hours.

Calculate the average speed of the plane.

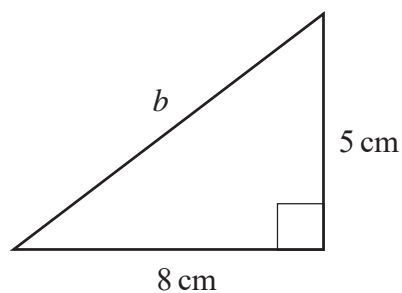
## Pythagoras' Theorem



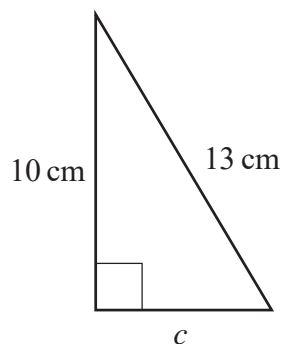
- 1) Find the length of side  $a$ .  
Give your answer to 1 decimal place.



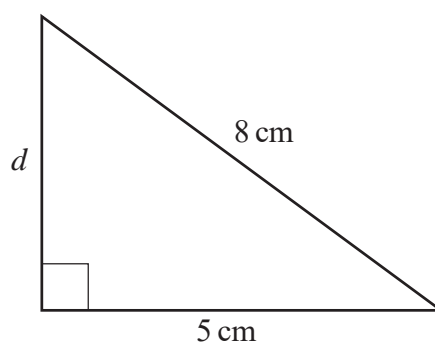
- 2) Find the length of side  $b$ .  
Give your answer to 1 decimal place.



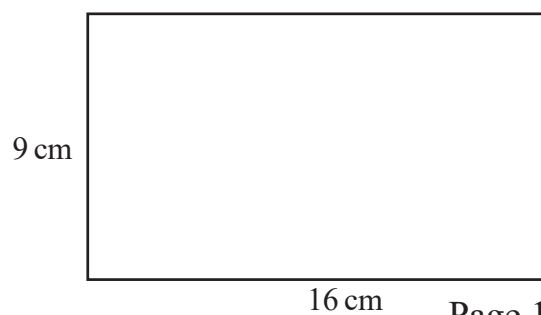
- 3) Find the length of side  $c$ .  
Give your answer to 1 decimal place.



- 4) Find the length of side  $d$ .  
Give your answer to 1 decimal place.



- 5) Find the length of the diagonal of this rectangle.  
Give your answer to 1 decimal place.

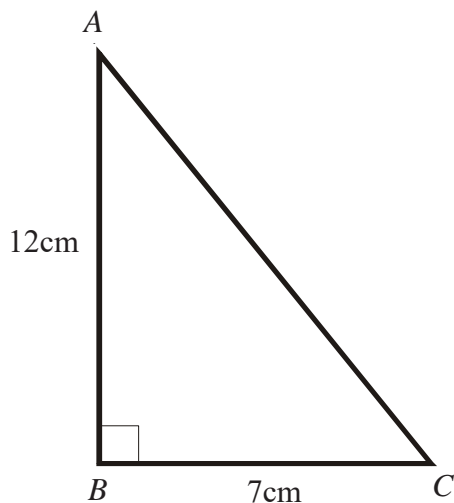




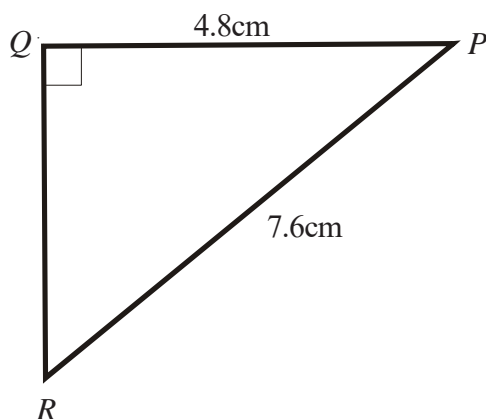
## Pythagoras' Theorem



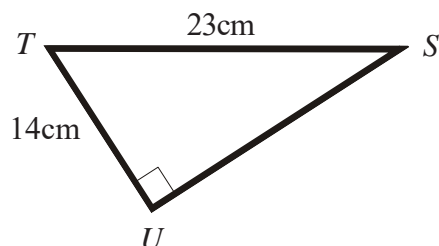
- 1) Find the length of side  $AC$ .  
Give your answer to 1 decimal place.



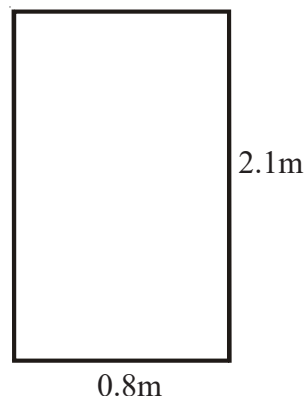
- 2) Find the length of side  $QR$ .  
Give your answer to 1 decimal place.



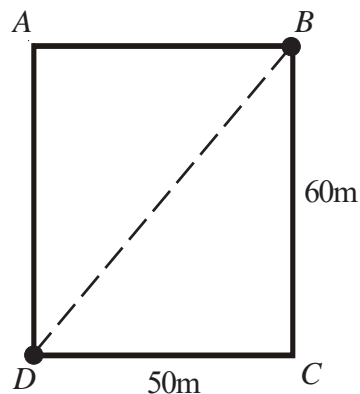
- 3) Find the length of side  $SU$ .  
Give your answer to 1 decimal place.



- 4) Below is a picture of a doorway.  
Find the size of the diagonal of the doorway.  
Give your answer to 1 decimal place.



- 5) In the sketch of the rectangular field, below, James wants to walk from  $B$  to  $D$ .



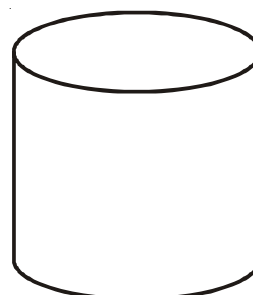
Which of the following routes is shorter and by how much?

From  $B$  to  $C$  to  $D$  or straight across the field from  $B$  to  $D$ .

Give your answer to the nearest metre.

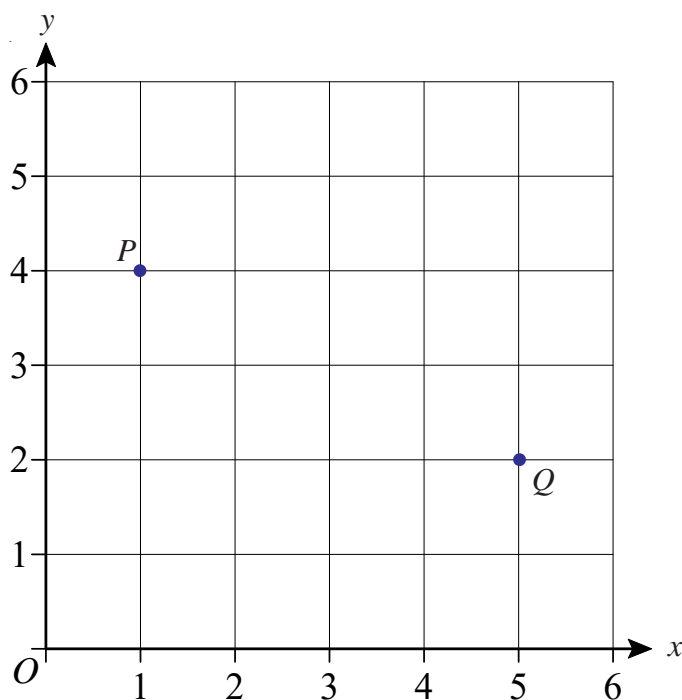


- 6) Fiona keeps her pencils in a cylindrical beaker as shown below.  
The beaker has a diameter of 8cm and a height of 17cm.  
Will a pencil of length 19cm fit in the beaker without poking out of the top?  
All workings must be shown.

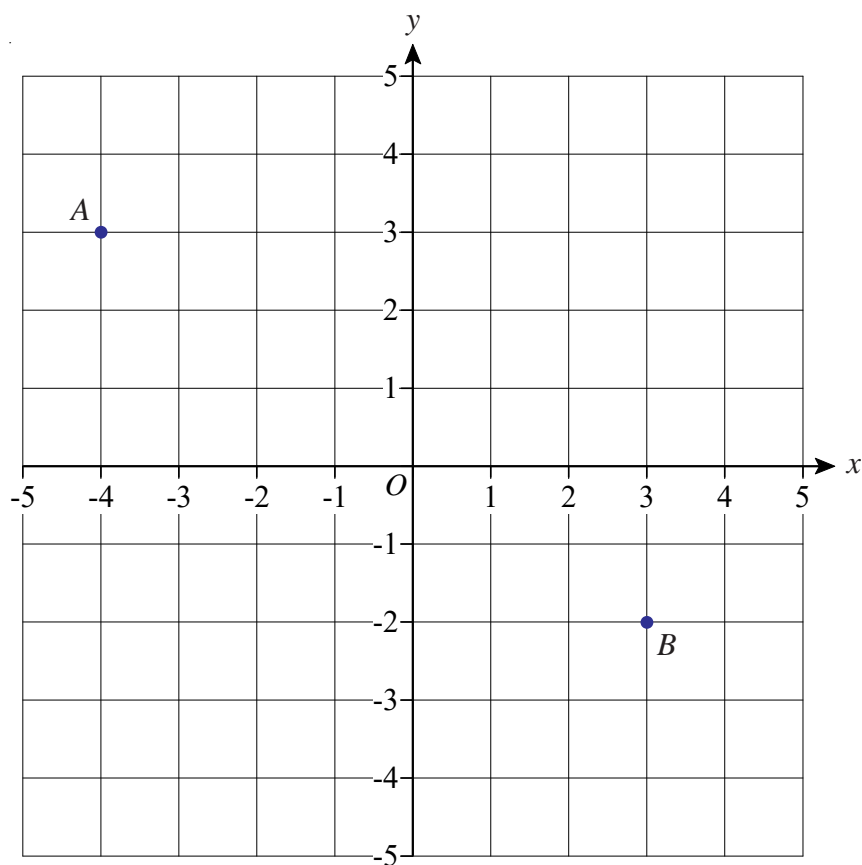




- 1) Points  $P$  and  $Q$  have coordinates  $(1, 4)$  and  $(5, 2)$ .  
Calculate the shortest distance between  $P$  and  $Q$ .  
Give your answer correct to 1 decimal place.

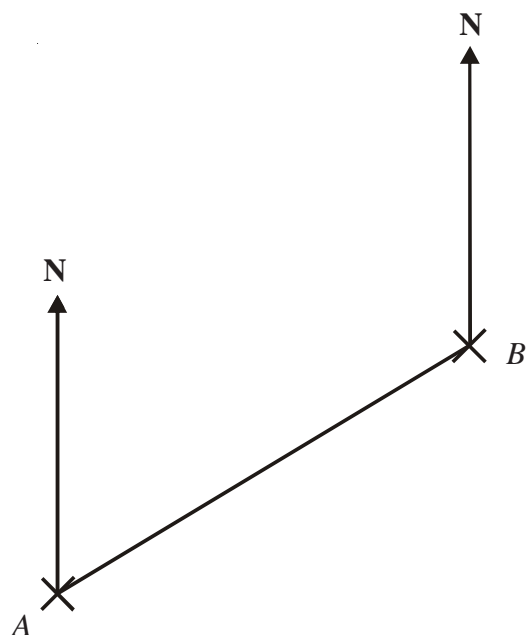


- 2) Points  $A$  and  $B$  have coordinates  $(-4, 3)$  and  $(3, -2)$ .  
Calculate the shortest distance between  $A$  and  $B$ .  
Give your answer correct to 1 decimal place.



## Bearings

- 1) The diagram shows the position of two telephone masts,  $A$  and  $B$ , on a map.

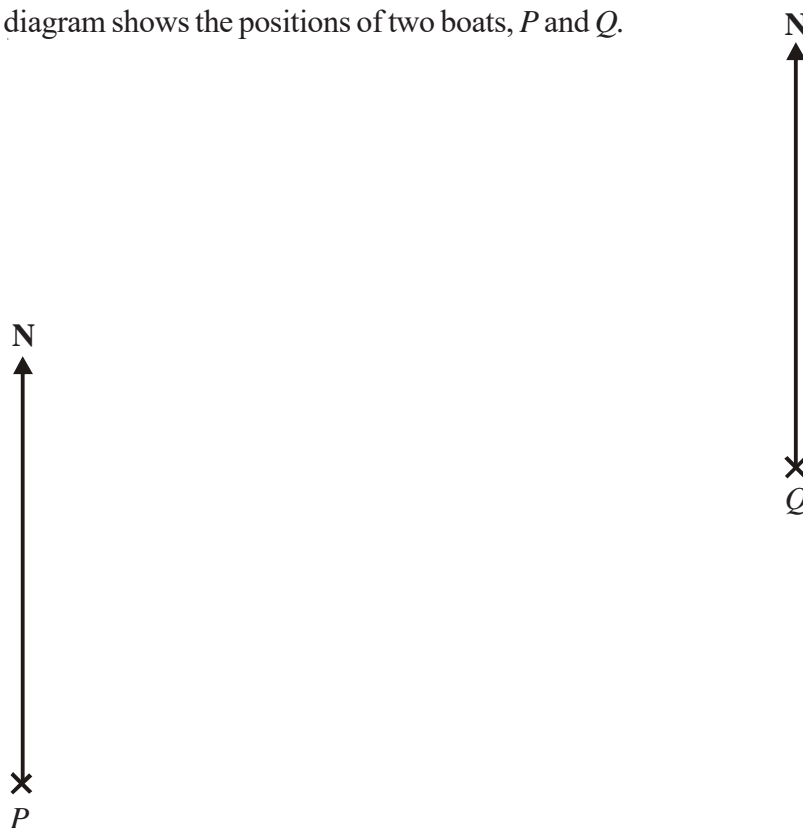


- a) Measure the bearing of  $B$  from  $A$ .

Another mast  $C$  is on a bearing of  $160^\circ$  from  $B$ .  
On the map,  $C$  is 4 cm from  $B$ .

- b) Mark the position of  $C$  with a cross and label it  $C$ .

- 2) The diagram shows the positions of two boats,  $P$  and  $Q$ .



The bearing of a boat  $R$  from boat  $P$  is  $050^\circ$

The bearing of boat  $R$  from boat  $Q$  is  $320^\circ$

In the space above, draw an accurate diagram to show the position of boat  $R$ .  
Mark the position of boat  $R$  with a cross ( $\times$ ). Label it  $R$ .

## Bearings

- 1) School  $B$  is due east of school  $A$ .  
 $C$  is another school.  
 The bearing of  $C$  from  $A$  is  $065^\circ$ .  
 The bearing of  $C$  from  $B$  is  $313^\circ$ .

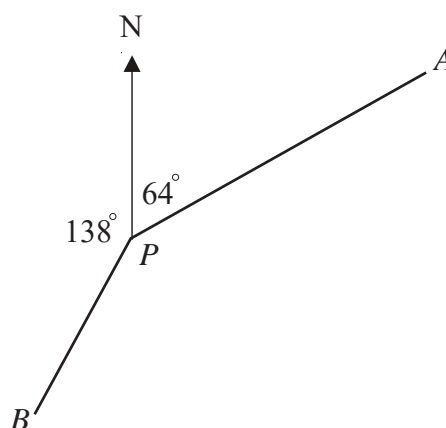
Complete the scale drawing below.  
 Mark with a cross the position of  $C$ .



- 2) In the diagram, point  $A$  marks the position of Middlewich.  
 The position of Middlemarch is to be marked on the diagram as point  $B$ .  
 On the diagram, mark with a cross the position of  $B$  given that:  
 $B$  is on a bearing of  $320^\circ$  from  $A$  and  
 $B$  is 5 cm from  $A$



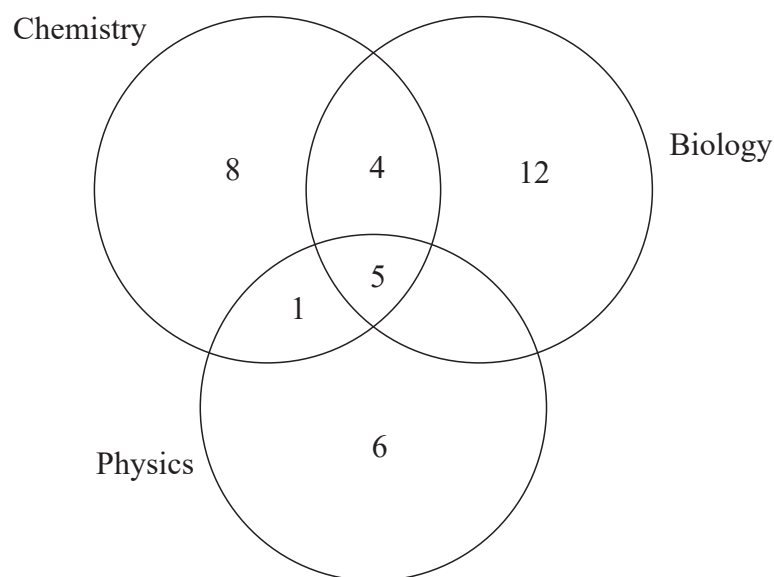
- 3) **Work out** the bearing of  
 a)  $B$  from  $P$   
 b)  $P$  from  $A$



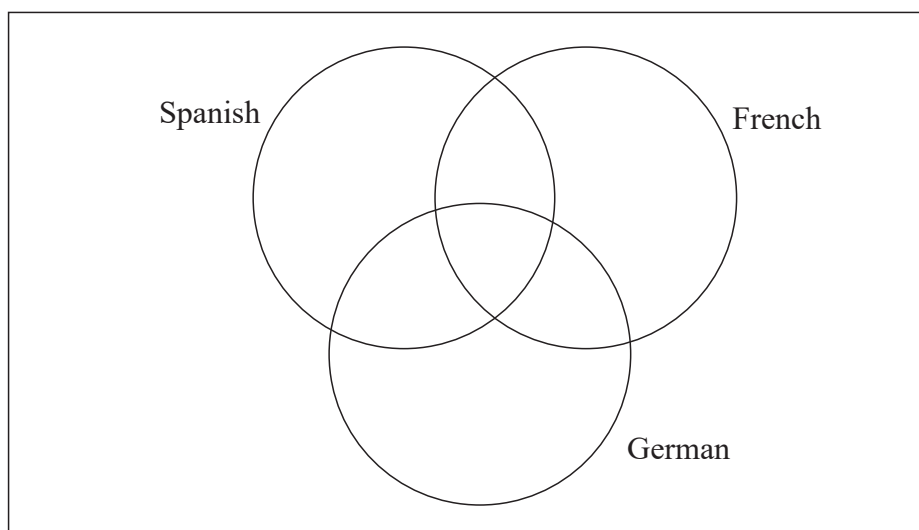
*Diagram NOT  
accurately drawn.*

## Venn Diagrams

- 1) The Venn diagram shows the number of students studying one or more of the sciences Chemistry, Biology and Physics.



- a) How many students are represented in this Venn diagram?
- b) How many students are studying exactly two sciences?
- c) What is the probability that a student chosen at random is not studying Physics?
- 2) There are 31 student who study languages.  
 All 31 study at least one of Spanish, French or German.  
 4 study all three languages.  
 9 study Spanish and French.  
 7 study French and German.  
 6 study Spanish and German.  
 7 study only French and 5 study only German.  
 Complete the Venn diagram to show this information.

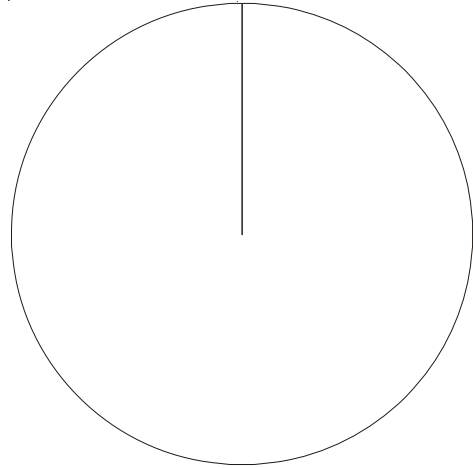


## Pie Charts

- 1) Patrick asked some of his colleagues which was their favourite holiday destination. The table shows the results.

City	Frequency
Alicante	8
Paris	7
Ibiza	15
St Lucia	1
Biarritz	9

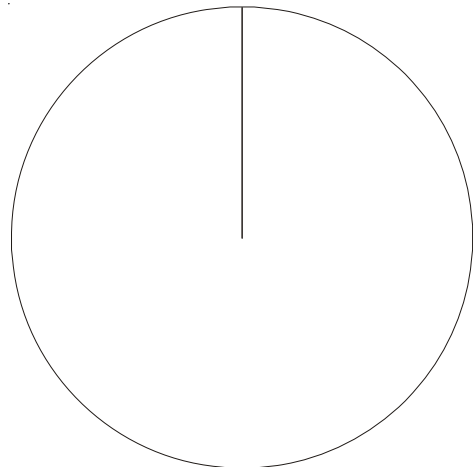
Draw a pie chart to illustrate the information.



- 2) Brian asked 60 people which region their favourite rugby team came from. The table shows the results.

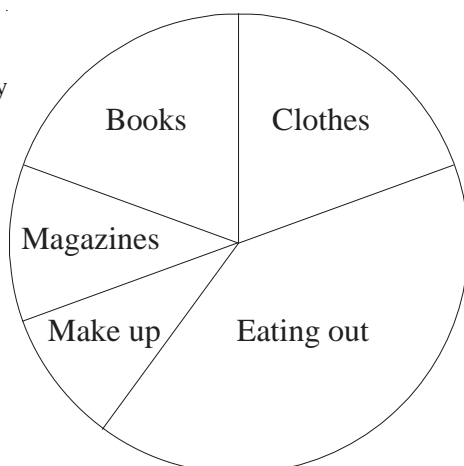
Region	Frequency
Southern England	9
London	23
Midlands	16
Northern England	12
Total	60

Draw a pie chart to illustrate the information.



- 3) Sophie represents her monthly expenses using a pie chart

Diagram accurately drawn



Numbers from her table have been rubbed out by mistake.

Use the pie chart to complete the table.

		Angle
Clothes	£35	
Eating out		
Make up	£17	34°
Magazines		
Books		
<b>Total</b>	<b>£180</b>	



- 1) Tom carried out a survey of the number of school dinners 34 students had in one week. The table shows this information.

Number of school dinners	Frequency	
0	0	
1	7	
2	14	
3	7	
4	4	
5	2	

Calculate the mean number of school dinners.  
Give your answer to 1 decimal place.



- 2) The number of pens in each pupil's pencil case in a classroom has been counted. The results are displayed in a table.

Number of pens	Number of pupils
0	4
1	6
2	7
3	5
4	3
5	1

- Work out the total number of pens in the classroom.
- Write down the modal number of pens in a pencil case.
- Work out the mean number of pens in a pencil case.
- Work out the range of the number of pens in a pencil case.



- 3) Thomas is analysing the local football team. He records the number of goals scored in each football match in the past twelve months.

Thomas said that the mode is 7  
Thomas is wrong.

- Explain why.
- Calculate the mean number of goals scored.

Goals scored	Frequency
0	7
1	5
2	3
3	6
4	2
5	1
6	1

1) Find the value of:

a)  $2^{-3}$

b)  $3^{-2}$

c)  $5^{-1}$

d)  $10^{-4}$

2) Find the value of:

a)  $2^{-3} \times 4^{-1}$

b)  $10^{-2} \times 2^{-4}$

c)  $5 \times 5^{-3}$

d)  $8 \times 2^{-3}$

3) Write these numbers in order of size.

Start with the smallest.

$3^2$   $3^{-1}$   $0.3$   $3^0$   $3^{-2}$   $-3$

4) If  $2^x = \frac{1}{64}$ , find the value of  $x$ .



## Percentage Change



- 1) A car dealer is comparing his sales over the past two years.

In 2006, he sold 175 cars.

In 2007, he sold 196 cars.

Work out the percentage increase in the number of cars sold.



- 2) In September 2005, the number of pupils attending MathsWatch College was 1352.

In September 2006, the number of pupils attending MathsWatch College was 1014.

Work out the percentage decrease in the number of pupils attending MathsWatch College.



- 3) The usual price of a shirt is £32.50

In a sale, the shirt is reduced to £29.25

What is the percentage reduction?



- 4) Olivia opened an account with £750 at the MathsWatch Bank.

After one year, the bank paid her interest.

She then had £795 in her account.

Work out, as a percentage, MathsWatch Bank's interest rate.



- 5) Keith buys a house for £270 000 and sells it two years later for £300 000.

What is his percentage profit?

Give your answer to 2 significant figures.



- 6) Shelley bought some items at a car boot sale and then sold them on ebay.

Work out the percentage profit or loss she made on each of these items.

a) Trainers bought for £15, sold for £20

b) DVD recorder bought for £42, sold for £60.90

c) Gold necklace bought for £90, sold for £78.30

d) A DVD collection bought for £120, sold for £81.60

## Reverse Percentage Problems



- 1) In a sale, normal prices are reduced by 20%.

The sale price of a shirt is £26

Calculate the normal price of the shirt.



- 2) A car dealer offers a discount of 15% off the normal price of a car for cash.

Emma pays £6120 cash for a car.

Calculate the normal price of the car.



- 3) In a sale, normal prices are reduced by 13%.

The sale price of a DVD recorder is £108.75

Calculate the normal price of the DVD recorder.



- 4) A salesman gets a basic wage of £160 per week plus a commission of 30% of the sales he makes that week.

In one week his total wage was £640

Work out the value of the sales he made that week.



- 5) Jason opened an account at MathsWatch Bank.

MathsWatch Bank's interest rate was 4%.

After one year, the bank paid him interest.

The total amount in his account was then £1976

Work out the amount with which Jason opened his account.



- 6) Jonathan's weekly pay this year is £960.

This is 20% more than his weekly pay last year.

Tess says "This means Jonathan's weekly pay last year was £768".

Tess is wrong.

a) Explain why

b) Work out Jonathan's weekly pay last year.



- 7) The price of all rail season tickets to London increased by 4%.

a) The price of a rail season ticket from Oxford to London increased by £122.40

Work out the price before this increase.

b) After the increase, the price of a rail season ticket from Newport to London was £2932.80

Work out the price before this increase.

## Compound Interest and Depreciation



- 1) Henry places £6000 in an account which pays 4.6% compound interest each year.

Calculate the amount in his account after 2 years.



- 2) Sarah puts £8600 in a bank. The bank pays compound interest of 3.8% per year.

Calculate the amount Sarah has in her account after 4 years.



- 3) Mary deposits £10000 in an account which pays 5.6% compound interest per year.

How much will Mary have in her account after 5 years?



- 4) Susan places £7900 in an account which pays 2.4% compound interest per year.

How much interest does she earn in 3 years?



- 5) Harry puts money into an account which pays 6% compound interest per year.

If he puts £23000 in the account for 5 years how much interest will he earn altogether?



- 
- 6) Laura buys a new car for £14600.

The annual rate of depreciation is 23%.

How much is the car worth after 3 years?



- 7) The rate of depreciation of a particular brand of computer is 65% per year. If the cost of the computer when new is £650 how much is it worth after 2 years?



- 8) Sharon pays £3500 for a secondhand car.

The annual rate of depreciation of the car is 24%

How much will it be worth four years after she has bought it?



- 
- 9) Dave places £17000 in an account which pays 4% compound interest per year.

How many years will it take before he has £19122.69 in the bank?



- 10) A new motorbike costs £8900.

The annual rate of depreciation is 18% per year.

After how many years will it be worth £2705.66?

- 1) A forest has 1260 trees.  
The trees are maple, beech or oak.  
A fifth of the trees are maple and the number of maple trees is 3 times the number of beech trees.  
The rest of the trees are oak.

$$\text{number of oak} : \text{number of beech} = n : 1$$

Work out the value of  $n$ .

You must show how you get your answer.

- 2)  $a : b$  is  $2 : 5$  and  $b : c$  is  $3 : 8$

Work out  $a : c$

Give your answer in its simplest form.

- 3) Given that  $\frac{x}{y} = \frac{1}{3}$  and  $\frac{y}{z} = \frac{4}{5}$

find  $x : z$

- 4)  $p : q = 1 : 5$

Circle the correct equation.

$$q = \frac{p}{5}$$

$$q = p + 4$$

$$q = p - 4$$

$$q = 5p$$

- 5)  $a : b = 7 : 2$

Form an equation.

- 6)  $x : y = \frac{1}{3} : \frac{2}{5}$

What is  $x$  as a fraction of  $y$ ?

Circle your answer.

$$\frac{1}{5}$$

$$\frac{5}{6}$$

$$\frac{3}{8}$$

$$\frac{6}{5}$$

1) Meg says,

“The sum of three prime numbers is always odd.”

Write an example to show that Meg is incorrect.

2) Mike says.

“If you cube a prime number, the result will always be odd.”

Give an example to show that Mike is wrong.

3) Explain why an odd number plus another odd number plus an even number is always even.

4)  $P$  is an odd number.

$Q$  is an even number.

Explain why  $2P + 2Q - 1$  is always odd.

5)  $P$  is an odd number.

$Q$  is an even number.

Tim says that  $P + Q$  is always a prime number.

Explain why Tim is wrong.

## Factorising and Solving Quadratics

1) Factorise and solve the following equations:

a)  $x^2 + 5x + 6 = 0$

b)  $x^2 + 9x + 20 = 0$

c)  $x^2 + x - 6 = 0$

d)  $x^2 + 5x - 24 = 0$

e)  $x^2 - 6x + 8 = 0$

f)  $x^2 - 3x - 28 = 0$

g)  $2x^2 + 7x + 3 = 0$

h)  $6x^2 + 11x + 3 = 0$

i)  $3x^2 + 13x - 10 = 0$

j)  $3x^2 - 34x + 63 = 0$

2) Lucy said that -1 is the only solution of  $x$  that satisfies the equation

$$x^2 + 2x + 1 = 0$$

Was Lucy correct?

Show working to justify your answer

3) Ben said that -5 is the only solution of  $x$  that satisfies the equation

$$x^2 + 10x + 25 = 0$$

Was Ben correct?

Show working to justify your answer

## The Difference of Two Squares

1) Factorise

a)  $x^2 - 16$

c)  $y^2 - 9$

e)  $x^2 - \frac{1}{4}$

b)  $a^2 - b^2$

d)  $x^2 - 1$

f)  $x^2 - \frac{1}{9}$

2) Factorise

a)  $x^2 - 4y^2$

c)  $9x^2 - 16y^2$

e)  $4x^2 - 25y^2$

b)  $9a^2 - b^2$

d)  $\frac{1}{4}x^2 - y^2$

f)  $x^2 - \frac{1}{9}y^2$

3) Simplify

a)  $\frac{y^2 - 4}{y + 2} \times \frac{5}{y + 5}$

b)  $\frac{3}{2x + 1} \times \frac{4x^2 - 1}{x - 2}$

c)  $\frac{12x^2 + 8x}{9x^2 - 4}$

d)  $\frac{25a^2 - 16b^2}{10ab - 8b^2}$

4) Solve

a)  $4x^2 - 16 = 0$

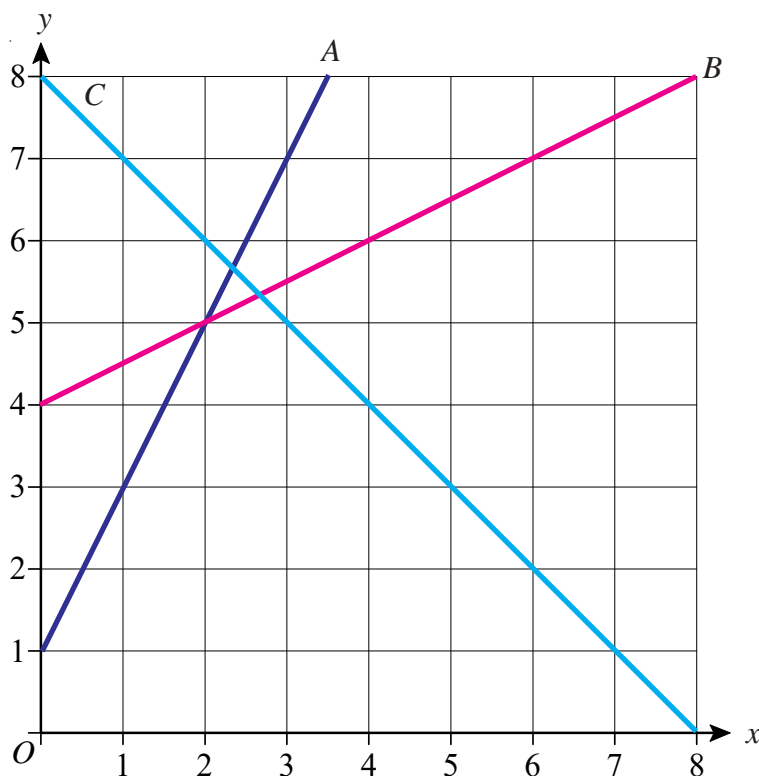
c)  $49x^2 = 121$

b)  $25x^2 = 1$

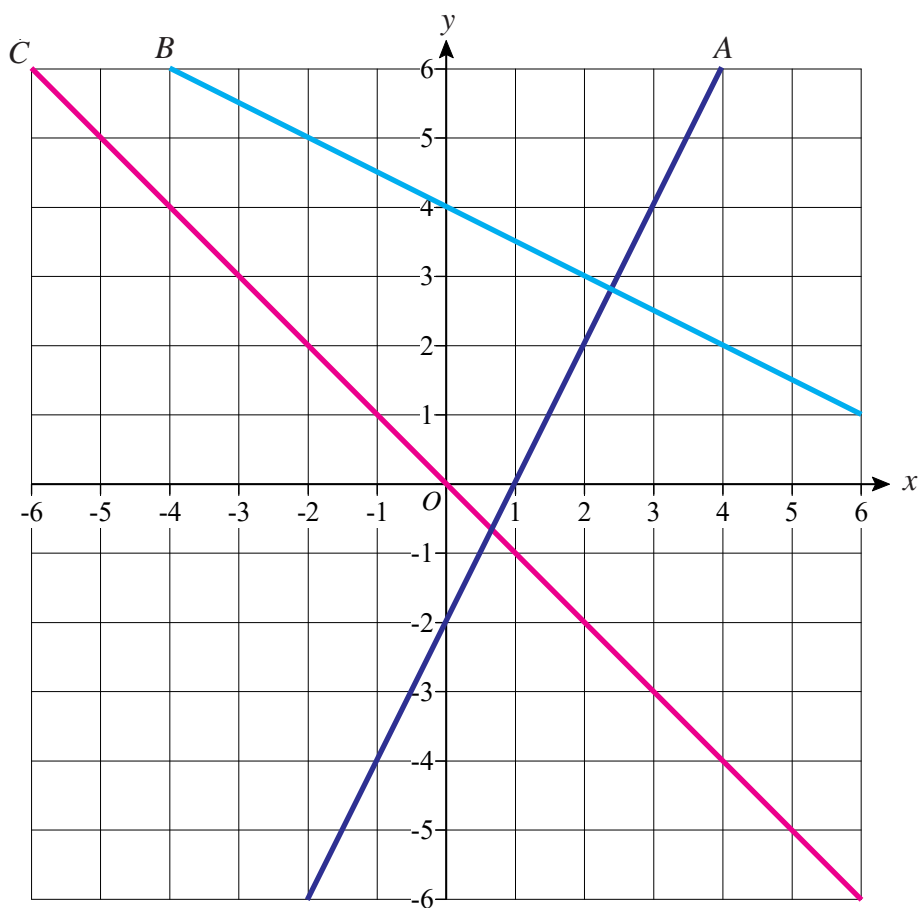
d)  $9x^2 - 9 = 7$

# Finding the Equation of a Straight Line

- 1) Find the equations of lines  $A$ ,  $B$  and  $C$  on the axes below



- 2) Find the equations of lines  $A$ ,  $B$  and  $C$  on the axes below

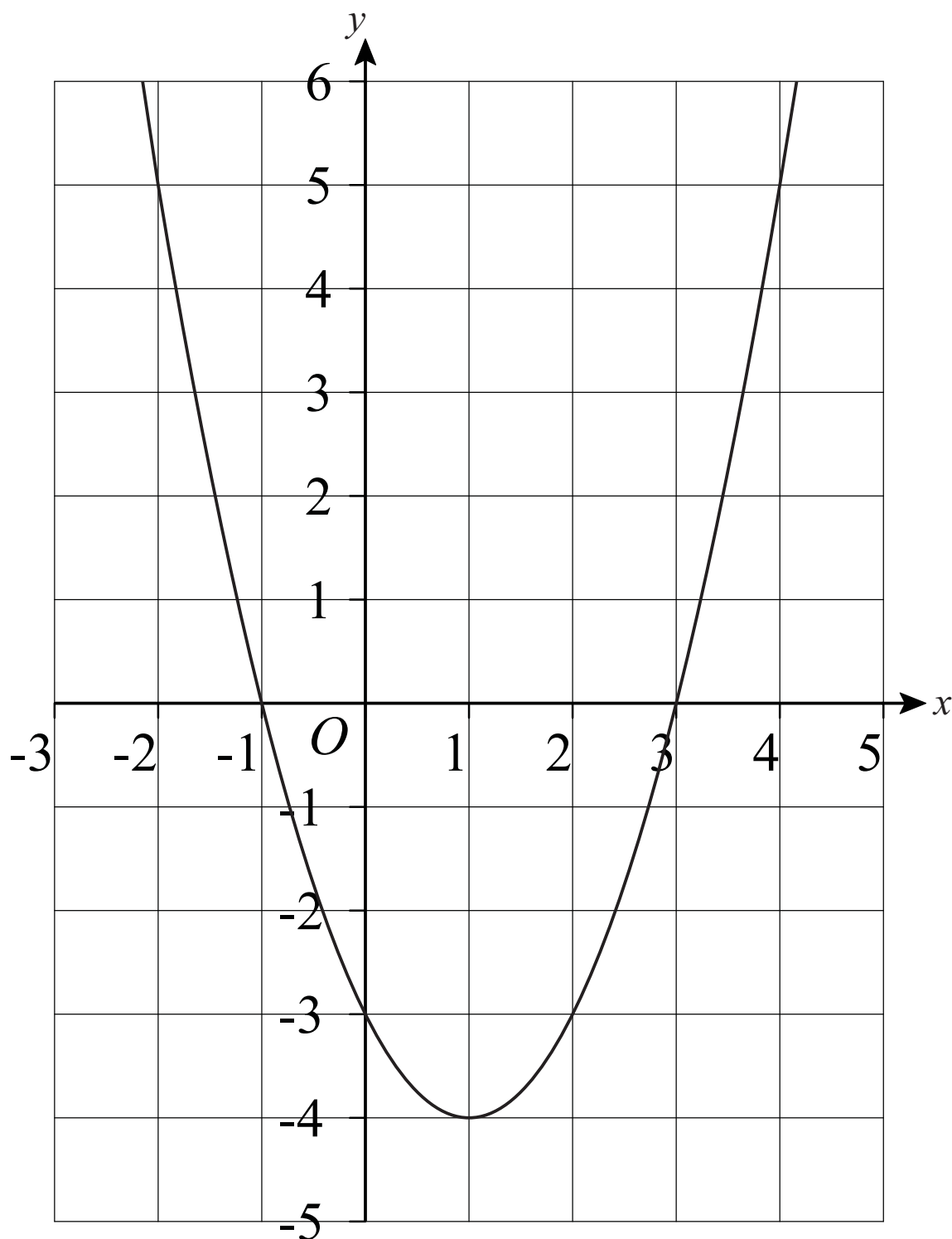




- 1) The graph of  $y = x^2 - 2x - 3$  is shown.

Write down the coordinates of:

- a) The turning point of the curve.
- b) The roots of the equation  $x^2 - 2x - 3 = 0$
- c) The intersection of the curve with the  $y$ -axis.



## Simultaneous Equations Algebraically

1) Solve

$$4x + 3y = 6$$

$$5x - 3y = 21$$

2) Solve

$$4x + 3y = 19$$

$$3x - 5y = 7$$

3) Solve

$$3x + 5y = 13$$

$$2x + 3y = 8$$



4) Solve

$$x + 4y = 5$$

$$4x - 2y = 11$$



5) Solve

$$2a + b = 3$$

$$4a - 5b = 20$$

6) Solve

$$5x + 3y = 4$$

$$3x + 4y = 9$$



7) Solve

$$6x - 2y = 13$$

$$2x + 3y = -3$$



8) Solve

$$3a - 2b = 14$$

$$4a + 3b = 13$$



9) Solve

$$5x + 4y = 5$$

$$2x + 7y = 29$$



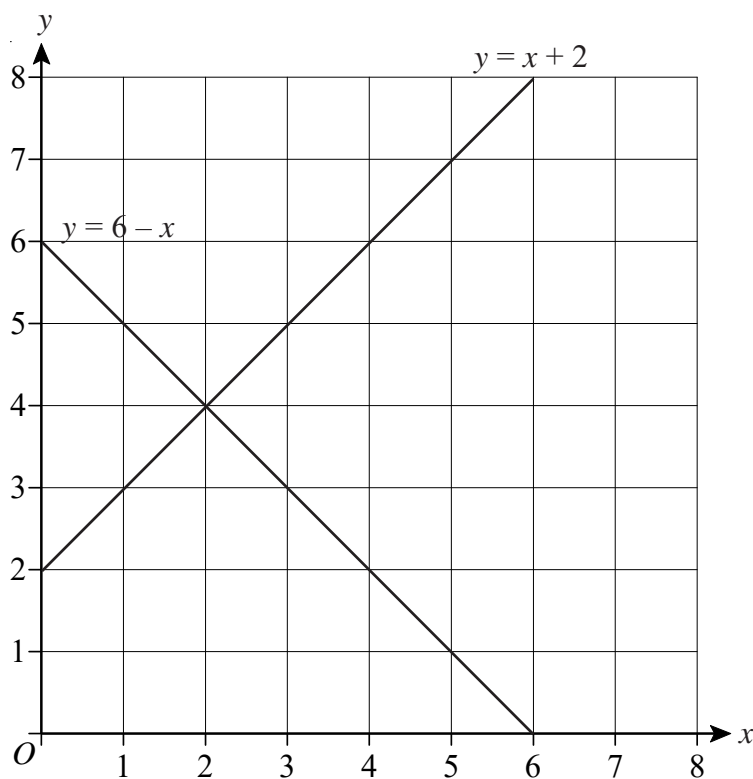
10) Solve

$$6x - 4y = 39$$

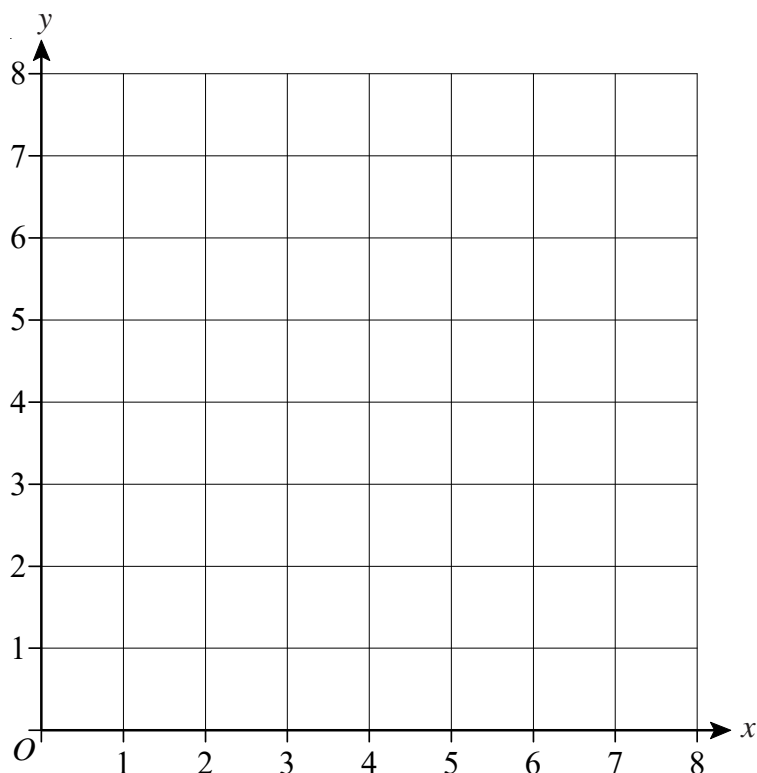
$$2x + y = 6$$

## Simultaneous Equations Graphically

- 1) On the axes below, the graphs of  $y = x + 2$  and  $y = 6 - x$  have been drawn.  
Use the graphs to solve the simultaneous equations  $y = x + 2$  and  $y = 6 - x$



- 2) On the axes below draw the graphs of  $y = 2x + 1$  and  $y = 7 - x$   
Use your graphs to solve the simultaneous equations  $y = 2x + 1$  and  $y = 7 - x$



## Solving Linear Inequalities

1) Solve

a)  $3x - 1 > 5$

b)  $7y + 2 \leq 30$

c)  $\frac{x}{2} - 3 \geq 2$

d)  $5 + 2x > 7$

e)  $8 < 5p - 2$

f)  $\frac{y}{3} + 5 \geq 3$

g)  $\frac{2x}{3} - 5 \geq -3$

h)  $6x - 5 > 2x + 3$

i)  $3p - 9 < 6 - 2p$

j)  $5 - 3y < 2y - 10$

2) a) Solve the inequality

$$2z + 2 \geq 7$$

b) Write down the smallest **integer** value of  $z$  which satisfies the inequality

$$2z + 2 \geq 7$$

3)  $5x + 2y < 10$

$x$  and  $y$  are both integers.

Write down two possible pairs of values that satisfy this inequality.

$x = \dots\dots\dots$ ,  $y = \dots\dots\dots$

and

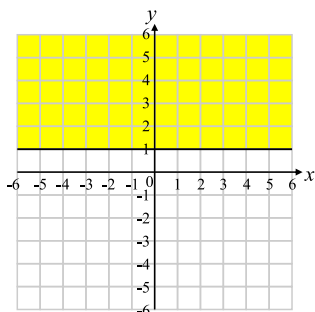
$x = \dots\dots\dots$ ,  $y = \dots\dots\dots$

- 1) Solve the inequality  $6x - 3 < 9$
- 2) Solve  $4x + 1 = 2x + 12$
- 3) a) Solve the inequality  $3t + 1 < t + 13$   
b) If  $2t^2 = 72$  find a value of  $t$
- 4) Solve  $3(x + 2) = 8$
- 5) Solve the inequality  $6y \geq y + 10$
- 6) Solve  $4(2x - 3) = 5x + 7$
- 7)  $h = 5t^2 + 3$   
Work out the value of  $t$  when  $h = 48$
- 8) Solve  $3(2p - 4) = 2p + 12$
- 9) Solve the equation  $4x + 1 = 19$
- 10) Solve  $\frac{29 - x}{3} = x + 5$
- 11) Solve  $3x - 10 = x + 30$
- 12) Solve the inequality  $3x - 2 > x + 7$
- 13) Solve the inequality  $\frac{2x}{3} < 10$

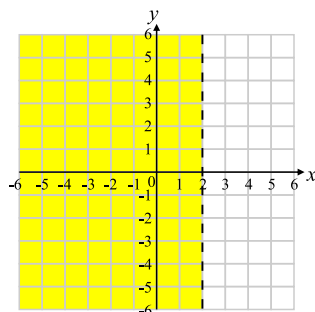
## Inequalities on a Graph

1) For each question below, find the inequality that is represented by the shaded region.

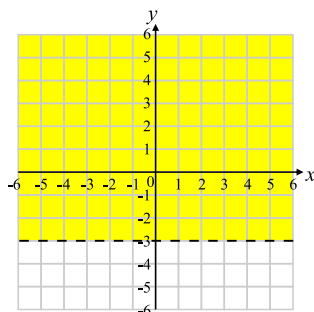
a)



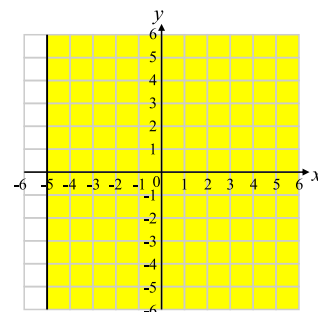
b)



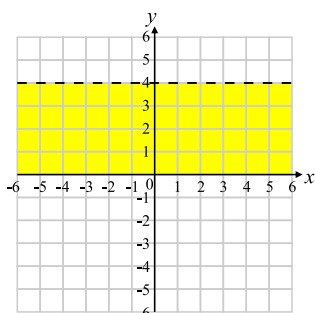
c)



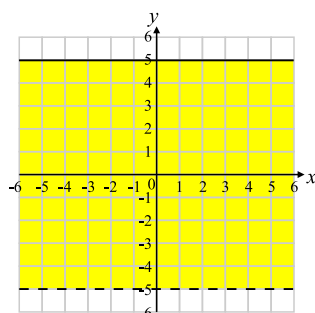
d)



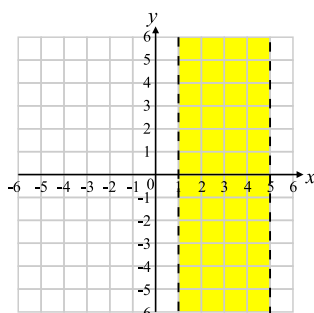
e)



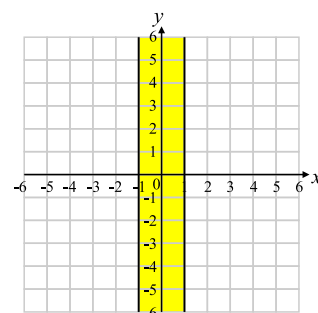
f)



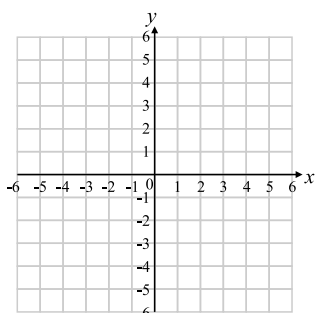
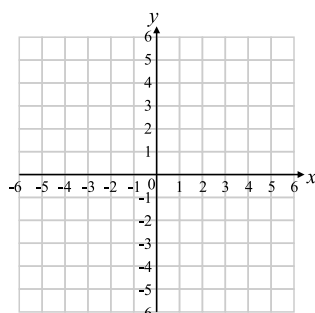
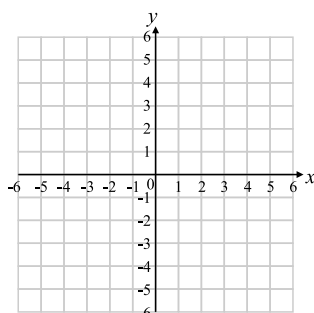
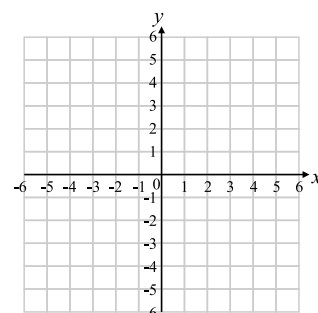
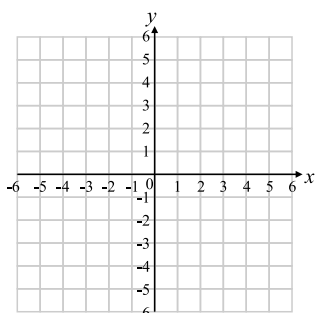
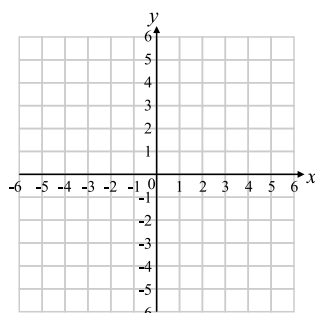
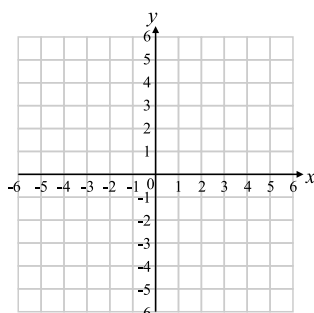
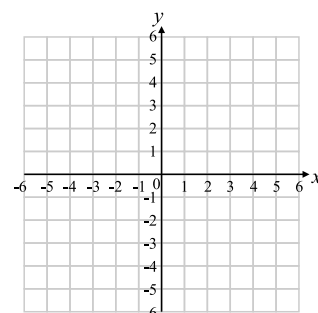
g)



h)



2) For each question below, shade the region represented by the inequality given.

a)  $x \geq 3$ b)  $y < 1$ c)  $x < -4$ d)  $y \geq 2$ e)  $-1 \leq x \leq 4$ f)  $-3 < y < 4$ g)  $-2 \leq y < 2$ h)  $-5 < x \leq -1$ 



- 1) An ice hockey puck has a volume of  $113 \text{ cm}^3$ .  
It is made out of rubber with a density of  $1.5 \text{ grams per cm}^3$ .  
Work out the mass of the ice hockey puck.



- 2) An apple has a mass of  $160 \text{ g}$  and a volume of  $100 \text{ cm}^3$ .  
Find its density in  $\text{g/cm}^3$ .



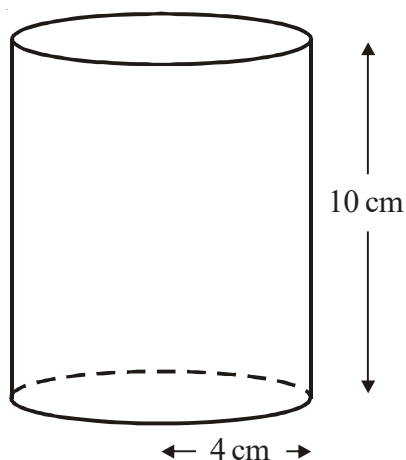
- 3) A steel ball has a volume of  $1500 \text{ cm}^3$ .  
The density of the ball is  $95 \text{ g/cm}^3$ .  
Find the mass of the ball **in kg**.



- 4) The mass of a bar of chocolate is  $1800 \text{ g}$ .  
The density of the chocolate is  $9 \text{ g/cm}^3$ .  
What is the volume of the bar of chocolate?



- 5) A solid cylinder has a radius of  $4 \text{ cm}$  and a height of  $10 \text{ cm}$ .



- a) Work out the volume of the cylinder.  
Give your answer correct to 3 significant figures.

The cylinder is made of wood.  
The density of the wood is  $0.7 \text{ grams per cm}^3$

- b) Work out the mass of the cylinder.  
Give your answer correct to 3 significant figures.

## Compound Units

$\text{Pressure} = \frac{\text{Force}}{\text{Area}}$
--

- 1) Work out the **pressure** when the force is 150 newtons and the area is  $30\text{cm}^2$ .  
Circle your answer.
- A.  $120\text{N/cm}^2$                       B.  $180\text{N/cm}^2$                       C.  $50\text{N/cm}^2$                       D.  $5\text{N/cm}^2$

- 2) Work out the **force** when the pressure is  $30\text{N/m}^2$  and the area is  $5\text{m}^2$ .  
Circle your answer.
- A. 150N                      B. 35N                      C. 25N                      D. 6N

- 3) A solid block exerts a force of 220 newtons on a surface area of  $100\text{cm}^2$ .  
Work out the pressure, giving the units of your answer.

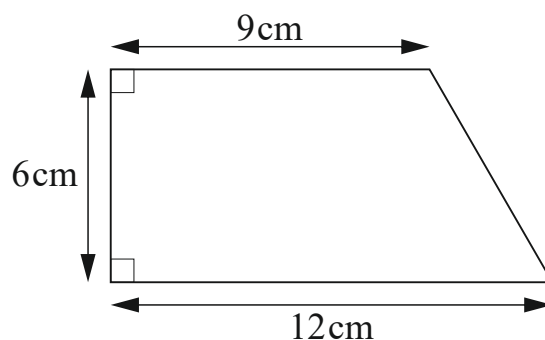
- 4) A box exerts a force of 100 newtons on a table.  
The pressure on the table as a result of the force applied by the box is  $5\text{N/cm}^2$ .  
Work out the surface area of the box that is in contact with the table.



- 5) A tank exerts a force of 600 newtons on the ground.  
The base of the tank in contact with the ground is a 2.5m by 1.2m rectangle.  
Work out the pressure applied to the ground by the tank.



- 6) A force is applied to the surface of this trapezium.  
The resulting pressure on the trapezium is  $5\text{N/cm}^2$ .  
Work out the force applied in newtons.

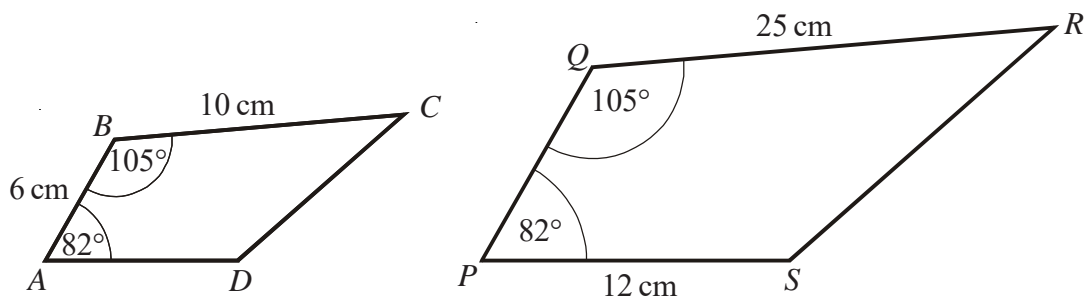




# Similar Shapes



1)

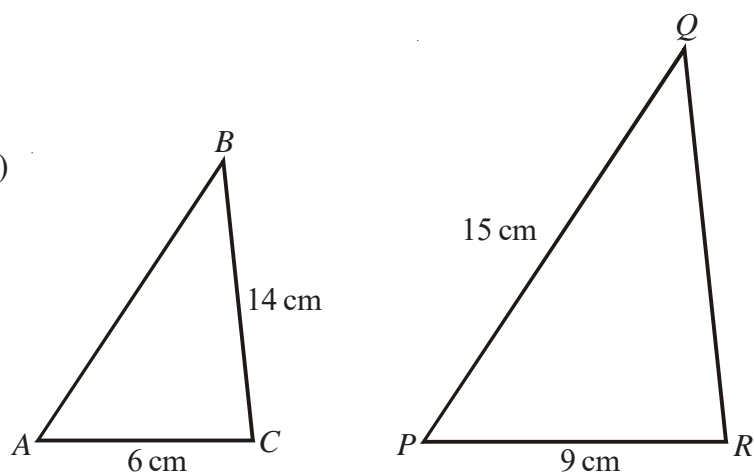


$ABCD$  and  $PQRS$  are mathematically similar.

- Find the length of  $PQ$ .
- Find the length of  $AD$ .



2)



Triangles  $ABC$  and  $PQR$  are mathematically similar.

Angle  $A$  = angle  $P$ .

Angle  $B$  = angle  $Q$ .

Angle  $C$  = angle  $R$ .

$AC = 6$  cm.

$BC = 14$  cm.

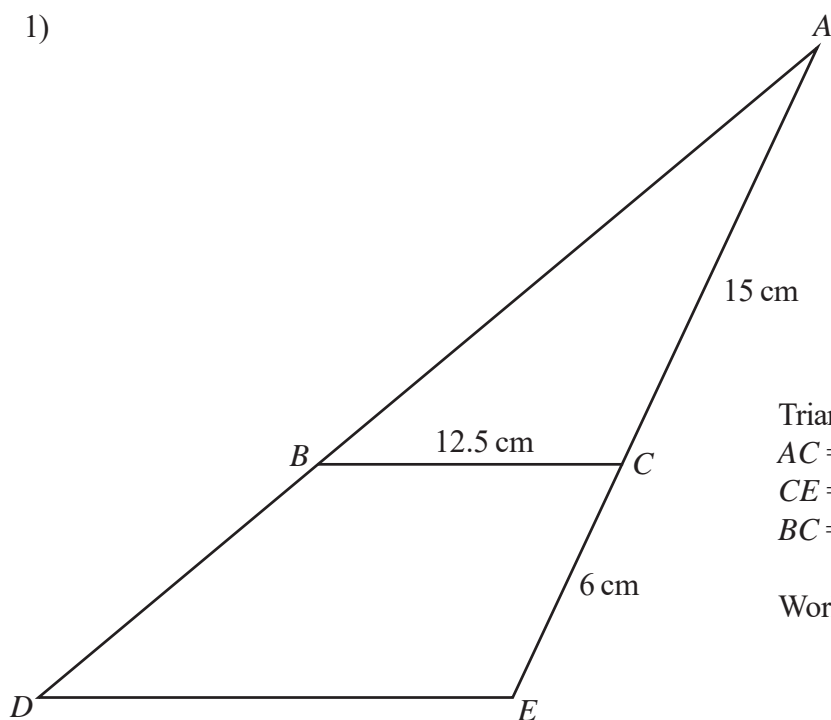
$PR = 9$  cm.

$PQ = 15$  cm

- Work out the length of  $QR$ .
- Work out the length of  $AB$ .



1)



Triangle  $ABC$  is similar to triangle  $ADE$ .  
 $AC = 15$  cm.  
 $CE = 6$  cm.  
 $BC = 12.5$  cm.

Work out the length of  $DE$ .



2)  $ABC$  and  $AED$  are straight lines.

$EB$  is parallel to  $DC$ .

Angle  $ACD = 90^\circ$

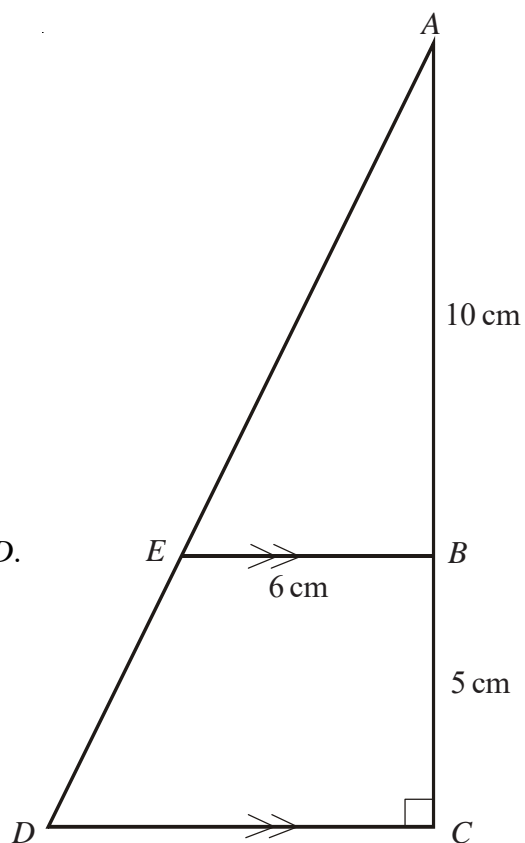
$AB = 10$  cm

$BC = 5$  cm

$EB = 6$  cm

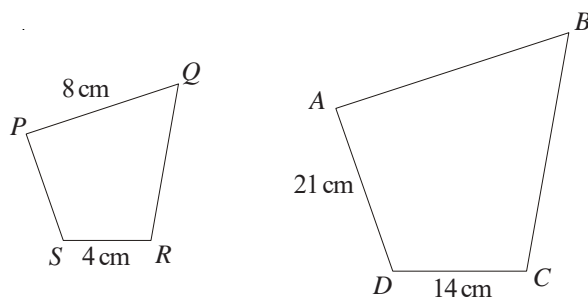
a) Work out the length of  $DC$ .

b) Work out the area of the trapezium  $EBCD$ .



# Similar Shapes

- 1) The diagram shows two quadrilaterals that are mathematically **similar**.

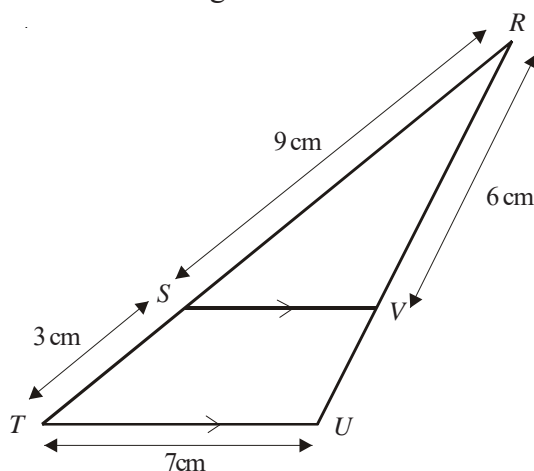


- Calculate the length of  $AB$
- Calculate the length of  $PS$



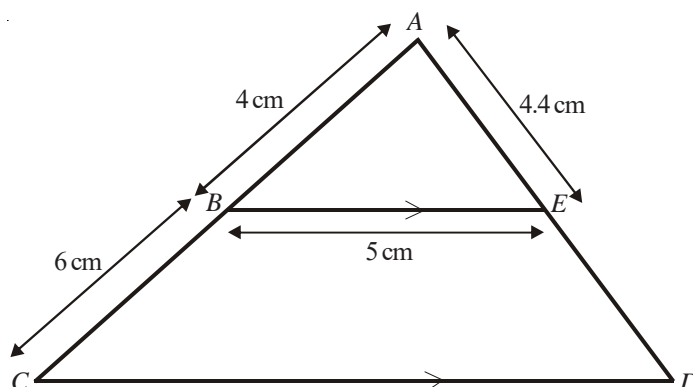
- 2)  $SV$  is parallel to  $TU$ .  
 $RST$  and  $RVU$  are straight lines.  
 $RS = 9$  cm,  $ST = 3$  cm,  $TU = 7$  cm,  $RV = 6$  cm

Calculate the length of  $VU$ .



- 3)  $BE$  is parallel to  $CD$ .  
 $ABC$  and  $AED$  are straight lines.  
 $AB = 4$  cm,  $BC = 6$  cm,  $BE = 5$  cm,  $AE = 4.4$  cm

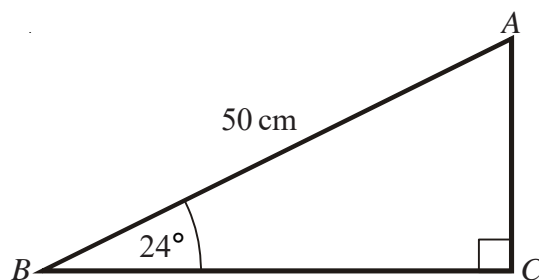
- Calculate the length of  $CD$ .
- Calculate the length of  $ED$ .



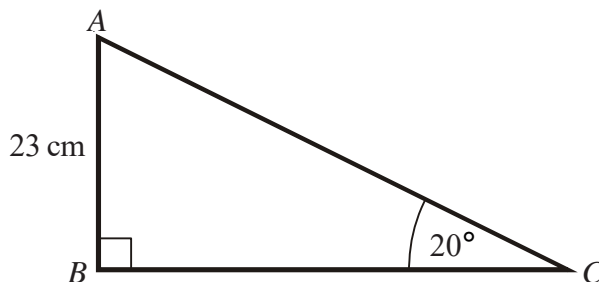
## Trigonometry



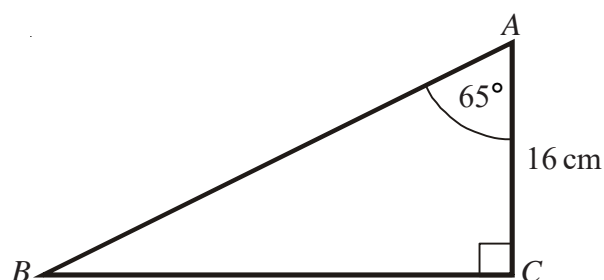
- 1)  $ABC$  is a right-angled triangle.  
 $AB = 50$  cm.  
 Angle  $ABC = 24^\circ$   
 Work out the length of  $BC$ .  
 Give your answer correct to 1 decimal place.



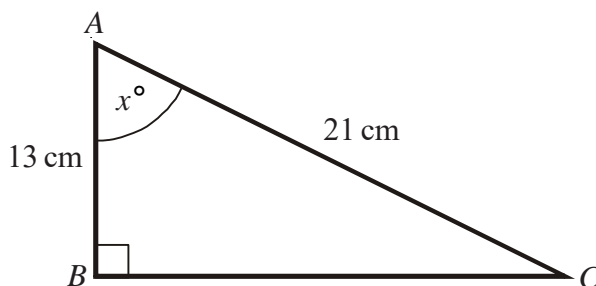
- 2)  $ABC$  is a right-angled triangle.  
 $AB = 23$  cm.  
 Angle  $BCA = 20^\circ$   
 Work out the length of  $AC$ .  
 Give your answer correct to 1 decimal place.



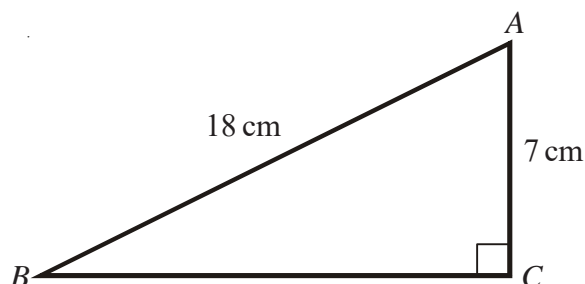
- 3)  $ABC$  is a right-angled triangle.  
 $AC = 16$  cm.  
 Angle  $CAB = 65^\circ$   
 Work out the length of  $BC$ .  
 Give your answer correct to 1 decimal place.



- 4)  $ABC$  is a right-angled triangle.  
 $AB = 13$  cm.  
 $AC = 21$  cm.  
 Work out the size of angle  $x$ .  
 Give your answer correct to 1 decimal place.



- 5)  $ABC$  is a right-angled triangle.  
 $AB = 18$  cm.  
 $AC = 7$  cm.  
 Work out the size of angle  $ABC$ .  
 Give your answer correct to 1 decimal place.

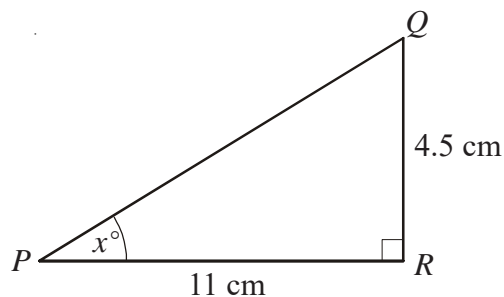


## Trigonometry



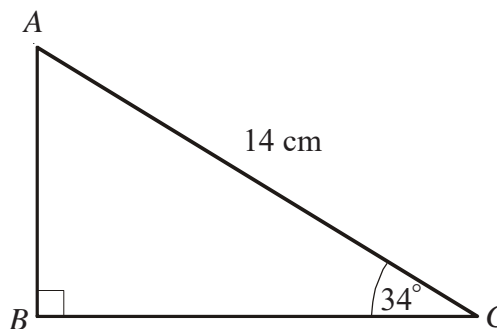
- 1)  $PQR$  is a right-angled triangle.  
 $PR = 11$  cm.  
 $QR = 4.5$  cm  
Angle  $PRQ = 90^\circ$

Work out the value of  $x$ .  
Give your answer correct to 1 decimal place.



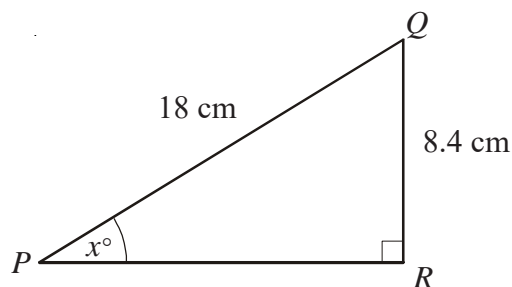
- 2)  $AC = 14$  cm.  
Angle  $ABC = 90^\circ$   
Angle  $ACB = 34^\circ$

Calculate the length of  $BC$ .  
Give your answer correct to 3 significant figures.



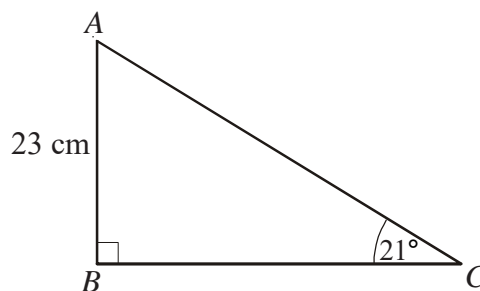
- 3)  $PQR$  is a right-angled triangle.  
 $PQ = 18$  cm.  
 $QR = 8.4$  cm  
Angle  $PRQ = 90^\circ$

Work out the value of  $x$ .  
Give your answer correct to 1 decimal place.



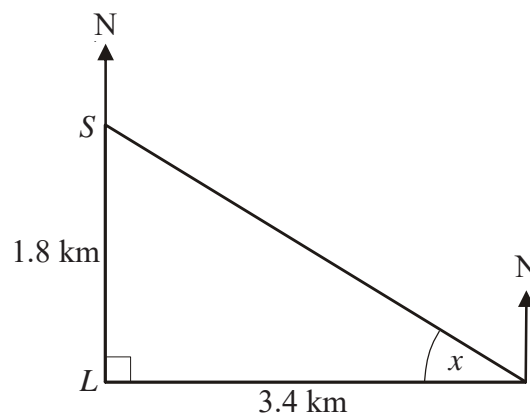
- 4)  $AB = 23$  cm.  
Angle  $ABC = 90^\circ$   
Angle  $ACB = 21^\circ$

Calculate the length of  $AC$ .  
Give your answer correct to 3 significant figures.



- 5) A lighthouse,  $L$ , is 3.4 km due West of a port,  $P$ .  
A ship,  $S$ , is 1.8 km due North of the lighthouse,  $L$ .

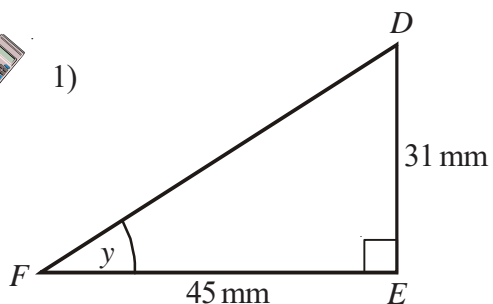
Calculate the size of the angle marked  $x$ .  
Give your answer correct to 3 significant figures.



# Trigonometry



1)



$DEF$  is a right-angled triangle.

$$DE = 31 \text{ mm}$$

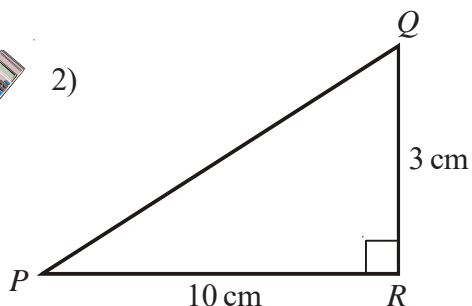
$$FE = 45 \text{ mm}$$

Calculate the size of angle  $y$ .

Give your answer correct to one decimal place.



2)



$PQR$  is a right-angled triangle.

$$QR = 3 \text{ cm}$$

$$PR = 10 \text{ cm}$$

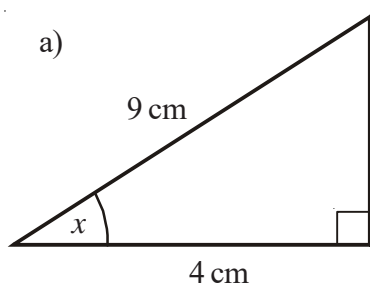
Work out the size of angle  $RPQ$ .

Give your answer correct to three significant figures.



3)

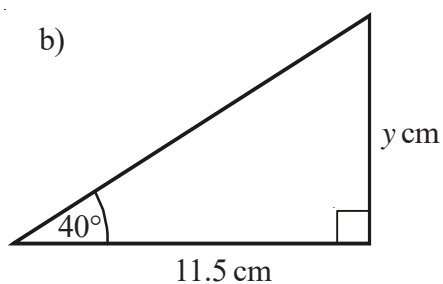
a)



Calculate the size of the angle marked  $x$ .

Give your answer correct to one decimal place.

b)



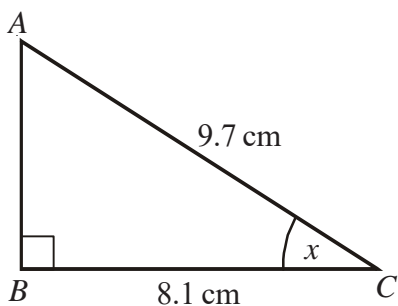
Calculate the value of  $y$ .

Give your answer correct to one decimal place.

# Trigonometry



1)



$ABC$  is a right-angled triangle.

$$AC = 9.7 \text{ cm}$$

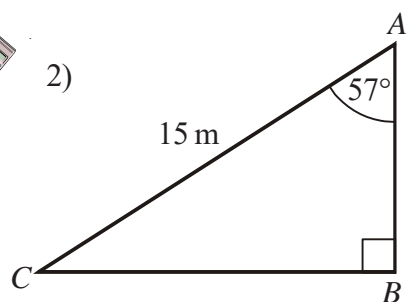
$$BC = 8.1 \text{ cm}$$

Calculate the size of the angle marked  $x$ .

Give your answer correct to three significant figures.



2)



$ABC$  is a right-angled triangle.

$$AC = 15 \text{ m}$$

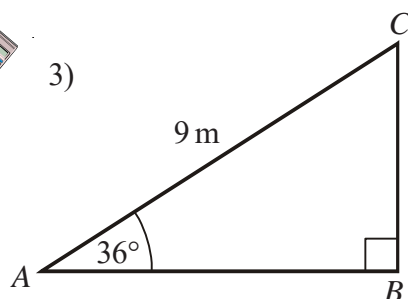
$$\text{Angle } CAB = 57^\circ$$

Calculate the length of  $AB$ .

Give your answer correct to three significant figures.



3)



$ABC$  is a right-angled triangle.

$$AC = 9 \text{ m}$$

$$\text{Angle } CAB = 36^\circ$$

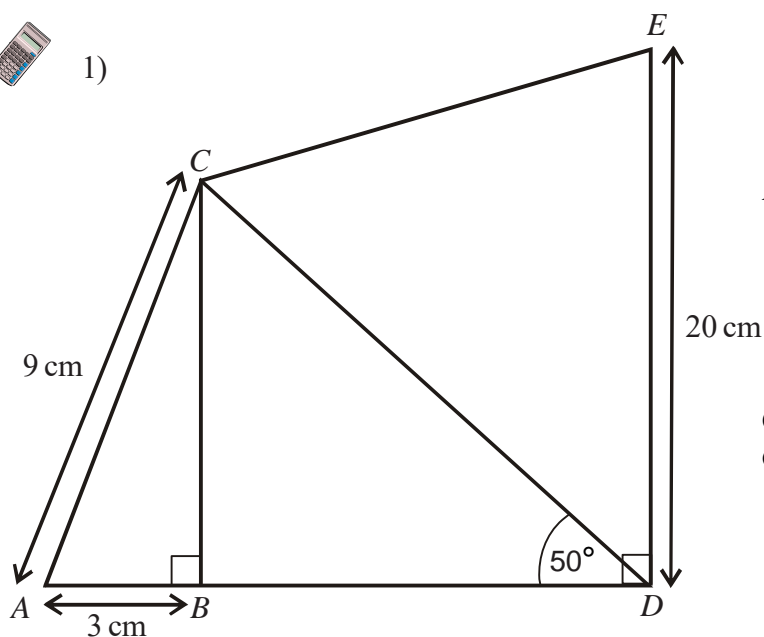
Calculate the length of  $AB$ .

Give your answer correct to three significant figures.

# Trigonometry



1)

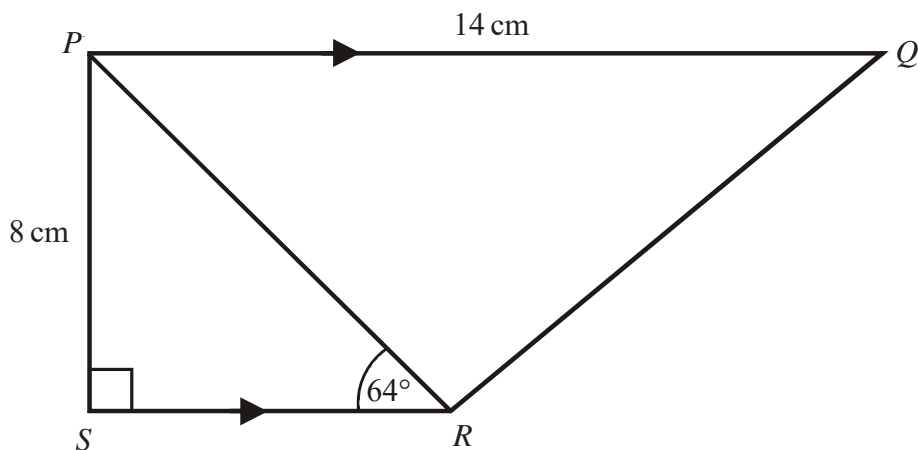


$AC = 9 \text{ cm}$   
 $AB = 3 \text{ cm}$   
 $DE = 20 \text{ cm}$   
 Angle  $ABC = \text{angle } CBD = \text{angle } BDE = 90^\circ$

Calculate the length of  $CD$ .  
 Give your answer to 3 significant figures.



2)



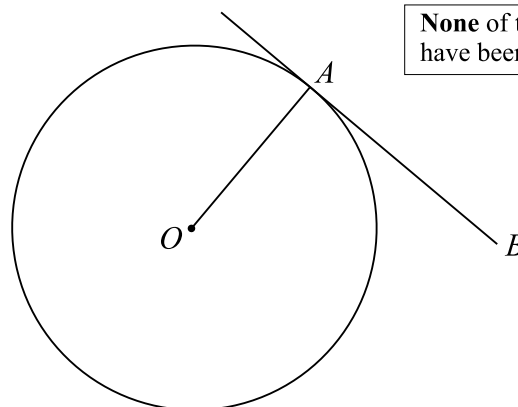
$PQRS$  is a trapezium.  
 $PQ$  is parallel to  $SR$ .  
 Angle  $PSR = 90^\circ$   
 Angle  $PRS = 64^\circ$   
 $PQ = 14 \text{ cm}$ .  
 $PS = 8 \text{ cm}$ .

Work out the length of  $PR$ .  
 Give your answer correct to 3 significant figures.



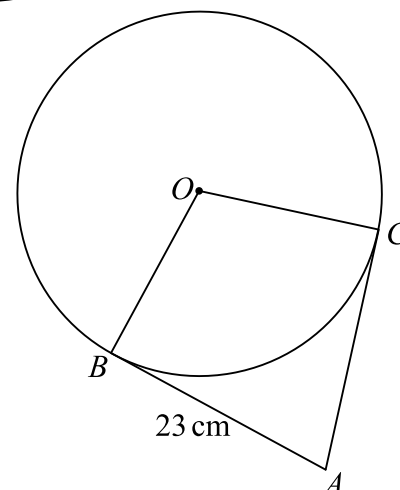
## Circle Theorems - Introduction

- 1)  $O$  is the centre of the circle.  
 $AB$  is a tangent to the circle.
- Write down the size of angle  $OAB$ .
  - Give a reason for your answer.

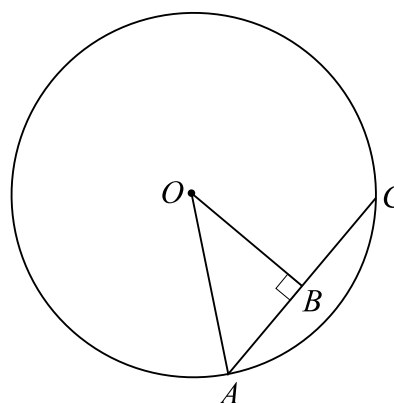


None of the diagrams have been drawn accurately.

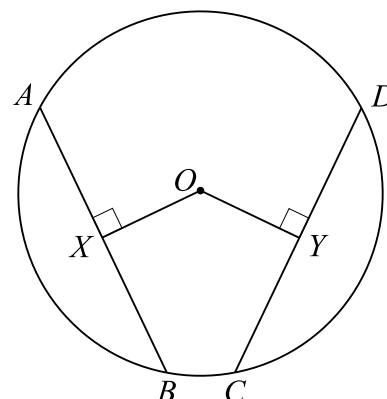
- 2)  $O$  is the centre of the circle.  
 $AB$  and  $AC$  are tangents to the circle.  
 $AB = 23$  cm
- Write down the length of  $AC$ .
  - Give a reason for your answer.
  - Write down the size of angle  $ACO$ .
  - Give a reason for your answer.



- 3)  $O$  is the centre of the circle.  
 $AC$  is a chord.  
 $AB = 8$  cm
- Write down the length of chord  $AC$ .
  - Give a reason for your answer.



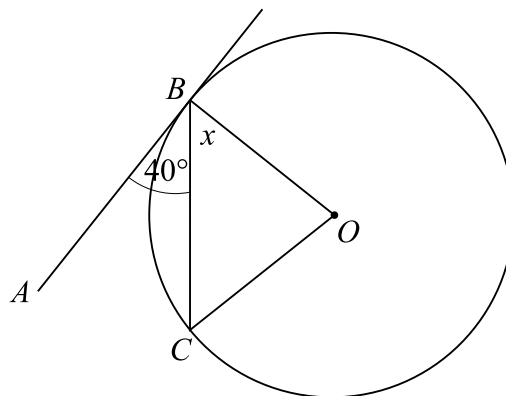
- 4)  $O$  is the centre of the circle.  
 $AB$  and  $CD$  are chords,  $AB = 12$  cm.  
 $OX = OY$
- Write down the length of chord  $CD$ .
  - Give a reason for your answer.



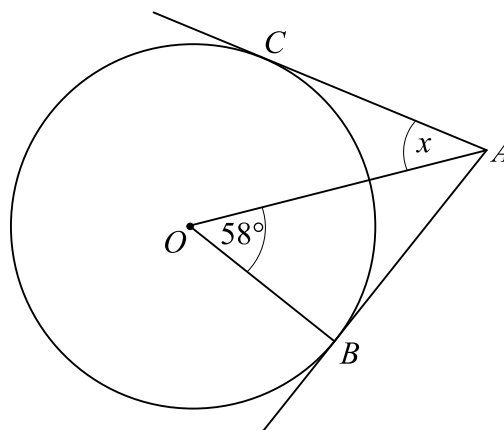
## Circle Theorems - Introduction

None of the diagrams have been drawn accurately.

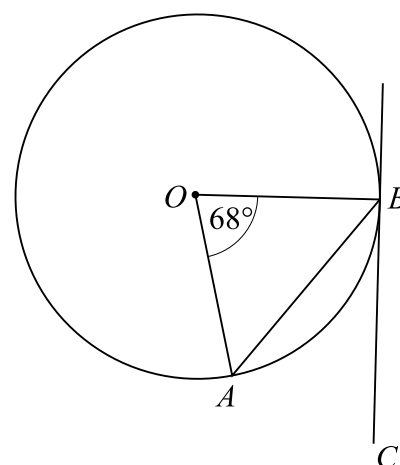
- 1)  $O$  is the centre of the circle.  
 $AB$  is a tangent to the circle.  
 Angle  $ABC = 40^\circ$   
 Work out the size of angle  $x$ .



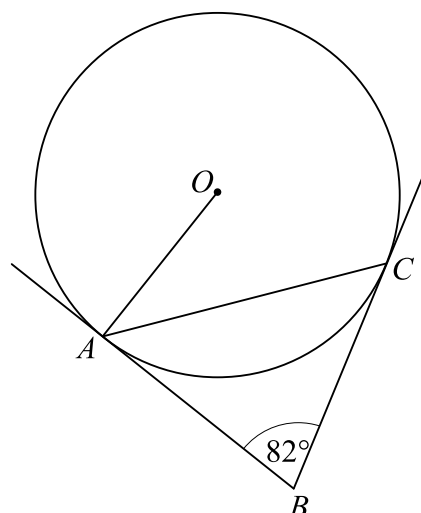
- 2)  $O$  is the centre of the circle.  
 $AB$  and  $AC$  are tangents to the circle.  
 Angle  $BOA = 58^\circ$   
 Work out the size of angle  $x$ .



- 3)  $O$  is the centre of the circle.  
 $CB$  is a tangent to the circle.  
 Angle  $AOB = 68^\circ$   
 Work out the size of angle  $ABC$ .  
 Give a reason for each step of your working.



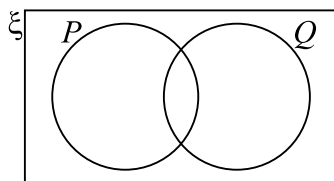
- 4)  $O$  is the centre of the circle.  
 $BA$  and  $BC$  are tangents to the circle.  
 Angle  $ABC = 82^\circ$   
 Work out the size of angle  $OAC$ .  
 Give a reason for each step of your working.



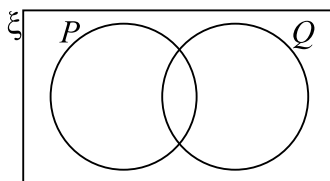
## Venn Diagrams - Notation

- 1) Shade the region represented by each set notation.

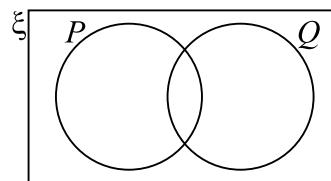
a)  $P \cup Q$



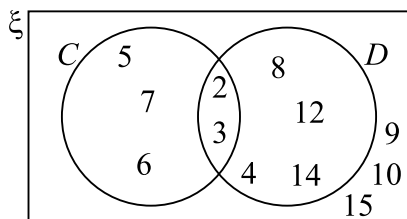
b)  $Q'$



c)  $P \cap Q$



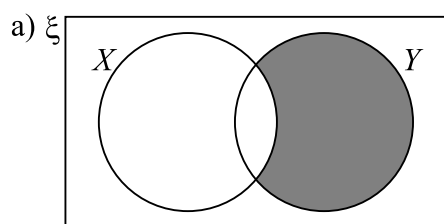
- 2) Here is a Venn diagram.



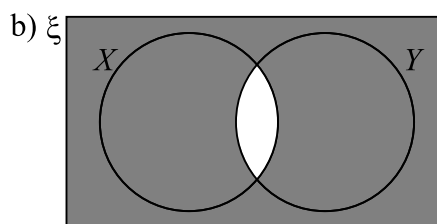
- a) List the elements of  $C \cap D$ .

- b) List the elements of  $(C \cup D)'$ .

- 3) For each diagram below, circle the option that represents the shaded region.



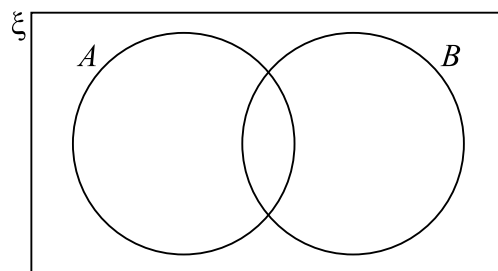
- A      B      C      D  
 $X'$      $X \cup Y'$      $X' \cap Y$      $X' \cap Y'$



- A      B      C      D  
 $X \cap Y$      $(X \cap Y)'$      $X' \cap Y'$      $(X \cup Y)'$

- 4)  $\xi = \{\text{odd numbers between 0 and 22}\}$   
 $A = \{5, 15\}$   
 $B = \{3, 5, 7, 11, 13, 17, 19\}$

- a) Complete the Venn diagram to represent this information.



- b) List the elements that belong to  $B'$ .

## Estimate for the Mean



- 1) Sindy recorded the time, in minutes, that her train was late over 100 days. Information about these times is shown in the table.

Time ( $t$ minutes)	Frequency		
$0 < t < 6$	15		
$6 < t < 12$	23		
$12 < t < 18$	28		
$18 < t < 24$	19		
$24 < t < 30$	15		

Calculate an estimate for the mean time that her train was late.  
Give your answer to 1 decimal place.



- 2) The table shows some information about the heights ( $h$  cm) of 100 plants.

Height ( $h$ cm)	Frequency		
$120 < h < 130$	9		
$130 < h < 140$	18		
$140 < h < 150$	27		
$150 < h < 160$	31		
$160 < h < 170$	15		

- a) Find the class interval in which the median lies.  
  
b) Work out an estimate for the mean height of the plants.



- 3) The table gives information about the number of books sold in a shop during each of the last 30 weeks.

Number of books ( $n$ )	Frequency		
$0 < n < 40$	2		
$40 < n < 80$	6		
$80 < n < 120$	13		
$120 < n < 160$	6		
$160 < n < 200$	3		

Calculate an estimate for the mean number of books sold each week.  
Give your answer correct to 1 decimal place.